THEORETICAL PREDICTION OF ACOUSTIC-GRAVITY PRESSURE WAVEFORMS GENERATED BY LARGE EXPLOSIONS IN THE ATMOSPHERE

by

Allan D. Pierce and Joe W. Posey

Department of Mechanical Engineering
Massachusetts Institute of Technology

Contract No. F19628-67-C-0217

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Work Unit No. 76391001

FINAL REPORT

Period Covered: February 1, 1967 through January 31, 1970

30. April, 1970

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Pressure Waveforms Generated by
Large Explosions in the Atmosphere

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Department of Mechanical Engineering Massachusetts Institute of Technology Cambridge, Massachusetts 02139

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ABSTRACT

A computer program is described which enables one to compute the pressure waveform at a distant point following the detonation of a nuclear explosion in the atmosphere. The theoretical basis of the program and the numerical methods used in its formulation are explained; a deck listing and instructions for the program's operation are included. The primary limitation on the program's applicability to realistic situations is that the atmosphere is assumed to be perfectly stratified. However, the temperature and wind profiles may be arbitrarily specified. Numerical studies carried out by the program show some discrepancies with previous computations by Harkrider for the case of an atmosphere without winds. These discrepancies are analyzed and shown to be due to different formulations of the source model for a nuclear explosion. Other numerical studies explore the effects of various atmospheric parameters on the waveforms. In the remainder of the report, two alternate theoretical formulations of the program are described. The first of these is based on the neglect of the vertical acceleration term in the equations of hydrodynamics and allows a solution by Cagniard's integral transform technique. The second is based on the hypothesis of propagation in a single guided mode and permits a study of the effects of departures from stratification on the waveforms.

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Chapter I

INTRODUCTION

1.1 SCOPE OF THE REPORT

The present report summarizes investigations carried out by the authors during the years 1966-1968 on the propagation of low frequency pressure disturbances under Air Force Contract No. F19628-67-C-0217 with the Air Force Cambridge Research Laboratories, Bedford, Massachusetts. The study performed was theoretical in nature.

The principal problem which the authors chose to study was that of the theoretical prediction of the pressure waveform (acoustic pressure versus time) which would be detected near the ground at a large horizontal distance (between 500 and 20,000 km) from a nuclear explosion in the lower atmosphere. This problem was selected for several reasons.

Nuclear explosions, particularly those in the megaton range, excite waves whose dominant periods lie in the so-called acoustic-gravity range (roughly between 1 and 20 minute periods). These acoustic-gravity waves are relatively little understood at present and exhibit many interesting properties which invite serious inquiry.

Of all the known sources which may excite acoustic-gravity waves capable of being detected at large distances, the nuclear explosions correspond most closely to point sources. This allows a considerable simplification in the analysis. Furthermore, the nuclear explosions are better understood and may be described in a more detailed quantitative fashion than would be natural sources such as volcano eruptions, weather disturbances, etc.

A considerable amount of data on pressure waveforms recorded following nuclear explosions exists and is published in the scientific literature. Since the explanation of data should be a principal reason for any theoretical development, it is natural to begin with the study of phenomena for which a large bulk of systematically obtained data exists.

It would appear that the possible application of a theory of waves generated by nuclear explosions to the interpretation of experimental data would be of some practical importance, either as an aid in a possible acoustic detection system of nuclear explosions, or as a means of inferring some of the as yet imperfectly known properties of the earth's upper atmosphere. In this respect, the first step would clearly be the development of a deterministic theory which, given certain properties of the explosion and of the atmosphere, allows one to predict the waveforms.

It should be mentioned at the outset that the problem under consideration has been of considerable interest to a large segment of the scientific community for some time and that the problem has an illustrious background. The present report merely reports a continuation of one facet of a lengthy pattern of research which has been carried on by a large number of investigators in the past. In a somewhat restricted sense, the work reported here is a continuation of work done by one of the authors (A. Pierce) under Air Force Contract No. AF 19 (628) - 3891 with Avco Corporation during 1964-1966.

A major part of the present report is concerned with the explanation, presentation, and description of a computer program (which we refer to by the name INFRASONIC WAVEFORMS) which was developed during the course of the contract. This program is based on a theory which assumes the atmosphere to be perfectly stratified and to have somewhat arbitrary temperature and wind velocity profiles. This theory, described in some detail in Chapter II, is based on a number of approximations which restrict its application to waveforms recorded near the ground at large distances from low to moderate altitude nuclear explosions. In addition, the computational method restricts the application of the program to the earliest portion of the dominant signal, which travels with a speed roughly equal to the speed of sound at the ground.

Chapter III gives a user's manual for the program, with instructions for preparing input, description of the possible output of the program, and sample input and output. A deck listing of the program is given in Appendix B.

In Chapter IV, some numerical studies made using the program are reported. These studies include the explanation of some discrepancies with previous computations by Harkrider for the case of atmospheres without winds; the discrepancies being due to differences of methods of incorporating a source model into the formulation. A discussion, with numerical examples, is also given of the effects of variations in parameters describing the atmosphere on the waveforms. There we conclude that the physical significance of the individual guided modes predicted for a given atmosphere model is extremely limited and that the total waveform

is relatively insensitive to variations in the parameters characterizing the atmosphere. An extensive comparison with data remains to be carried out. The only example presented in this report is for the case recorded at Berkley, California, on 30 October, 1962 following an explosion 13.60° N. 172.22° W. near Johnson Island. We chose this record as it appeared to be the least affected by ambient noise of the records exhibited by Donn and Shaw. Although the choice may therefore appear somewhat fortuitous, the agreement of the theoretically obtained waveform with this record would appear, from a subjective standpoint, to be extremely good.

The following two chapters, V and VI, present two alternate theoretical formulations of the problem of predicting waveforms. The first of these, described in Chapter V, represents an application of various mathematical techniques generally known as Cagniard's method to the idealized case when the vertical acceleration term in the equations of hydrodynamics is neglected at the outset. The second, described in Chapter VI, is based on the assumption that the propagation is predominantly in a single quasi-mode which resembles Lamb's mode for an isothermal atmosphere. This theory represents an extension of some ideas recently expressed by Bretherton (1969) and by Garrett (1969), and shows considerable promise in that it is not restricted to a stratified atmosphere or to linear equations. The quantitative implications of these theories are not explored, but are discussed in the present report with the hope that they may be of interest to other researchers concerned with acoustic-gravity wave propagation. At the time of this writing, we are especially optimistic about the single mode theory and hope to have some quantitative assessment of its applicability in the very near future.

Chapter II

THEORETICAL BASIS OF INFRASONIC WAVEFORMS

2.1 SUMMARY OF THE THEORETICAL MODEL

The mathematical model on which the computer program INFRASONIC WAVEFORMS is based is briefly summarized here. The geometry adopted (Fig. 2-1) is that of a stratified atmosphere above a rigid flat earth. The ambient atmosphere is described by a sound speed profile c(z) and a wind velocity profile v(z), where z is height above the ground. Both of these profiles are assumed independent of horizontal coordinates x and y and of time t. Moreover, the ambient winds are assumed to be horizontal.

The air comprising the atmosphere is taken as an ideal gas of constant specific heat ratio γ = 1.4 and of constant mean molecular weight. Thus the ambient pressure p and density p satisfy the hydrostatic relation and the ideal gas law

$$p_{o}(z) = p_{o}(0) \exp \left[-\int_{0}^{z} (\gamma g/c^{2}) dz \right]$$
 (2.1.1)

$$\rho_0 = \gamma p_0/c^2$$
 (2.1.2)

where $p_0(0)$ (taken as 10^6 dynes/cm²) is the ambient pressure at the ground. Since the propagation is considered to be predominantly in the lower atmosphere, the acceleration of gravity g is taken to be constant with height and equal to the typical earth surface value of .0098 km/sec².

The neglect of earth curvature is in accordance with the results of previous studies by Weston (1961) and by Harkrider (1964) which indicate that the curvature of the earth can approximately be accounted for by multiplying the flat earth waveform by the factor

$$[(r/r_e)/\sin(r/r_e)]^{1/2}$$
 (2.1.3)

where r is the great circle propagation distance and r is the radius of the earth. This result holds in particular for waves which have traveled somewhat less than one-fourth the circumference of the earth. Since the intended application of the program is for the interpretation of data recorded at distances less

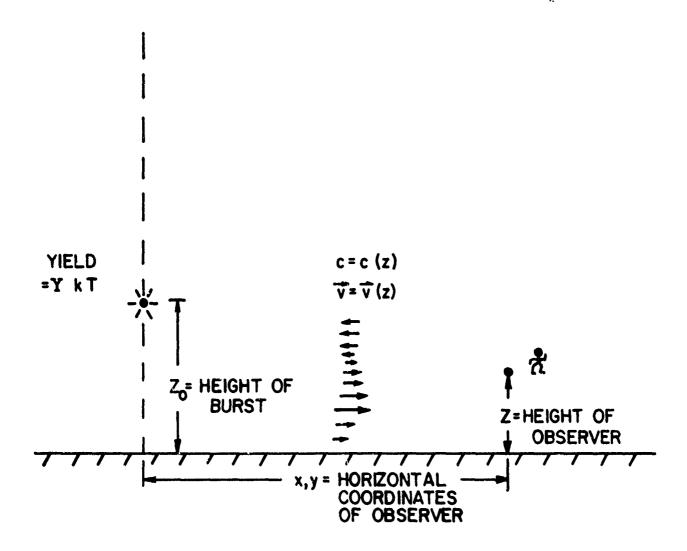


Figure 2-1. Sketch showing the general model adopted in the theoretical formulation. An explosion of yield Y is at height z above a flat rigid ground in an atmosphere with stratified sound speed c and horizontal wind velocity v. The wave disturbance is detected by an observer with coordinates (x,y,z).

than this and since the factor above does not vary appreciably from 1 for such a range of distances, this correction is neglected. In general, we consider such a correction to be minor compared with the inevitable uncertainties in the source model and the ambient atmosphere.

In order that the model be amenable to computation, we consider the propagation to be governed by the linearized equations of hydrodynamics. This would appear to be a fair approximation at large distances from the explosion, although it is clearly not applicable close-in. It is therefore implicitly assumed that any near field nonlinear effects may be taken into account by a judiciously chosen source model.

The source model adopted here (whose rationale is discussed at some length in the next section) is that where the presence of the source and the near field nonlinear effects are represented by a time-varying point energy source term added to the right hand side of the linearized equation which corresponds to energy conservation. Thus the governing equations (which are to be satisfied everywhere above the ground) are taken to be of the form

$$\rho_0 \overrightarrow{D_t^{\dagger}} + (\overrightarrow{u} \cdot \nabla) \overrightarrow{v} = - \nabla p - g \rho \overrightarrow{e}_z$$
 (2.1.4a)

$$D_{\mathbf{t}}\rho + \nabla \cdot (\rho_{\mathbf{0}}\mathbf{u}) = 0$$
 (2.1.4b)

$$\left(D_{\mathbf{t}}^{p} + \mathbf{u} \cdot \nabla p_{o}\right) - c^{2}\left(D_{\mathbf{t}}^{\rho} + \mathbf{u} \cdot \nabla \rho_{o}\right) \\
= 4\pi c^{2} f_{E}(\mathbf{t}) \delta(\mathbf{r} - \mathbf{r}_{o}) \qquad (2.1.4c)$$

where

$$D_{t} = (\partial/\partial t) + \dot{\mathbf{v}} \cdot \nabla$$

is the time derivative corresponding to an observer moving with the ambient wind. In the above, p, ρ , and u represent the deviations of pressure, density, and fluid velocity from their ambient values. The quantity e_z is the unit vector in the vertical direction, while e_z denotes the source location.

The time-dependent quantity $f_E(t)$ represents a function characteristic of the source. For convenience of referral, we state here our choice of this function prior to a discussion of

the rationale behind such a choice. We take

$$f_E(t) = \int_0^t f_E^*(t) dt$$
 (2.1.5a)

where

$$f_E^*(t) = Y_{KT}^{1/3}[p_o(z_o)/p_o(0)]^{2/3}L_sf_{1KT}(t/\lambda_oY_{KT}^{1/3}])$$
 (2.1.5b)

Here Y_{KT} is the explosion yield in KT, $p_0(z_0)$ is the ambient pressure at the height of burst, and λ_0 is a scaling factor given by

$$\lambda_{o} = [c(0)/c(z_{o})][p_{o}(0)/p_{o}(z_{o})]^{1/3}$$
 (2.1.6)

The quantity L is a length identically equal to 1 km, which we include in the theory for dimensional "purity". The function $f_{1KT}(t)$ is given by

$$f_{1KT}(t) = (P_g)(1 - t/t_g)e^{-t/t_g} U(t)$$
 (2.1.7)

where

$$P_s = 1.61 \times 34.45 \times 10^3 \text{ dynes/cm}^2$$

$$t_s = 0.48 \text{ sec.}$$

Here U(t) is the Heaviside unit step function and z denotes the height of burst.

In the actual computation, the source location r is taken to be a fixed point in space. An alternative assumption which might seem more plausible is to take the source as moving with the ambient wind at the height z of burst. However, the results of the computation should be insensitive as to just which assumption is made. This follows since we limit our analysis to disturbances which travel with speeds near the speed of sound near the ground and since the wind speeds are invariably much less than the sound speed. Any phenomenon analogous to a doppler shift would undoubtedly be smaller than could feasibly be detected by experiment.

Boundary conditions on Eqs. (2.1.4) are that u = 0 at the ground z = 0 and that of causality (no disturbance in the far

field before $f_E(t)$ first becomes nonzero). The time origin here is not considered of too much relevance. With the definition given for $f_E(t)$, it is approximately (the discrepancy being due to nonlinear effects) equal to the time of detonation. We also take the source location to be on the z axis $(x_0 = y_0 = 0)$. Generally, we consider the +x axis to point eastward, and the +y axis to point northward.

2.2 THE SOURCE MODEL

Here we summarize the rationale behind the choice of the source model given in the preceding section. The discussion partly follows the development previously given by Pierce (1968).

We consider a basic nonlinear hydrodynamics model of a nuclear explosion consisting of an initially isothermal sphere of vanishingly small radius in an unbounded homogeneous atmosphere with negligible gravity. The initial isothermal sphere has ambient density and fluid velocity, but is assumed to have very high temperature and pressure. The total chermal energy (the specific heat of air is assumed independent of temperature) inside the sphere is denoted by E_h, which represents the total hydrodynamic energy released by the explosion. This, according to what is given in Glasstone's text (1962) should be roughly 1/2 of the total energy of the explosion.

The pressure waveform of the explosion in this idealized model can easily be shown to correspond to hydrodynamic scaling, i.e.

$$p = p_0 F(R/\lambda, ct/\lambda)$$
 (2.2.1)

where p $_{\mbox{\scriptsize 0}}$ and c are ambient pressure and sound speed, F is a universal function, and λ is a characteristic length given by

$$\lambda = (E_{hy}/p_o)^{1/3}$$
 (2.2.2)

Experiment and numerical computations show that at moderate distances (between 3 and 10λ from a nuclear explosion) the time dependence of the blast overpressure is approximately of the form (t relative to time of shock arrival)

$$p = (P)(1 - t/\tau)e^{-t/\tau}U(t)$$
 (2.2.3)

where P and T are functions of distance. According to Eq.

(2.2.1) above, we may take

$$\tau = (\lambda/c)A(R/\lambda) \qquad (2.2.4a)$$

$$P = p_0 B(R/\lambda) \qquad (2.2.4b)$$

where A and B are universal functions of (R/λ) . It is clear, since the far field propagation should be governed by linear acoustics, that A should at large R be a relatively slowly varying function of R/λ and that, at large R, B should be approximately (spherical spreading)

$$B \stackrel{\sim}{\sim} E_{\mathbf{g}} \lambda / R \tag{2.2.5}$$

where B_{α} is a very slowly varying function of R/λ .

The basic idea in our source term selection is that $f_E(t)$ in Eq. (2.1.4c) should be such that the solution of the linearized equations of hydrodynamics with the neglect of gravity and winds and for the same uniform ambient atmosphere should agree with Eq. (2.2.1) at moderate distances. The ambient atmosphere for this matching process is taken as that characteristic of the burst location. The solution of the linearized equations under the circumstances outlined above gives

$$p = R^{-1}f_{E}^{\dagger}(t - R/c)$$
 (2.2.6)

Thus, we would choose f_E^{\dagger} to be

$$f_E^{\dagger}(t) = p_0 E_0 \lambda (1 - t/\tau) e^{-t/\tau} U(t)$$
 (2.2.7)

The value of R/λ chosen for the matching is that corresponding to 1 km from a 1 KT explosion at sea level. According to Glasstone's text(1962) the value of P at one mile from such an explosion is 34.45×10^3 dynes/cm² while the value of τ is 0.48 sec. Since we expect the shock overpressure to fall off nearly inversely with R between 1 km and 1 mile we may take P to be $34.45 \times 10^{-3} \times 1.61$ dyne/cm² at one km. (Here we use the fact that 1 mile is 1.61 km.) Thus

$$p_0 B_0 \lambda = P_s L_s Y_{KT}^{1/3} [p_0(z_0)/p_0(0)]^{2/3}$$
 (2.2.8a)

$$\tau = Y_{KT}^{1/3}[p_o(0)/p_o(z_o)]^{1/3}[c(0)/c(z_o)]t_s \qquad (2.2.8b)$$

where P_S, L_s, and t_s are as defined in the preceding section and Y_{KT} is the energy yield in KT. Equations (2.2.7), (2.2.8a,b) agree with the definition of f_E^{\dagger} given in the preceding section.

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It now remains to examine the limitations of this source model. The basic assumption vehave made is that gravity and atmospheric gradients have relatively little effect on the early development of the blast wave. Another important assumption is that the initial fireball radius (before the shock detaches from the fireball) is sufficiently small that the radius of the initial sphere may be idealized as zero. This radius is conjectured by Pierce (1968) to be about .05 λ . The two approximations would clearly be inappropriate if the initial sphere radius were of the order of a scale height H . Thus one should certainly require $\lambda << 20~{\rm H}_{\rm c}$.

The establishment of a more realistic upper bound appears to be a somewhat complicated problem. Our best guess to date is that the positive phase duration by the time the blast overpressure is down to 10% ambient should be smaller than 1/10 the period (about 5 minutes) corresponding to Brunt's frequency $\omega_{\rm B}$ or Hines' $\omega_{\rm A}$. This would insure that there be negligible acoustic-gravity wave dispersion in the waveform while nonlinear effects are appreciable. This requirement gives roughly

$$Y_{MT} < 200 p_{A'TMOS}$$
 (2.2.9)

where $Y_{\rm MT}$ is the yield in MT and $p_{\rm ATMOS}$ is the ambient pressure at the height of burst in atmospheres [see Fig. 2-2]. We are not sure if this requirement is too conservative or too generous at present, but we offer it as a rough guideline to workers who might wish to use the program.

It should be noted that, in our source model, we have taken a point energy source rather than a point mass source. In actual practice, for the computation of ground level waveforms, it makes relatively little difference whether one adopts an energy source or a mass source. However, when one considers the fact that a nuclear explosion adds much energy but relatively little mass to the atmosphere, it is clear that the energy source model is a priori the more realistic. One of the authors (Pierce, 1968) has examined the relative merits of the two types of sources. He found the linear initial value problem of waves generated by the release of an initially isothermal sphere of ambient density was better represented by the point energy source. (It should be noted that the use of a point energy source rather than a point mass source is a relatively new concept in the theory of acoustic-gravity wave propagation. In particular, all of the

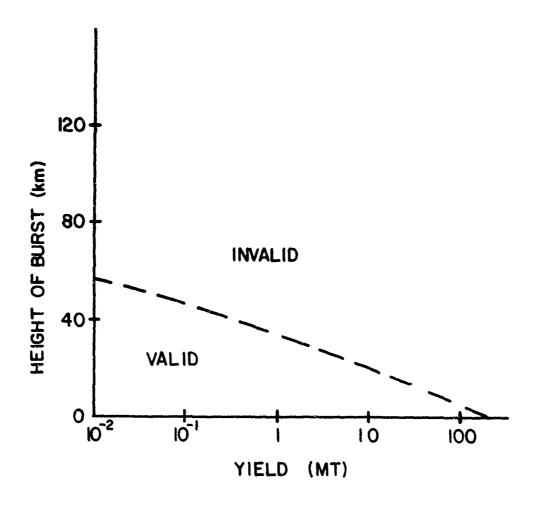


Figure 2-2. Estimated range of yields and source altitudes for which the effective point source model is valid.

authors' work prior to 1968 was based on the use of a point mass source model.]

One inherent defect in the model is that we have no mechanism for taking into account the far field nonlinear effects. In the related problem of sonic boom propagation, these are known not to be negligible. While they do not change waveforms appreciably over shorter distances, their accumulative effects can cause large distortions over very large distances. While these far field nonlinear effects should be examined in some detail in the future, we suspect that they are not as important in the infrasonic nuclear explosion problem as they are for sonic booms. The basis for this belief is that the inherent dispersive nature of the atmosphere as a waveguide tends to filter out the higher frequencies from the lowest part of the atmosphere and causes the lower frequencies to tend to arrive first. The nonlinear effects should be of lesser importance for the dominant lower frequency arrivals since the time for a wave peak to overtake a node is correspondingly longer for lower frequencies.

2.3 THE SOLUTION IN TERMS OF FOURIER TRANSFORMS

Since the linearized equations of hydrodynamics do not depend explicitly on time and, except at the source location, do not depend explicitly on horizontal position \bar{x} (due to the assumed stratification of the ambient atmosphere), one may express their solution as a triple Fourier transform over frequency ω and horizontal wave number vector components, k and k. Thus one may write the acoustic pressure p, for example, as

$$p = \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} e^{i\mathbf{k}\cdot\mathbf{x}} \left\{ \int_{-\infty+i\varepsilon}^{\infty+i\varepsilon} \hat{\mathbf{f}}_{E}(\omega)\hat{\mathbf{p}}(\omega,\mathbf{k},z,z_{0}) e^{-i\omega t} d\omega \right\} dk_{x} dk_{y}$$
(2.3.1)

Here $\hat{f}_E(\omega)$ is the Fourier transform of $f_E(t)$, i.e.

$$\hat{f}_{E}(\omega) = (2\pi)^{-1} \int_{-\infty}^{\infty} f_{E}(t) e^{i\omega t} dt \qquad (2.3.2)$$

The quantity ϵ is chosen sufficiently large that the integral over ω vanishes identically at times t before the source is first excited, if k and k are real. Thus the line is above the real axis should pass above all poles and branch lines of the inte-

grand. The function $\hat{p}(\omega, \vec{k}, z, z)$ must be defined such that this can be accomplished. Fourier transforms \vec{u} and \hat{p} are defined analogously.

A direct substitution of (2.3.1) and its counterparts for ρ and u into the linearized equations gives the following ordinary differential equations for $\hat{\rho}$, $\hat{\rho}$, and \hat{u} :

$$-\rho_0 i\Omega \hat{w} = -d\hat{p}/dz - g\hat{p}$$
 (2.3.3a)

$$-\rho_0 i \hat{\Omega}_{ij}^{\dagger} + \rho_0 \hat{\Theta} d\vec{v}/dz = -i \vec{k} \hat{\rho}$$
 (2.3.3b)

$$-i\Omega\hat{\rho} + \rho_0 \vec{k} \cdot \vec{u}_h + d(\rho_0 \hat{w})/dz = 0 \qquad (2.3.3c)$$

$$-i\Omega(\hat{p} - c^2\hat{p}) + \rho_0 \hat{w}[(\gamma - 1)g + dc^2/dz] = (c^2/\pi)\hat{f}_E \delta(z - z_0)$$
(2.3.3d)

Here we have abbreviated

$$\Omega = \omega - k \cdot v$$

for the Doppler shifted angular frequency and also have abbreviated $\hat{\mathbf{w}}$ and \mathbf{u}_{H} for the vertical and horizontal components of \mathbf{u} .

It turns out [Pierce, 1965] that the above set of ordinary differential equations may be reduced to two differential equations for

$$z = \hat{p}/\rho_0^{1/2}$$
 (2.3.4a)

$$Y = i\rho_0^{1/2} \hat{w}/\Omega \qquad (2.3.4b)$$

These equations are

$$\left(\frac{\mathrm{d}}{\mathrm{d}z} + \mathrm{S}\right) z - \mathrm{S}_{12} Y = \left(\frac{-\mathrm{g}}{\mathrm{i}\Omega_{\mathrm{p}}^{1/2}\pi}\right) \delta(z - z_{\mathrm{p}})$$
 (2.3.5a)

$$\left(\frac{d}{dz} - s\right) Y - s_{21} Z = \left(\frac{-1}{i\Omega\rho^{1/2}\pi}\right) \delta(z - z_0)$$
 (2.3.5b)

where

$$S = (1-\gamma/2)g/c^2 - c^{-1} dc/dz$$
 (2.3.6a)

$$S_{12} = \Omega^2 - (\gamma - 1)g^2/c^2 - (g/c^2)(dc^2/dz)$$
 (2.3.6b)

$$S_{21} = (k^2/\Omega^2) - c^{-2}$$
 (2.3.6c)

The remaining quantities of interest are given by

$$\hat{\rho} = \rho_0^{1/2} Z/c^2 + \rho_0^{1/2} [(\gamma - 1)g + dc^2/dz] Y/c^2 + [1/(\pi i\Omega)] \delta(z - z_0)$$
(2.3.7a)

$$\hat{\vec{u}}_{H} = (\vec{k}/\Omega)\rho_{o}^{-1/2}Z - \rho_{o}^{-1/2}Y$$
 (2.3.7b)

The solution to Eqs. (2.3.5) is easily worked out [Pierce, 1967] in terms of solutions of the homogeneous equations

$$\frac{d}{dz} \begin{bmatrix} z \\ y \end{bmatrix}_{u,\ell} = \begin{bmatrix} -s & s_{12} \\ s_{21} & s \end{bmatrix} \begin{bmatrix} z \\ y \end{bmatrix}_{u,\ell}$$
 (2.3.8)

Let Z and Y be nonzero solutions which satisfy these equations for $z^u > z$ and which are analytic functions of ω for given real k and k and for all Im ω greater than some finite value. Similarly, let Z_{ϱ} , Y_{ϱ} be a nonzero set of solutions for z < z which satisfy the boundary condition $Y_{\varrho} = 0$ at z = 0. Then the solutions of the inhomogeneous equations are given by

$$\begin{bmatrix} z \\ y \end{bmatrix} = \alpha_{\ell}(z_0) \begin{bmatrix} z_u(z) \\ y_u(z) \end{bmatrix} \qquad (z > z_0) \qquad (2.3.9a)$$

$$\begin{bmatrix} z \\ y \end{bmatrix} = \alpha_{\mathbf{u}}(z_{0}) \begin{bmatrix} z_{\ell}(z) \\ y_{\ell}(z) \end{bmatrix} \qquad (z < z_{0}) \qquad (2.3.9b)$$

where

$$\alpha_{\ell,u} = \frac{-1}{i\Omega\rho_0^{1/2}\pi W} [2_{\ell,u} - gY_{\ell,u}]$$
 (2.3.10)

with the Wronskian W given by

$$W = (Y_{u}^{Z}_{\ell} - Z_{u}^{Y}_{\ell})_{\text{any } z} = Y_{u}(0)Z_{\ell}(0)$$
 (2.3.11)

That W is independent of height follows directly from the differential equations (2.3.8).

It now follows from the preceding analysis that the integrand in Eq. (2.3.1) is given by

$$p = \left\{ \frac{\rho_{o}(z)}{\rho_{o}(z_{o})} \right\}^{1/2} \frac{1}{\pi[\omega - k \cdot v(z_{o})]} \left\{ \frac{\Psi(z, z_{o})}{Z_{\ell}(0)Y_{u}(0)} \right\} \qquad (2.3.12)$$

where

$$\Psi(z,z_{o}) = [Z_{u}(z_{o}) - gY_{u}(z_{o})]Z_{\chi}(z) \qquad z_{o} > z \qquad (2.3.13a)$$
$$= [Z_{\chi}(z_{o}) - gY_{\chi}(z_{o})]Z_{u}(z) \qquad z_{o} < z \qquad (2.3.13b)$$

It should be noted that a previous statement of the above result has a misprint, $[\rho_0(z)/\rho_0(z)]$ instead of $[\rho_0(z)/\rho_0(z)]$ in the paper by Pierce (1968).

2.4 THE GUIDED MODE APPROXIMATION

The Fourier transform solution given in the previous section is too complicated as it stands for direct integration. Thus it is appropriate to take advantage of any approximations which may be appropriate to the cases of primary interest (namely, waves detected near the ground at large distances which arrive at times roughly corresponding to the lower atmosphere sound speed). The primary approximation we make in this respect is the guided mode approximation. The mathematical manipulations leading to this approximation are described in many texts for waves in stationary media and were first discussed by Pridmore-Brown (1962) and later modified by Pierce (1965) for the case of waves from a point source in a windy stratified atmosphere.

Before introducing the guided mode approximation, we first consider the symmetry properties of the factors f_E , \hat{p} , and of their product

$$I(\omega,\vec{k}) = \hat{f}_{F}(\omega)\hat{p}(\omega,\vec{k},z,z_{0})$$
 (2.4.1)

which appears in the integrand of Eq. (2.3.1). We set $\vec{k} = \vec{k}_R + i\vec{k}_I$ where \vec{k}_R and \vec{k}_I are real vectors and similarly set

 $\omega = \omega_R + i\omega_T$. Since p is real, we have (or at least can choose)

$$I(\omega, \vec{k}) * = I(-\omega_R + i\omega_I, -\vec{k}_R + i\vec{k}_I)$$
 (2.4.2)

Thus, taking the complex conjugate of I is equivalent to changing the signs of the real parts of ω and k. Since $f_p(\omega)$ must a priori have this property $[f_p(t)$ is real], it follows that \widehat{p} must also have this property.

A final symmetry property which can be insured by appropriate choice of branch lines is that, for real k and complex ω ,

$$\hat{p}(-\omega, -\vec{k}, z, z_0) = -\hat{p}(\omega, \vec{k}, z, z_0)$$
 (2.4.3)

To prove this, one should first note that the differential equations (2.3.5) are invariant if $\omega \to -\omega$, $k \to -k$, $Z \to -Z$, $Y \to -Y$. Also, the lower boundary condition is unchanged. This suggests that we may be able to take

$$Z(\omega,\vec{k}) = -Z(-\omega,-\vec{k}) \tag{2.4.4}$$

While it would appear that this neglects the consideration of an upper boundary condition, this is actually not the case, since any posed upper boundary condition would of necessity have to be equivalent to the requirement that $Z(\omega,k)$ be analytic for $\omega_T \geq \varepsilon$. Thus Eq. (2.4.4) merely states that we are free to define $Z(\omega,k)$ for values of ω in the lower half of the complex ω plane in such a manner that Eq. (2.4.4) is satisfied. In what follows we consider that we have made such a definition with an appropriate selection of branch lines. Equation (2.4.3) then follows from the above and (2.3.4a). Since $\widehat{\rho}$ is almost everywhere analytic in k, it would seem appropriate to consider (2.4.3) to hold also when the components of k are complex.

Returning now to the central task of deriving the guided mode approximation, let us first interchange the order of ω and k integrations in Eq. (2.3.1). It follows that we can do this if we can find an ε which does not depend on k. The analysis by Friedland and Pierce (1969) would apparently indicate that such an ε can be found providing the atmosphere is inherently stable. Let us assume this is the case. Then the integration over k and k is replaced by one over k and θ_k (polar coordinates) where

$$k_x = k \cos \theta_k$$
; $k_y = k \sin \theta_k$ (2.4.5)

Since the integrand is clearly periodic in θ_k and since increasing the value of θ_k by π is equivalent to changing the sign of k, we obtain

$$p = \int_{-\infty+i\epsilon}^{\infty+i\epsilon} e^{-i\omega t} \hat{f}_{E}(\omega) \int_{\theta-\pi/2}^{\theta+\pi/2} Q D\theta_{k}$$
 (2.4.6)

where

$$Q = \int_{0}^{\infty} \hat{p}(\omega,\vec{k}) e^{i\vec{k}\cdot\vec{x}} kdk - \int_{-\infty}^{0} \hat{p}(\omega,\vec{k}) e^{i\vec{k}\cdot\vec{x}} kdk \qquad (2.4.7)$$

Here θ is the angle (reckoned counterclockwise) which the horizontal vector x makes with the x axis. It should be noted that the factor $k \cdot x$ in the exponent is kR $\cos(\theta - \theta_k)$ where R is the net horizontal distance from source to receiver.

Using Cauchy's theorem, we may show for $\cos(\theta - \theta_k) > 0$ that

$$Q = Q_{R} - Q_{L} + 2Q_{I}$$
 (2.4.8)

where $\mathbf{Q}_{\mathbf{R}}$, $\mathbf{Q}_{\mathbf{L}}$ and $\mathbf{Q}_{\mathbf{I}}$ are contour integrals of the form

$$\int_{C} \hat{p}(\omega, k) e^{ikR \cos(\theta - \theta_{k})} kdk \qquad (2.4.9)$$

where the contour C is taken as follows:

- Q_R : C circles the upper right quadrant of the k plane in the counter-clockwise sense.
- Q_L : C circles the upper left quadrant of the k plane in the counter-clockwise sense.
- Q_{τ} : C goes straight up the imaginary axis from 0 to ∞ .

The integral Q_T is readily seen to be relatively small for large R compared to Q_R and to Q_L and is accordingly neglected at the outset. The contour integrals Q_R and Q_L are then evaluated by Cauchy's method of residues. It is anticipated that contributions from any branch lines encircled in the shrinking process are of minor importance at large R. Thus we obtain the

approximate result

$$Q = 2\pi i \{ (\Sigma \text{ Res})_R - (\Sigma \text{ Res})_L \}$$

where the quantities (Σ Res) $_R$ and (Σ Res) $_L$ are the sums of the residues of

at the poles in the right upper and left upper quadrants, respectively.

The integrals over θ_k are performed by the saddle point approximation [see, for example, Morse and Feshbach (1954)] under the assumption that the poles $k_n(\omega,\theta_k)$ are much more slowly varying functions of θ_k than is $\cos(\theta-\theta_k)$. Physically, this assumption is equivalent to the neglect of crosswinds. Thus we have a typical integral evaluated in the manner

$$\int_{\theta-\pi/2}^{\theta+\pi/2} \phi_n(\omega,\theta_k) e^{-ik_n R \cos(\theta-\theta_k)} d\theta_k$$

$$\stackrel{\text{ik}_{n}(\omega,\theta)_{R}}{\approx} \phi_{n}(\omega,\theta) \int_{-\infty}^{\infty} e^{ik_{n}R(\theta-\theta_{k})^{2}/2} d\theta_{k}$$

$$\approx \left(\frac{2\pi}{|k_{n}|^{2}}\right)^{1/2} e^{i(k_{n}^{R} - \pi/4) + iPh(k_{n}^{R})/2} e^{(2.4.10)}$$

where the pole location is taken at $\theta_k = \theta$. Here $\text{Ph}(k_n)$ is the phase of k_n (between 0 and π).

Thus Eq. (2.4.6) becomes

$$p = 2\pi i \int_{-\infty+i\epsilon}^{\infty+i\epsilon} \hat{f}_{E}(\omega) \sum_{n} \left(\frac{2\pi}{|k_{n}|R} \right)^{1/2} k_{n} S_{n} e^{i[k_{n}R - \omega t - \pi/4]} \frac{iPh(k_{n})/2}{e} \phi_{n} d\omega$$
(2.4.11)

where ϕ_n is the residue of \hat{p} at $k = k_n(\omega, \theta)$ and S_n is 1 if k_n corresponds to a pole of \hat{p} in the upper right quadrant; -1 for the upper left quadrant. It is assumed throughout the preceding analysis that ω has a nonzero imaginary part. The k_n in general will be complex numbers with positive imaginary parts.

We may let $\epsilon \to 0$ as long as the $k_n(\omega_R + i\omega_I, \theta)$ have nonnegative imaginary parts as $\omega_T \to 0$ from above. We assume this is the case, since otherwise the ambient atmosphere would be unstable. It is necessary to consider the possibility (since it is a certainty in the absence of dissipation) that some of the k_n may be real when ω is real. However, we wish to avoid spurious terms which correspond to poles lying below the real k axis when $\omega_I > 0$. This can be accomplished by simply requiring that, for real ω and real k, only those terms be included for which

$$\partial k_n/\partial \omega \ge 0$$
 (2.4.12)

(which is equivalent to the requirement that the group velocity be positive.)

At this point we make use of the symmetry properties of \hat{p} . The integral over ω may be separated into one from $-\infty$ to 0 and one from 0 to ∞ . The former is then subjected to a change of variable $\omega \to -\omega$. One can readily show from (2.3.2) that the former must be just the complex conjugate of the latter. Thus

$$p = \operatorname{Re} \int_{0}^{\infty} \hat{f}_{L}(\omega) \sum_{n} A_{n}(\omega, \theta) e^{i[k_{n}R - \omega t - \pi/4]} d\omega \qquad (2.4.13)$$

where

$$A_{n} = 4\pi i \left[\frac{2\pi}{|k_{n}|R} \right]^{1/2} S_{n} e^{iPh(k_{n})/2} \phi_{n} k_{n}$$
 (2.4.14)

The pole locations are assumed to be piecewise continuous functions k (ω,θ) of ω . Thus we can interchange the sum and integral in Eq. (2.4.13), obtaining

$$p = \sum_{n} p_{n}$$
 (2.4.15)

where p_n is the contribution from the n^{th} guided mode, given by

$$p_{n} = Re \int \hat{f}_{E}(\omega) A_{n}(\omega, \theta) e^{i[k_{n}R - \omega t - \pi/4]} d\omega \qquad (2.4.16)$$

The integration limits extend over a range of positive ω for which $k_n(\omega,\theta)$ is defined. It should be noted that the k_n are in general

complex. Their imaginary parts must be positive, but (at least formally) their real parts could be either positive or negative. In the terminology used by Friedman (1967), those modes with a non-zero imaginary part of k_n are called leaky modes. It is possible that a given mode may be leaky over a given range of ω and then be non-leaky (real k_n) over another range of ω .

It is tempting to discard all leaky modes or leaky portions of modes at the outset with the glib statement that at sufficiently large R they are negligible. However, just whether or not they are negligible depends on the magnitude of $Im(k_n)$. Since we are primarily interested in propagation to distances of the order of $10,000~\rm km$, the values of $Im(k_n)$ should be greater than, say, $10^{-3}~\rm km^{-1}$ if we are to consider a leaky mode to be negligible. We might term modes where $Im(k_n)$ is less than this value as slowly leaking modes.

Just when slowly leaking modes are important in waveform synthesis is intimately related to the nature of the topmost region of the assumed model atmosphere. If the top of the atmosphere is adjacent to a rigid surface or is bounded by a free surface, then there is nowhere for energy to leak and there are no leaking modes. On the other hand, as was originally observed by Press and Harkrider (1962), if the uppermost region of the atmosphere is taken as an isothermal half-space, then there are certain regions of the k vs. ω (for fixed θ) plane (with k and ω real) in which the dispersion curves for non-leaking modes cannot penetrate. If a mode's dispersion curve apparently terminates at the edge of such a region, then it would seem that the extension of the mode into such a region would be a leaky mode. None of these three types of models is too fair a representation of the upper atmosphere, but one may argue that, if the major portion of the energy is channeled near the ground, then the variations in the model atmosphere above 150 km should have relatively little effect on the actual waveform. Numerical studies such as described elsewhere in this report would seem to support this conclusion.

The discussion given above would suggest that we may avoid the consideration of leaky modes by adopting a suitable model of the uppermost portion of the atmosphere. Just what model is adopted should probably be a compromise between what is known about the upper atmosphere and the desire to minimize the contribution from the slowly leaking modes. In what follows, we assume such a model has been selected and accordingly consider only real non-leaking modes.

Since we are interested primarily in interpreting data on

waves arriving at times corresponding to group velocities roughly equal to the sound speed in the lower atmosphere, it is clear that we may discard at the outset any modes or portions of modes which give negligible contributions at such times. Since the contribution to a mode at time t comes primarily from frequencies near that at which ω satisfies

$$\frac{t}{R} = \frac{\partial k_{R}}{\partial \omega} \tag{2.4.17}$$

it would seem appropriate to consider only those modes where $\partial \mathbf{k}_{n}/\partial \omega$ is of the order of 1/c where c is a representative sound speed. To this purpose, the following theorem derived by Pierce (1965) for non-leaking modes may be of assistance.

$$\frac{\partial k}{\partial \omega} = \frac{0}{\infty}$$

$$\int_{0}^{\infty} \{\Omega Y^{2} + (k^{2}/\Omega^{3})Z^{2}\} dz$$

$$\int_{0}^{\infty} \{\Omega (\vec{k} \cdot \vec{v}/k)Y^{2} + k\omega\Omega^{-3}Z^{2}\} dz$$
(2.4.18)

The fact that wind speeds are small compared to the sound speed suggests that we may estimate the magnitude of $\partial k/\partial \omega$ for cases of interest with the neglect of wind velocity. In this limit, the above expression becomes

$$\frac{\partial k}{\partial \omega} \sim \frac{k}{\omega} + \frac{\omega^2}{k} \alpha^2 \tag{2.4.19}$$

where α^2 is positive. Thus $\partial k/\partial \omega$ is positive only if k>0 (given $\omega>0$). Furthermore, the group velocity $(\partial k/\partial \omega)^{-1}$, if positive, should always be less than the phase velocity. Thus, we may restrict our analysis to modes where k>0 and where ω/k is greater than, say, half the sound speed at the ground. It would certainly seem appropriate to discard all modes where k is negative or where ω/k is less than the maximum wind speed, given that the maximum wind speed is small. (The reasoning here may be somewhat circular since we initially neglected the winds to arrive at this deduction. However, a more detailed examination seems unwarranted at the present stage.)

Let us next examine the quantity $A_n(\omega,0)$ in Eq. (2.4.14) under the assumption that k_n is positive, real, and greater than ω times the maximum wind speed. The poles of \hat{p} which satisfy these requirements must, by Eq. (2.3.12), correspond to zeros of

 $Y_u(0)$, when considered as a function of k. The residue ϕ of \widehat{p} at such a pole is given by (2.3.12), only with $Y_u(0)$ replaced by $\partial Y_u(0)/\partial k$. The latter derivative has been shown by Pierce (1965) to be given by

$$-2\int_{0}^{\infty} \{\Omega(\vec{k} \cdot \vec{v}/k)Y^{2} + k\omega\Omega^{-3}Z^{2}\} dz$$

$$\frac{\partial Y_{u}(0)}{\partial k} = \frac{\sigma}{Z_{u}(0)}$$
(2.4.20)

Furthermore, since $Y_u(0)$ is 0 at a pole, the upper and lower boundary conditions are both satisfied when $k = k_n$ and we may discard the subscripts ℓ and u. Thus we have

$$\phi_{\rm n} = -\left[\frac{p_{\rm o}(z)}{\rho_{\rm o}(z_{\rm o})}\right]^{1/2} \frac{i}{2\pi\Omega(z_{\rm o})} \frac{[Z(z_{\rm o}) - gY(z_{\rm o})]Z(z)}{\int\limits_{0}^{\{\Omega(\vec{k}\cdot\vec{v}/k)Y^2 + k\omega\Omega^{-3}Z^2\}} dz}$$
(2.4.21)

where the direction of k is θ and its magnitude is $k_n(\omega, \theta)$.

If Eq. (2.4.21) is substituted into (2.4.14), we find

$$A_{n} = \left[\frac{\rho_{o}(z)}{\rho_{o}(z_{o})}\right]^{1/2} \left[\frac{8\pi k_{n}}{R}\right]^{1/2} \frac{1}{\Omega(z_{o})} \frac{[Z(z_{o}) - gY(z_{o})]Z(z)}{\int_{0}^{\infty} {\{\Omega(\vec{k} \cdot \vec{v}/k)Y^{2} + k\omega\Omega^{-3}Z^{2}\}dz}}$$
(2.4.22)

It should be recalled that the expression for a guided mode is given by Eq. (2.4.16). The quantities $k_{u}(\omega,\theta)$ are zeros of $Y_{u}(0)$ and it is assumed that we need only consider contributions from mode segments where Ω is positive for all z and where $k_{u}>0$.

The only remaining piece of analysis to complete our formal derivation is the derivation of an explicit expression for $f_E(\omega)$. If we insert Eqs. (2.1.5) into Eq. (2.3.2), we find

$$\hat{f}_{E}(\omega) = (2\pi)^{-1} Y_{KT}^{1/3} [p_{O}(z_{O})/p_{O}(0)]^{2/3} L_{s} \int_{0}^{\infty} e^{i\omega t} \int_{0}^{t} f_{1KT}(t'/[\lambda_{O}Y_{KT}^{1/3}]) dt'dt$$

or, after an integration by parts,

$$\hat{f}_{E}(\omega) = -(2\pi)^{-1} Y_{KT}^{1/3} [p_{o}(z_{o})/p_{o}(0)]^{2/3} L_{S} \left(\frac{1}{i\omega}\right) \int_{0}^{\omega} e^{i\omega t} f_{1KT}(t/[\lambda_{o}Y_{KT}^{1/3}]) dt$$

From Eq. (2.1.7), we find

$$\int_{0}^{\infty} e^{i\omega t} f_{1KT}(t/[\lambda_{o}Y_{KT}^{1/3}]) dt = \frac{P_{s}i\omega}{[\omega + i(\lambda_{o}Y_{KT}^{1/3}t_{s})^{-1}]^{2}}$$

Thus

$$\hat{f}_{E}(\omega) = -(2\pi)^{-1} Y_{ET}^{1/3} [p_{o}(z_{o})/p_{o}(0)]^{2/3} L_{s} P_{s}/[\omega + i(\lambda_{o} Y_{KT}^{1/3} t_{s})^{-1}]^{2}$$
(2.4.23)

The symbols in this expression are as defined in Sec. 2.1.

2.5 SUMMARY OF THE GUIDED MODE SOLUTION

For convenience of referral, the solution derived in the previous sections is summarized. First, we have the wave as a sum of guided modes, the acoustic overpressure p being given by

$$p = \sum_{n} p_{n}(R, \theta, \mathbf{z}_{o}, \mathbf{z}, t)$$
 (2.5.1)

where the arguments of $p_{\mathbf{n}}$ are

R = horizontal distance from source

 θ = azimuth angle of observer (counter-clockwise in horizontal plane)

 z_0 = height of burst

z = height of observation location

t = time of observation

In addition p_n depends on the sound speed and wind velocity profiles, c(z) and v(z), and on the yield Y_{KT} of the explosion in KT.

A particular guided mode wave is given as an integral of

the form

$$p_{n} = \int D_{n} \cos \left[\omega t - k_{n}R + e\right] d\omega \qquad (2.5.2)$$

where the integration extends over all positive frequencies ω for which a real $k_n(\omega,\theta)$ is defined. The quantities D_n and e are real functions of ω . We may define D_n as $\pm \left|f_EA_n\right|$ and take e as $\pi/4$ minus the pahse of $\pm f_EA_n$. The choice of sign depends on just which real factors are incorporated into D_n .

The particular forms which we may take for $\mathbf{D}_{\mathbf{n}}$ and $\mathbf{e}_{\mathbf{n}}$ are

$$D_{\rm n} = \left[\frac{\rho_{\rm o}(z)}{\rho_{\rm o}(z_{\rm o})}\right]^{1/2} \left[\frac{2k}{\pi R}\right]^{1/2} \frac{Y_{\rm KT}^{1/3} [p_{\rm o}(z_{\rm o})/p_{\rm o}(0)]^{2/3} L_{\rm s} P_{\rm s}}{[\omega^2 + (\lambda_{\rm o} Y_{\rm KT}^{1/3} t_{\rm s})^{-2}]}$$

$$\times \frac{1}{\Omega(z_0)} \frac{\left[Z(z_0) - gY(z_0)\right]Z(z)}{\infty}$$

$$\int_{0}^{\left\{\Omega \vec{k} \cdot \vec{v}/k\right\}Y^2 + k\omega\Omega^{-3}Z^2\} dz}$$

$$(2.5.3)$$

$$e = 5\pi/4 + 2 \times \text{phase} \left[\omega + i(\lambda_0 Y_{KT}^{1/3} t_s)^{-1}\right]$$
 (2.5.3)

where

$$P_s = 1.61 \times 34.45 \times 10^3 \text{ dynes/cm}^2$$
 $L_s = 1 \text{ km}$
 $t_s = 0.48 \text{ sec}$
 $\lambda_o = [c(0)/c(z_o)][p_o(0)/p_o(z_o)]^{1/3}$
 $k = k_n(\omega, \theta)[e_x \cos \theta + e_y \sin \theta]$

The functions Y and Z are eigenfunctions of two coupled homogeneous ordinary differential equations and $k_n(\omega,\theta)$ may be considered the corresponding eigenvalue.

To introduce the nomenclature used in the discussion of the computer program, we set

$$D_n = (1/R^{1/2}) \text{ (AMPLTD)}$$
 (2.5.4a)

AMPLTD = (FACT)
$$(Y_{KT}^{2/3}k^{1/2}/\omega) |s(\omega \lambda_o Y_{KT}^{1/3})|$$
 (AMP) (2.5.4b)

FACT =
$$[4/2\pi)^{1/2}$$
]c(0)[$\rho_o(z)/\rho_o(z_o)$]^{1/2}[$\rho_o(z_o)/\rho_o(0)$]^{1/3} (2.5.4c)

$$AMP = -\frac{[Z(z_o) + gY(z_o)]Z(z)}{\sum_{0}^{\infty} (2.5.4d)}$$

$$-2\Omega(z_o)c(z_o) \int_{0}^{\infty} {\{\Omega(\vec{k} \cdot \vec{v}/k)Y^2 + \omega k\Omega^{-3}Z^2\}dz}$$

$$S(\omega) = \frac{i\omega P_s L_s}{[\omega + it_s^{-1}]^2}$$
 (2.5.4e)

PHASQ =
$$e = 3\pi/4$$
 - Phase $\{S(\omega \lambda_0 Y_{KT}^{1/3})\}$ (2.5.4f)

The subscript n on various quantities is omitted for brevity.

In terms of the quantities introduced above, the contribution \boldsymbol{p}_{n} from the n-th guided mode becomes

$$P_n = R^{-1/2} \int AMPLTD \cos \left[\omega(t - R/v_p) + PHASQ\right] d\omega \qquad (2.5.5)$$

where

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$$v_{p} = \omega/k \tag{2.5.6}$$

is the phase velocity (varying with ω) of the guided mode.

2.6 THE MULTILAYER METHOD

In order to compute the dispersion curves $k_n(\omega,\theta)$ [or, equivalently, phase velocity v_n vs. ω] for the guided modes and the functions Y and Z, it is convenient to formally replace the actual atmosphere by a multilayer model, in which the model is comprised of a discrete number of layers, each having constant temperature and wind velocity. Such a technique is fairly common in the numerical solution of wave propagation problems and dates at least as far back as Haskell (1950). The multi-

layer method has some shortcomings and has been criticized by various authors. It is important that the reader realize that the method is only a numerical integration technique. We do not approximate the atmosphere by a multilayer model at the outset but only use this as a device to evaluate the quantities needed for numerical evaluation of the solution summarized in the previous section. In actual fact, any given multilayer atmosphere would most likely be unstable for disturbances of sufficiently short wave length. However, for any given \boldsymbol{k} and $\boldsymbol{\omega}_{\text{\tiny{\textbf{i}}}}$ we may always pick a model (by simply including enough layers) that the numerical solution of the homogeneous residual equations (2.3.8) is in good agreement with the result which might be obtained by using a given continuous atmosphere. This has been demonstrated previously by one of the authors [Pierce, 1966]. It may be argued that the multilayer method is not the most efficient numerical method, but the authors believe that, from the standpoint of coding the problem for numerical computation, the multilayer method is generally to be preferred.

For the purpose of making the organization of the computation scheme as simple as possible, it is assumed that one has picked a multilayer model of sufficient detail that it suffices for all numerical computations necessary to evaluate a given waveform. The same model will then be used throughout the computation. Guidelines for selecting such a model have been discussed by Pierce (1967) and by Vincent (1969). The user, if he so wishes, may establish his own guidelines by numerical experiment.

In multilayer computations, it is convenient to deal with quantities Φ_1 and Φ_2 rather than Z and Y since the latter are not in general continuous at layer boundaries. The functions Φ_1 and Φ_2 are defined as

$$\Phi_1 = cY \tag{2.6.1a}$$

$$\Phi_2 = gY/c - Z/c$$
 (2.6.1b)

These can be shown from Eq. (2.3.8) to satisfy the residual equations

$$\frac{d}{dz} \begin{bmatrix} \phi_1 \\ \phi_2 \end{bmatrix} = \begin{bmatrix} A_{11} & A_{12} \\ A_{21} & A_{22} \end{bmatrix} \begin{bmatrix} \phi_1 \\ \psi_2 \end{bmatrix}$$
 (2.6.2)

where the elements of the matrix [A] are given by

$$A_{11} = gk^2/\Omega^2 - \gamma g/(2c^2)$$
 (2.6.3a)

$$A_{12} = 1 - c^2 k^2 / \Omega^2$$
 (2.6.3b)

$$A_{21} = g^2 k^2 / \Omega^2 c^2 - \Omega^2 / c^2$$
 (2.6.3c)

$$A_{22} = -A_{11} \tag{2.6.3d}$$

It follows from the form of these coefficients that Φ_1 and Φ_2 must be continuous with z even when c and v are discontinuous. In any given layer, the matrix [A] is constant.

One restriction we place on the multilayer atmosphere is that the top-most layer (bounded below by $z=z_T$) be an isothermal halfspace with constant winds. The only solution of Eq. (2.6.2) which, for real k, is analytic in ω for $z>z_T$ for all ω for which $\text{Im}(\omega)>0$, and which vanishes as $\text{Im}(\omega)+\varpi$ (these conditions are equivalent to the causality condition) is of the form

$$\begin{bmatrix} \varphi_1 \\ \varphi_2 \end{bmatrix} = \mathcal{V} \begin{bmatrix} -A_{12} \\ A_{11} + G \end{bmatrix} e^{-G(z - z_T)} \qquad (z > z_T) \qquad (2.6.4)$$

where

$$G^2 = \Lambda_{11}^2 + \Lambda_{12}^A \Lambda_{21} \tag{2.6.5}$$

with the coefficients A_{ij} appropriate to the upper half space. The phase of G is chosen such that G is analytic in the upper half of the ω plane and such that the phase of G approaches 0 as $\text{Im}(\omega) \!\!\!\! \to \!\!\!\! \infty$. The quantity D in the above expression is any convenient constant. A necessary consequence of this is that the phase of G must be 0 when ω is real on all regions of the real ω axis where $G^2 > 0$. If $G^2 < 0$, the phase of G could be either $\pi/2$ or $-\pi/2$, depending on which choice is compatible with the requirement that G is analytic for $\text{Im}(\omega) > 0$. It should be noted that G has branch points on the real axis.

The values of ϕ_1 and ϕ_2 at lower values of z are found by integrating Eqs. (2.6.2) down from z = z_T with (2.6.4) as starting conditions. Since the equations are linear, we can determine a transmission matrix [R] such that

$$\begin{bmatrix} \phi_1 \\ \phi_2 \end{bmatrix}_{z=0} = [R] \begin{bmatrix} \phi_1 \\ \phi_2 \end{bmatrix}_{z_T}$$
 (2.6.6)

where [R] is independent of the values of ϕ_1 and ϕ_2 at $z=z_T$. The condition that $\phi_1(0)=0$ is therefore

$$F(\omega, \vec{k}) = \Lambda_{12}R_{11} - (G + \Lambda_{11})R_{12} = 0$$
 (2.6.7)

where G, Λ_{11} ; and Λ_{12} are quantities appropriate to the upper halfspace. The function $F(\omega,k)$ for general ω and k is called the <u>normal mode dispersion function</u>. It is defined here for all values of ω in the upper half plane and for all real k.

If, as implied previously, we restrict our attention to modes where ω and k are real, then the matrix [R] will be real and G must be real if Eq. (2.6.7) is to be satisfied. This limits the region in the ω , k space where one need search for roots of the normal mode dispersion function. Since we need only consider points such that G is real, we can simply say that the normal mode dispersion function does not exist if this condition is not satisfied. We can also say that, if Φ_1 and Φ_2 describe a non-leaking guided mode (which is the only type we consider), then Φ_1 and Φ_2 must satisfy an upper boundary condition of decaying exponentially with increasing z in the upper half space.

One of the chief advantages of the multilayer approximation is that one can formulate a straightforward algorithm which computes the normal mode dispersion function $F(\omega,k)$ for given real ω and k. Thus the computer can formally consider $F(\omega,k)$ as a known function in obtaining dispersion curves. The details of the computation of $F(\omega,k)$ are discussed in the description of the program's subroutines. [See Appendix B.]

2.7 TABULATION OF DISPERSION CURVES

One of the principal difficulties in coding the numerical synthesis of waveforms was that of obtaining a feasible method for tabulating the dispersion curves of the guided mode. By dispersion curves, we here mean the graphs of phase velocity $v_p(\omega,\theta)$ versus ω for fixed θ , where v_p satisfies

$$F(\omega, \vec{k}) = 0 \tag{2.7.1}$$

with

$$\vec{k} = (\omega/v_p)[\vec{e}_x \cos \theta + \vec{e}_y \sin \theta]$$
 (2.7.2)

We denote the value of $F(\omega,\vec{k})$ when \vec{k} is given by Eq. (2.7.2) as $F_{\theta}(\omega,v_p)$. Thus we wish to tabulate curves in the v_p , ω plane along which

$$F_{O}(\omega, v_{p}) = 0$$
 (2.7.3)

given a computational scheme which either computes F_θ for given ω and v or else tells us that a real $F_\theta(\omega,v_p)$ does not exist for such values.

Such a tabulation of dispersion curves is complicated by the fact that it requires some care to insure that we do not mix modes. For example, if (ω_1, v_1) and (ω_2, v_2) are two points at which $F_{\Theta} = 0$, it is difficult to determine whether or not these points both lie on the same curve or on different curves. An obvious goal is to eliminate the need for human intervention in answering such questions. The manner in which we accomplished this may be of some intrinsic interest as analogous problems occur in many other contexts.

We specify a rectangular region of the \boldsymbol{v} versus $\boldsymbol{\omega}$ plane and consider a dense rectangular array of points p in this region. Each point lying on the same row corresponds to the same value of ν and each point lying on the same column corresponds to the same value of $\omega.$ For each such point we compute the sign, + or - (or X if $F(\omega, v)$ does not exist), of the normal mode dispersion function. Pone can visualize such a computation as being presented in the form of a picture (which we term a table) analogous to what one sees on a television screen. (See Fig. 2-3.) In such a picture one may readily perceive (providing the density of points is sufficiently great) clear-cut regions of the v versus ω plane where the sign of F_{θ} is +, regions where F_{θ} is negative, and regions where F_{θ} does not exist (all X's). The dispersion curves would then correspond to the more or less sharply defined lines which separate regions of all +'s from regions of all -'s. The technique used by the authors was (1) to systematically and selectively increase the density of considered points to such an extent that all dispersion curves in the rectangular region could be clearly perceived and (2) to use the picture array as a guide for systematically tabulating the dispersion curves for each given mode and to define starting brackets for homing in on particular points on the curves.

```
* Vousi
            HURMAL MODE DISPERSION FUNCTION SIGN
  0.58621
            ++++++--+---++---++---++
  0.57241
            --++++--+---+
  0.55862
  0.54483
  0.53103
            X---++--++--++---++---++
  0.51724
            Y---++--++---++---++----++----
  0.57345
           X---++--++--++--++---++--
  9.48966
           ·Y----+--++--++---++----+++--
  0.47586
           X---++---++---++
  0.46237
           XX---++--++---++---++--
  0.44828
  0.43445
           XX---++--++---++----+
  0.42069
            XX---++---++---++----++
  0.49690
            XX----++---++----+++--
           XY---++---++
  0.30314
  0.37931
  0.36552
           XX---+++---+++++
           XX---+++-----+++----+++
  0.35172
  0.32702
           XX----++++------++++++++
  0.32414
           XX+++-+++++------++++
  0.31034
  0.23655
  0.29276
  0.25517
  0.24139
  0.22750
 0.21370
           123456789012345678901234567890
PHASE VELOCITY DIPECTION IS
 OPFG4
                                             DEGREES
UMERY =
   ウ・ᲜᲔᲔᲔᲔ₽−₽2
                 0.92759F-02
                              0.115525-01
                                            C.14928F-01
                                                         0.181035-01
   0.213790-01
                 0.244556-01
                              1.27931F-01
                                            0.312075-01
                                                         0.34483F-01
   0.377591-01
                 0.410346-01
                              0.44710F-01
                                            0.475965-01
                                                         0.508625-01
   0.541305-01
                 0.574145-01
                              1.606915-11
0.77069E-0]
                                            0.639650-01
                                                         C.47241F-01
   2.705175-01
                 1.73793F-31
                                                         0.836216-01
   C.86896F-01
                 0.901726-01
                                            0.057246-01
                                                         C.10000F 02
```

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Figure 2-3. Sample table of normal mode dispersion function signs. An "X" means that the function does not exist at that point in the phase velocity-frequency plane.

Although the above discussion may seem to be expressed in humanistic terms, the actual computation is carried out by the machine without human intervention.

在一个时间,我们就是一个时间,我们就是一个时间,我们的时间,我们的时间,这个时间,我们的时间,我们的时间,这个时间,这时间,这时间,这时间,这个时间,这个时间,

One subsidiary problem which had to be solved was that of determining the criteria for when the density of points in the "picture" is sufficiently great that all of the dispersion curves in the rectangular region may be clearly defined. For this purpose the following theoretical conjectures were of considerable utility:

- 1. No two dispersion curves may intersect each other.
- 2. As long as v is greater than the maximum wind speed, $dv_{p}/d\omega \leq 0 \mbox{ for any dispersion curve.}$

The first conjecture follows from the fact that if two curves cross at a point (ω, \mathbf{v}) then one must have $\mathbf{F}_{\theta} = 0, \partial \mathbf{F}_{\theta}/\partial \omega = 0$ $\partial \mathbf{F}_{\theta}/\partial \mathbf{v} = 0$ all simultaneously satisfied at this point. To locate such a point, we would have to solve three equations for the two unknowns ω and \mathbf{v} . Since we have more equations than unknowns, it would be highly unlikely that such a point could be found. To date, we have not found any case of this happening, although the separation between adjacent curves can be very small.

The second conjecture follows from Eq. (2.4.18). Using the fact that $v_p = \omega/k$, we find, after some algebra, that

$$\frac{d\mathbf{v}_{\mathbf{p}}}{d\omega} = \frac{-1}{k^2} \frac{0}{\sum_{k=0}^{\infty} \left[k\omega\Omega^{-3}\mathbf{z}^2 + \Omega(\mathbf{k}\cdot\mathbf{v}/\mathbf{k})\mathbf{y}^2\right] d\mathbf{z}}$$
(2.7.4)

This is clearly negative as long as the denominator is positive. However, if the denominator is negative, then Eq. (2.4.18) would require the group velocity to be negative. If the group velocity is negative, then the discussion associated with Eq. (2.4.12) implies that the mode should not contribute to the waveform. In any event, the denominator in Eq. (2.7.4) must be positive for no winds and would most likely be positive if the winds are sufficiently weak. (Throughout this discussion we consider $\Omega > 0$ for all z.) Thus, while we have not succeeded in giving a truly rigorous proof of either of these conjectures, they seem likely to always hold in all cases of interest.

With the acceptance of the two conjectures discussed above, we may regard a pictorial array as being sufficient to resolve the modes if it indicates no apparent violations of the two conjectures. If it does indicate an anomaly, we simply add more points to the array (i.e., increase the density of points) until the anomaly disappears. The method of adding points should be formulated in such a manner that one does not go overboard, as the signs of the normal mode dispersion function will in general occupy a large amount of storage space in the machine. The method utilized in the program seems to be fairly foolproof and yet reasonably conservative in the number of points added to correct apparent anomalies. Further details may be found in the discussion of the program's subroutines.

As an example of how the table expansion process works in practice, suppose that the region of the ω , ν plane considered is that where $.2 \le \nu \le .6$ km/sec, $.005 \le \omega^p \le .1$ rad/sec. The first tabulation is made with 900 points, corresponding to 30 equally spaced values of ω and 30 equally spaced values of ω . For a particular ω and a particular model atmosphere, the result (which may at the user's discretion be printed out by the machine) is shown in Fig. 2-3. We arbitrarily number the modes starting in the lower left corner of the table and going up towards the upper right corner. Note that modes 3 and 4 almost touch near (0.0214, 0.324), modes 4 and 5 seem to disappear near (0.0443, 0.320), and other modes seem to vanish as well. In order to get rid of these anomalies, the computer judiciously adds new rows and columns. The table in Fig. 2-4 is the result. Note that the ω coordinates of the rows and the phase velocity coordinates of the columns are not equally spaced in the expanded table.

2.8 OTHER NUMERICAL TECHNIQUES

The result of the dispersion curve computation is a tabulation (stored in the machine) of points (ω, v) which lie on the n-th mode's dispersion curve and which describe that portion of the curve which lies in some prespecified rectangular region of the (ω, v) plane. Some specified number of modes are tabulated. The Size assumed for the rectangular region is an inherent limitation on the computation and largely determines the limits of integration used in the evaluation of (2.5.5). Since these limits are not the true limits of the mode, an additional approximation is implied by this technique. There is some degree of "art" involved in the selection of this rectangular region and in the interpretation of waveforms computed with such a truncation.

```
KUDANT AUDE UTSHERSTON LANCELUN 2104
VPHST
P.62000
0.59621
     4444444444444
     n, 55665
     0.54483
0,63104
     X---++++--++---++----
0.51774
     0.50745
0.44044
     0.47586
0.44707
     0.44829
     XX--+++++--+++--++++---+++-----+
0:43448
     XX---++++----+++----+++----
6.45060
     0.49690
     0.39310
     ¥<u>\___+++++----+++----+++</u>++------+
0.37031
     XX----++++-----+++-----++++++
0. 37241
     0.34552
     0.35842
     0.35177
     XX----+++++---------+++++-----------
0.34483
0.33703
     0.32414
     yx++++----+++-------+++++++++++++
0.32241
0.22050
     0.31897
0.31010
      0.31789
      0.31779
      0.31773
      ¥¥444-----+++++++++++++++++++++++
C.31770
      0.31767
      0.31746
      0.31724
      0.31034
      0.29655
0.79276
0.24897
0.25617
 0.24139
0.22750
0.21379
 0.20000
      12345678901234557890123456789012345678901234
DMFGA
                     C.O DEGREES
      PHASE VELOCITY DIRECTION IS
DHEGA *
                              0.181036-01
 0.500005-02
                0.1155?F-91
                       0.149798-01
         0.427595-92
                       0.24655E-01
                              0.279316-01
  10-107515.0
         0.23017F-01
                0.238365-01
                0.377595-01
                              0.426725-21
                       0.41034F-01
  0.312075-01
         1,34483F-01
                0.508425-01
                       0.541395-01
                              0.57414E-01
  0.443105-01
         0.475866-01
                              0.705178-01
         n.62328F-01
                0.63965F-01
                       0.472418-01
  0.626906-01
                              0.836218-01
         n.73703F-31
                0.770695-01
                       0.80345F-91
  0.721555-01
                       0.934486-01
                              0.95086E-01
                0.018105-01
         0.901725-01
  n. 848945-01
                              0.96315F-01
                0.95975F-31
                       2.941125-01
         0.957008-31
  1,054965-01
                0.983428-01
                       ח. וחרחור זה
         0.967746-11
  0.045195-91
```

Figure 2-4. An expanded version of the table in Fig. 2-3 created by the INFRASONIC WAVEFORMS code. Rows and columns have been added so that the modes are distinct.

Let $v(\omega)$ be the phase velocity as a function of frequency for a given mode which is tabulated at $\omega = \omega_1$, ω_2 , ... ω_N ; the corresponding values of v being denoted by v_1 , ... v_N . For each of the values ω_1 , the wavenumber $k_1 = \omega_1/v_1$ is computed and then the quantities AMPLTD and PHASQ in Eqs. (2.5.4) are computed. The values of AMPLTD, k_1 , and PHASQ at values of ω between neighboring ω_1 are approximated by linear interpolation, following a technique introduced by Aki (1960) for numerical integration over oscillatory integrands. This defines the integrand at all values of ω between ω_1 and ω_1 . The resulting integral may then be expressed as a sum of N_1 - 1 terms, each term involving elementary functions, with no further approximations. The evaluation of this sum then leads to an approximate value of p_1 for given t_1 and t_2 .

The Aki technique described above for numerical integration, although approximate, would appear to be a considerable improvement over the method of stationary phase, commonly used in wave propagation computations. It would appear that the stationary phase approximation would probably give grossly erroneous results, in view of the fact that some of the modes are very weakly dispersive. We should point out that the technique used here was suggested to the authors by Harkrider's paper (1964).

A shortcoming of the computation scheme is that the resulting solutions formally violate the causality requirement. Although causality is guaranteed by the Fourier transform solution, the guided mode solution, being an approximation, may not preserve this property. Furthermore, the truncation of integration limits will tend to amplify the non-physical waveform predicted at times before the true wave should actually arrive. However, at moderate and large distances, the noncausal portion of the wave should have relatively small amplitudes. This is borne out by the numerical computations. The authors believe that, with proper care in the selection of input parameters, the scheme described here should give a fair representation of the dominant portion of the waveform for low altitude observation of waves from low altitude explosions - providing, of course, that the stratified model for the atmosphere is adequate.

Chapter III

USER'S GUIDE TO INFRASONIC WAVEFORMS

3.1 INTRODUCTION

INFRASONIC WAVEFORMS is a digital computer program written in FORTRAN IV for the IBM 360 system at M.I.T. A slightly modified version for the IBM 7094 is currently in operation at the Air Force Cambridge Research Laboratories in Bedford, Massachusetts. The purpose of the program is to give a theoretical prediction of the acoustic pressure waveform which would be recorded at large horizontal distances (500 km to 10,000 km) from a low to moderate altitude thermonuclear explosion in the atmosphere. The program represents a substantial extension to an earlier program, INFRASONIC MODES, written by A. Pierce (1966).

In the program, the atmosphere is assumed to consist of a number (possibly as large as 100) of horizontal layers, each having constant temperature and wind velocity. The temperatures, wind-velocity magnitudes, and wind-velocity directions are not necessarily assumed to be the same in each layer. Such a multi-layer atmosphere, if judiciously chosen, may be expected to give a reasonable approximation to any continuously stratified atmosphere in so far as the calculations of waveforms are concerned.

It is the authors' intent that the program be written in such a form as to facilitate use by anyone having access to a large digital computer. It is written in a manner such that it should not be too difficult to modify for application to similar problems or for use in other computer installations. The fact that we were able to modify the M.I.T. version for the AFCRL computer with only a moderate expenditure of time attests to the latter.

The key to insuring that any program be amenable to wide-spread usage is documentation. This report represents one such attempt to provide such documentation. In addition, the program is written with a predominance of COMMENT statements. A listing of the program is given in Appendix B. The comments at the beginning of each subroutine attempt to explain the function of each, and its purpose in relation to the main task of the program. Definitions of all variables, input and output, as well as of those presumed in COMMON storage are given. This rather elaborate procedure was suggested to the authors by a recent book on computer analysis of time series by Simpson. (Frankly, we believe that this is the manner in which all computer programs should be written.)

The present program has been continuously tested and used for well over a year now and we are reasonably certain that it is free of major coding errors. However, the sheer length of the program prohibits us from certifying this with certainty.

The theory on which the program is based is summarized in the preceding chapter. Here, we attempt to describe the program from the viewpoint of its operation - i.e., to give a user's manual for the program. To a certain extent, this duplicates the statements given in the deck listing of the program. However, in a matter such as this, only a slight amount of confusion can cause undue grief and expenditure of time and money. Thus, we feel that it is vastly preferable to give an overdetailed account of the program than to run the risk of dissuading someone from use of the program. The comments given here apply mainly to the operation of the M.I.T. version - it is to be hoped that users at other installations will be able to quickly ascertain just what modifications in the program and in its rules of usage are necessary.

3.2 GENERAL DISCUSSION OF PROGRAM USAGE

To obtain a synthesized waveform and/or other auxiliary information, the user must decide in advance on the values of various input parameters which control the operation of the program. These input parameters may be considered as falling within one of six general categories:

- 1) Farameters specifying the nature of the model atmosphere to be used.
- 2) Parameters specifying the nature of the explosion; namely, its yield and height of burst.
- 3) Parameters specifying the location of the observation point with respect to the explosion.
- 4) Parameters controlling the nature of the theoretical and numerical approximations made in the computation.
- 5) Parameters controlling the extent, detail, and type of the output.

It is important that the user realize that not all input parameters need be specified. The program is written so as to allow considerable flexibility in input and output. Possible outputs of the computation include the following:

- 1) Punched cards containing intermediate results in a format suitable for input to future runs of the program.
- 2) A tabulation on the printout of the assumed model atmosphere's properties in a standard format. (Fig. 3-1)
- 3) Printout of all input quantities as they are read in (Fig. 3-2).
- 4) Pictorial displays of the phase velocity curves of the guided modes as being lines separating regions where a + sign is printed at every point from regions where a (minus) sign is printed at every point of a rectangular array of points in the phase velocity versus angular frequency plane. These displays may later be used to check on whether all desired modes were included and on whether or not the computation process was successful in resolving the modes. (Figures 3-3 and 3-4)
- 5) A listing of the tabulation of phase velocity versus frequency for each guided mode (Fig. 3-5).
- 6) A second listing giving the same as in 5 plus parameters of the ϕ_1 and ϕ_2 profiles (defined in Eq. 2.6.1) for each point in the tabulation. (Fig. 3-6)

- 7) A third listing giving the same as in 5 plus an amplitude factor independent of yield. (Fig. 3-7)
- 8) A fourth listing giving the same as in 5 plus the yield dependent amplitude and phase which appear in the integrand of the integral over frequency which represents the contribution to the waveform from a given guided mode. (Fig. 3-8)
- 9) Tabulations of acoustic pressure versus time for selected guided mode waveforms. (Fig. 3-9)
- 10) Tabulation of acoustic pressure versus time for the total waveform. (Fig. 3-9)
- 11) A plot of acoustic pressure versus time for selected guided mode waveforms on the CALCOMP plotter. (Fig. 3-10)
- 12) A plot of acoustic pressure versus time for the total waveform on the CALCOMP plotter. (Fig. 3-10)

MODEL ATMOSPHERE OF 34 LAYERS

LAYER	28	ZT	н	С	٧x	VY
34	225.00	INFINITE	INFINITE	0.8014	9.0	0.0
33	205.00	225.00	20.00	0.7655	2.0	9.9
37	195.00	205.00	10.00	0.7469	0.0	0.0
31	185.CC	195.CC	10.00	0.7279	2.0	0.0
30	175.00	185.00	10.00	0.7097	0.0	0.0
29	165.00	175.00	10.00	0.6882	J.U	c.o
28	155.00	165.00	10.00	0.6584	0.0	0.0
27	145.00	155.00	10.GO	0.6093	0.0	0.0
26	135.00	145.00	10.00	0.5413	0.0	0.0
25	125.CO	135.0C	10.00	0.4783	2.0103	0.0
24	115.00	125.00	10.00	0.4007	0.0236	0.0
23	105.CO	115.0C	10.0C	0.3168	0.0309	C.0
22	95.00	105.00	10.00	0.2833	0.6103	0.0
21	85.00	95.CC	10.00	0.2718	-0.0051	0.0000
20	75.CC	85.00	10.00	0.2725	0.0077	0.0
19	65.00	75.00	10.00	0.2869	0.0206	0.0
18	55.CC	65.00	10.00	0.3104	0.0216	C.O
17	45.00	55.CC	10.00	0.3230	0.0216	0.0
16	40.00	45.00	5.00	0.3261	0.0175	0.0
15	35.CC	40.00	5.00	0.3161	2.0082	0.0
14	30.00	35∙00	5.00	0.3084	0.0021	0.0
13	25.00	30.0C	5.00	0.3019	-0.0021	0.0000
12	20.00	25.CC	5.00	0.2938	-0.0072	0.000
11	18.00	20.00	2.00	0.2869	-0.0058	-0.0021
10	16.00	18.00	2.00	0.2819	0.0055	0.0055
9	14.CO	16.00	2.00	0.2869	0.0103	0.0040
8	12.00	14.00	2.00	0.2938	0.0139	0.0
7	10.00	12.00	2.00	0.3005	0.0154	0.0
6	8.00	10.00	2.00	0.3078	0.0129	0.0
5	6.00	8.00	2.00	0.3161	0.0098	0.0
4	4.00	6.00	2.00	0.3230	0.0046	0.0
3	2.00	4.CO	2.00	0.3292	0.0346	0.0
2	1.00	2.00	1.00	0.3400	0.0011	-0.0C11
1	0.0	1.00	1.00	0.3424	0.0011	-0.0011

ZB=HEIGHT OF LAYER ROTTOM IN KM
ZT=HEIGHT OF LAYER TOP IN KM
H =HIOTH OF LAYER IN KM
C =SOUND SPEED IN KM/SEC
VX=X COMP. OF WIND VEL. IN KM/SEC
VY=Y COMP. OF WINC VEL. IN KM/SEC

Figure 3-1. Printout of model atmospheric properties for 30° N. 140° W. in October.

MAME HAS .	JUST REEN READ IN		
START=	1.NPRNT=	1.4PNCH=	

LANGLE=	1.IMAX=	33,T= 292.0	00000 . 284.	COJO3 6 270.	
36. 00000	• 225.0000C	215.00000	205.60000		
237.00000	. 249.00000	265.00000	266.0000	. 190.0000	, 205.0
2 30.00000	1 250.0000	• 400.00000	• 57C • COOOL	• 240.00000	. 205.0
1255.0000	1370.0000	1390.0000	1460-0000	· 730.66000	925.0
0.0	. 0.0	• 0.0		• 1600.0c03	. 0.0
0.0	0.0	. 0.0		• 0.0	. 0.0
2.0	. O.C	. C.C	• 0.0	. 2.0	. 0.0
0.0	, 0.0	0.0		. 2.0	. 0.0
0.0	, 0.0	. 6.6	. 0.0	. 0.0	0
0.0	. 0.0	. 0.0	. 0.0	• 0.0	. C.O
0.0	, 0.0	. 0.0	. 0.0	. 0.0	. 0.0
3.0	. 0.c	. 0.0	• 0.0	• 3.0	. 0.0
0.0	. 0.0	• 0.0	. 0.0	• 0.0	. 0.0
2.0	, 2.0	. 0.0	• 0.0	• C.O	. 0.0
3.0	0.0	• C.O	, 0.0	, 3.0	. 0.0
9.0	• 0.0		• 0 • 0	• 0.3	. G.O
0.0	, 0.0	• 0.0	. 0.0	• 0.0	, c.o
2.0	. 0.0	• 0.0 • 0.0	• 0.0	. 0.0	, 0.0
0.0	• 0.0	. 0.0	• 0.0	• 0.0	. 0.0
0.0	. C.O		, 0.0	• 0.0	. 0.0
0.0	. 0.0	• 6.0	• 0.0	• 0.0	. 0.0
0.0	• 0.0	• 0.0	, 0.0	. 0.0	. C.O
0.0	• C•C	• 0.0	, 0.0	• 3.0	. 0.0
0.0	. 0.0	, 0.0	. 0.0	, 0.0	. 0.0
2.0		. 0.0	• 0.0	• 0.0	. C.O
0.0		. 0.0	• 0.0	.VKNTY= C.O	•
0.0	. 0.0	. 0.0	. 0.0	. 0.0	, U.O
0.0		• 0.0	• 0.0	. 0.0	. 0.0
0.0	A -	, 0.0	• 0.0	• 0.0	, 0.0
0.0		• 0.0	. 0.0	• 0•0	. 0.0
0.0	• 6•0	• 0.0	. 0.0	. 0.0	. C.O
0.0	• 6•0	• 0.0	• 0.0	• 2•0	. 0.0
0.0	• 0•0	. 0.0	• 0.0	, 0.3	. C.O
0.0	• 0.0	• 0.0	. 0.0	• 0.0	. 0.0
0.0	. 0.0	. 0.0	• 0.0	. 0.0	. 0.0
0.0	. 0.0	. 0.0	• 0.0	. 3.0	. 0.0
0.0	• 0.0	. 0.0	• 0.0	. 0.3	. 0.0
0.0	+ 0.0	. 0.0	• 0.0	. 0.0	, 0.0
30.000000	*WINDY* 3.000				0000 .
16.000000	• 27.900000	. 21.000000	15.000000	. 12.000,000	, 14.C
60.00000	. 34.000000	. 42.000000	42.000000	+0.000000	. 15.C
9•0	• 40.000000	• 30.000000	• 0 • 0	. 0.0	. 0.0
, •u	• 0.0	, 0.0	• 0.0	. 0.0	. 0.0

Figure 3-2. Sample of NAMELIST printout.

```
VPHSE
        NCRMAL MODE DISPERSION FUNCTION SIGN
0.60000
0.53793
        X---++-++-++--++--++
7.57586
        Y----
0.56379
        X---++--+--++--++
0.55172
        X---++---+
0.53966
        Y---++---+
        X----+--+---++---++---
0.52759
0.51552
        X----++--++---++---
0.50345
        X----++--++---++---
        X---++--++---++---
0.49138
1.47931
        X----++--++--
0.46724
        X----++--+++---+++
0.45517
        X---++--++
3.4431C
        >---++---++
3.43103
        X----++--++---+
0.41897
        X----++---
0.49690
        X----++---++---+++----++++---
0.39483
        X----++---+++
0.38276
        >----++----++-----+++
        X----+
0.37069
0.35862
        X----++----++---
0.34655
        X----+++
        X----++++----
0.33448
 0.32241
0.31034
        X-+++----
        X-+++-------++++++++++
 0.29828
28621
        X-++++-----
0.27414
0.26207
2.25000
DMEGA
        123456789012345678901234567890
        PHASE VELOCITY DIRECTION IS
                              35.0CODEGREES
OMEGA =
  0.50000E-02
             0.82759E-02
                       0.11552E-01
                                  C.14828E-01
                                             0.18103E-01
  0.21379E-01
             0.24655E-01
                       0.279315-01
                                  0.31207E-01
                                             C.34483E-01
                       0.44310E-01
                                  0.47586E-01
                                             0.50862E-01
  0.37759E-01
             0.41034E-01
                                             C.67241E-C1
  0.54138E-C1
             C.57414E-01
                       0.60690F-01
                                  0.63965E-01
                       0.77069E-01
                                  0.80345E-01
                                             0.83621E-01
  0.70517E-01
             0.73793E-01
             C.9C172E-01
                       0.93448E-01
                                  0.96724E-01
                                             0.13000E 30
  0.86896E-01
```

Figure 3-3. Tabulation of the normal mode dispersion function signs for the atmosphere of Figure 3-1 and a direction of propagation of 35° north of east.

```
NORMAL MODE DISPERSION FUNCTION SIGN
VPHSE
2.60000
0.58793
          ----++--++-+++++--+++--+++
0.57586
         ----+++--++--+++--+++--
0.56379
         ----++--++-
9.55172
       Y----+++--+++---++---
0.53966
       X----++--++--+
0.52759
          ----++--+++
0.51552
        0.50345
         0.49138
          -----++--++---
0.47931
        X----++--++---++----+++----+++-
0.46724
         ----++
         ------+
0.45517
0.4431C
          _____+
0.43103
         -----
0.41897
2.47690
          ----+---++++----+++--
C.39483
0.39276
         -----+
0.37069
0.35862
          -----++-----++-----+++---
0.34655
         ------++++
9.34052
0.33448
          -----+++++------++++++
3.32241
         ------++++++
0.31940
        X++-----++++++++
0.31789
        X-+++++--+++++-----+++
0.31713
0.31638
        X--+++++---++++
        Y--+++++-----++++---
7.31487
         -+++++----++
2.31336
0.31034
        X---+++++---
         ____.......
0.29828
0.28621
0.27414
3.26207
          _____
2.25000
        1234567890123456789012345678901234567
OMEGA
        PHASE VELOCITY DIRECTION IS 35.000DEGREES
NYEGA =
  0.50000E-02
            0.82759E-02
                      C.86853E-02
                                0.88901E-02
                                          C.93948E-02
            0.11552E-01
  0.99139E-02
                      0.14828E-01
                                0.18103E-C1
                                          0.21379E-01
            0.27931E-01
                      0.31207E-01
                                0.34483E-01
                                          C.37759E-01
  0.24655E-01
  0.41034E-C1
            0.44310E-01
                      0.45948E-01
                                C.46767E-01
                                          0.47586E-01
            C.54138E-01
                      0.57414E-01
                                0.60690E-01
                                          C.63965E-01
  0.50862F-01
            0.70517E-01
                      0.73793E-01
                                0.77069E-C1
                                          C.80345E-01
  0.67241E-01
  C.83621E-01
            C.86896F-01
                      0.88534E-01
                                0.90172E-C1
                                          C.9344BE-C1
            C.10000E 00
  0.96724E-01
```

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Figure 3-4. Expanded version of the table in Figure 3-3. Rows and columns have been added to make the modes distinct.

TABULATION OF FIRST

8 MODES

	MODE 1
OMEGA (RAD/SEC)	VPHSE (KM/SEC)
0.008276 0.008685 0.908890 0.009095 0.009914 0.011013	0.257854 0.256762 0.256238 0.255711 0.253487 0.249999
	MODE 2
OMEGA (RAD/SEC)	VPHSE (KM/SEC)
0.008276 0.008644 0.008685 0.008712 0.008785 0.008852 0.008890 0.008987 0.009095 0.009590 0.009914 0.010319 0.011192 0.011552 0.012215 0.013410	0.317475 0.317133 0.316778 0.316379 0.314870 0.313362 0.312499 0.310344 0.308013 0.298275 0.292628 0.286206 0.274137 0.269688 0.269688 0.262068
	MODE 3
OMEGA (RAD/SEC)	VPHSE (KM/SEC)
0.008276 0.008500 0.008621 C.008685 0.008727 0.008890 0.009095 0.009914 0.011552 C.014828 0.018103	0.328731 0.322413 0.319396 0.318234 0.317887 0.317615 0.317559 0.317503 0.317503 0.317446 0.317323 0.317161

Figure 3-5. A portion of the normal mode dispersion curve tabulation printed by INFRASONIC WAVEFORMS as determined using the table in Figure 3-4.

PHIL AND PHIZ PROFILE DATA.

IAPIMX = NO. CF LAYER FOR WHICH ABS(PHIL(IAPIMX)) IS A MAXIMUM IAPPMX = NO. OF LAYER FOR WHICH ABS(PHI2(IAP2MX)) IS A MAXIMUM

R1 = PHII(IAPIMX) / ABS(PHI2(IAP2MX))
R2 = PHI2(IAP2MX) / ABS(PHI2(IAP2MX))
R3 = PHI2(I) / ABS(PHI2(IAP2MX))
NZC1 = NO. CF TIMES PHI1 CHANGES SIGN
NZC2 = NO. OF TIMES PHI2 CHANGES SIGN

MODE 1

OMEGA	VPHSE	IAP1MX	R1	NZC 1	1AP2MX
0.00828	C.25785	34	7.09325	2	16
0.0869	0.25676	15	6.55537	2	16
0.00889	0.25624	15	6.57698	2	16
0.00909	C.25571	15	6.59924	2	٠ 16
0.00991	0.25349	15	6.69513	2	16
0.01101	C.25000	15	6.84304	2	16

MODE 2

CMEGA	VPHSE	IAP1MX	R1	NZC1	IAP2MX
0.00828	0.31748	33	2.07396	3	1
0.00854	G.31713	32	14.98704	3	i
0.00869	0.31678	32	28.47873	3	ī
0.00871	0.31638	32	39.86269	3	24
0.00878	C.31487	32	39.20818	ĭ	24
0.00885	0.31336	32	38.63559	ī	24
0.00885	C.31250	32	38.31291	i	24
0.00899	0.31034	32	37.49858	i	24
0.00909	0.30801	32	36.60118	i	24
0.00955	C.29828	31	33.53206	i	23
0.00991	0.29 3	30	31.02254	ĩ	23
0.01032	0.28621	29	28.49094	i	23
0.01119	0.27414	28	25.01674	i	23
0.01155	0.26969	28	24.25139	i	23
0.01222	0.26207	28	22.75203	i	23
0.01341	0.25000	27	20.41315	i	23

Figure 3-6. Sample printout of ϕ_1 and ϕ_2 profile data

TABULATION OF SOURCE FREE AMPLITUDES FROM SUBROUTINE PAMPDE

HEIGHT HEIGHT	_	BURST = OBSERVER=	3.000 0.0	KM KM
FACT			0.558	KM/SEC
AL AM		*	1.173	

MODE	1		•	
	-	OMEGA	VPHSE	1MP
		0.00828	0.25785	-0.00455954
		0.00869	0.25676	-0.00459953
		0.00889	0.25624	-0.00459171
		C.OC9G9	0.25571	-0.00457545
		0.00991	0.25349	-0.00446189
		0.01101	0.25000	-6.90421712
		0.01101	0.23000	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,
MODE	2			440
		OMEGA	· VPHSE	AMP
		0.06828	C.31748	-0.02964770
		C.90864	0.31713	-0.02382846
		0.00869	0.31678	-0.01535239
		G.OC871	0.31638	-0.00928055
		0.00878	0.31487	-0.00245403
		0.00885	0.31336	-0.00113502
		0.00889	0.31250	-0.00082699
		C.0C899	0.31034	-0.00046585
		0.00909	0.30801	-0.00030775
		0.00959	0.29828	-0.00014295
		0.00991	0.29263	-0.00012778
		0.0103?	0.28621	-0.00013161
		0.01119	0.27414	-0.00019093
		0.01155	0,26969	-0.00023866
		0.01222	0.26207	-0.00038533
		0.01341	C. 25000	-0.00098984
MUDE	3		VPHSE	AMP
		OMEGA		-0.00006837
		0.00828	0.32873	-C.00049140
		0.00850	0.32241	-0.00049140
		0.00862	0.31940	-0.01440191
		0.00869	0.31823	-0.01440191
		0.00873	0.31789	-0.02886438
		C.00889	0.31761	-0.02937463
		0.00909	0.31756	-0.02952643
		0.00991	0.31750	-0.02792043

Figure 3-7. Tabulation of modes including the amplitude factor AMP which is independent of the source strength.

MODE TABULATION FOR Y= 10000.00 KILDTONS

MODE	1			
	OMEGA	VPHSE	AMPLTD	PHASE
	0.00828	0.25785	-67670.	3.72680
	0.00869	0.25676	-70010.	3.71697
	C.00889	0.25624	-70745.	3.71206
	C.009C9	0.25571	-71337.	3.70715
	5.00991	0.25349	-72784.	3.68753
	0.01191	0.25000	-72766.	3.66127
MODE	2			
	OMEGA	VPHSE	AMPL TO	PHASE
	C.CO828	0.31748	-3.96551E 05	3.7268C
	C.00864	0.31713	-3.25613E 05	3.71796
	C.C0869	0.31678	-2.10378E 05	3.71697
	C.C0871	0.31638	-1.27441E 05	3.71634
	C.00878	0.31487	-33915.	3.71458
	C.C0885	0.31336	-15781.	3.71297
	C.00889	0.31250	-11538.	3.71206
	C.03899	0.31034	-6555.5	3.70974
	C.C0909 C.C0959	0.30801	-4371.9	3.70715
	C.C0991	0.29828 0.29263	-2116.2	3.69529
	C.01032	0.28621	-1939.9 -2058.8	3.68753
	0.01119	0.27414	-3169.8	3.67785
	0.01155	0.26969	-4053.6	3.65701 3.64844
	C.01222	0.26207	-6811.7	3.63267
	0.01341	0.25000	-18688.	3.60436
MODE	3			
	OMEGA	VPHSE	AMPL TD	PHASE
	0.00828	0.32873	-898.67	2 72400
	C.00850	0.32241	-6606.2	3.72680 3.72143
	0.00862	0.31940	-47486.	3.71851
	C.C0869	0.31823	-1.96905E 05	3.71697
	0.00873	C.31789	-3.14976E 05	3.71596
	0.00889	0.31761	-3.94443E 05	3.71206
	0.00909	0.31756	-4.10974E 05	3.70715
	C.C0991	0.31750	-4.30359E 05	3.68753
	C.01155 C.01483	0.31745	-4.60767E 05	3.64844
	0.01403	0.31732	-5.10123E 05	3.57093

Figure 3-8. Tabulation of modes including the source-dependent amplitude and phase, AMPLTD and PHASE, respectively.

TABULATION OF RESPONSES

	TIME	TOTAL	MODE 1	MODE 2
ì	16000.0	-3.21	0.04	1.20
2	16015.0	-2.57	0.01	1.38
3	16030.0	1.87	-0.01	1.54
4	16045.0	3.34	-0.04	1.63
5	16060.0	-0.06	-0.06	1.79
6	16075.0	-1.70	-0.09	1.87
7	16090.0	1.47	-0.11	1.92
8	16105.0	3.41	-0.13	1.94
9	16120.0	0.42	~0.15	1.93
10	16135.0	-! -72	-0.17	1.83
11	16150.0	1.68	-0.18	1.81
12	16165.0	5.46	-0.19	1.70
13	16180.0	3.97	-0.20	1.57
14	16195.0	1.21	-0.20	1.41
15	16210.0	2.95	-0.20	1.23
16	16225.0	5.67	-0.19	1.03
17	16240.0	3.21	-0.18	0.81
18	16255.0	-0.95	-0.16	€.58
19	16270.C	0.80	-0.15	0.34
SÚ	16285.0	6.37	-0.12	6.09
21 22	16300.0	7.21	-0.10	-0.16
23	16315.0	3.09	-0.07	-0.41
24	16330.0	1.78	-0.04	-0.65
25	16345.0 16360.0	4.58 4.56	-0.01	-0.88
26	16375.0	0.16	0.02	-1.09
27	16390.0	~1.55	0.05	-1.29
28	16405.0	1.82	0.08 0.10	-1.47
29	16420.0	3.29	0.13	-1.62 -1.75
30	16435.0	-0.45	0.16	-1.85
31	16450 • C	-2.80	0.18	-1.92
32	16465.0	0.15	0.19	-1.96
33	16480.0	1.79	0.21	-1.96
34	16495.0	-2.78	0.21	-1.93
35	16510.0	-6.93	0.22	-1.88
36	16525.0	-4.05	0.22	-1.79
37	16540.0	0.15	0.21	-1.67
38	16555.0	-2.20	0 • 20	-1.53
39	16570.0	-6.80	0.19	-1.36
40	16585.0	-5.11	0.17	-1.17
41	16600.0	-0.42	0.15	-0.96
42	16615.0	-2.15	0.13	-0.73
43	16630.0	-8.42	0.10	-0.50
44	16645.0	-8.92	0.07	-0.25

Figure 3-9. Sample printout of the total and modal pressure histories. The time is given in seconds after the blast, and pressure in dynes/cm².

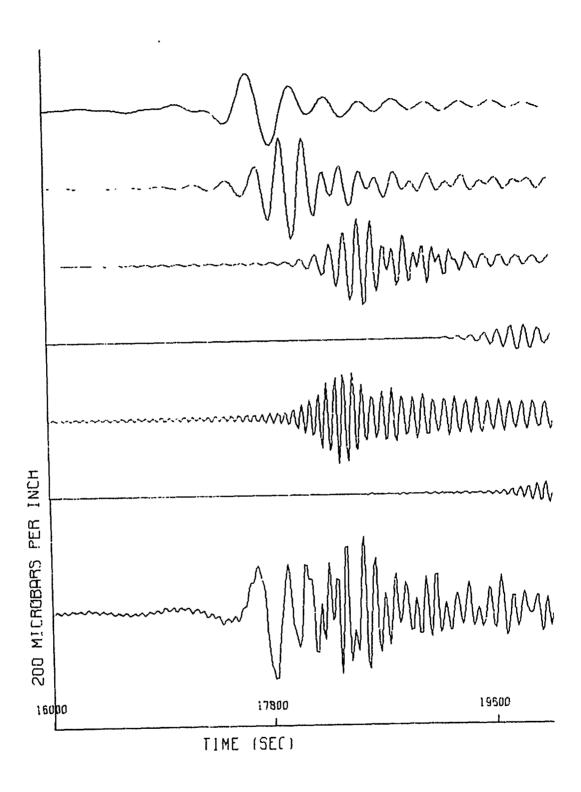


Figure 3-10. CALCOMP plot of modal and total waveforms on a common time axis and with a common pressure scale. (Reduced to 250 µbars per inch.) See Figure 3-12 for a complete listing of the input data.

It is at the user's discretion as to just what output is actually realized in a given run of the program. A fuller discussion of input and output variables is given in subsequent sections.

3.3 INPUT PARAMETERS CHARACTERIZING THE ATMOSPHERE, THE SOURCE, AND THE OBSERVER LOCATION

The atmosphere model is characterized by three possible sets of parameters. These are listed below:

Set 1	Set 2	Set 3
IMAX	XAMI	XAMI
T	T	CI
VKNTX	MÍŅDY	VXI
VKNTY	WANGLE	VYI
LANGLE	LANGLE	
ZI	ZI	HI

The variables which appear in these three lists are defined below:

- 1) IMAX is the number of layers of finite thickness in the multilayer atmosphere. It is an integer and may take any value between 2 and 99, inclusive.
- 2) T is the absolute temperature in degrees Kelvin. It is a subscripted real variable; T(1) is the temperature in the lowest layer; T(IMAX + 1) is the temperature in the upper half space. (The layers are numbered from the bottom.) Exactly IMAX + 1 values T(I) should be supplied.
- 3) CI is a subscripted real variable representing sound speed in km/sec. CI(I) is the sound speed in the I-th layer. Exactly IMAX + 1 values should be supplied.
- 4) VKNTX and VKNTY are subscripted (IMAX + 1 values) representing x and y components of wind speed in knots of the IMAX + 1 layers (including the upper half space).
- 5) WINDY is a subscripted variable (IMAX + 1 values) representing the wind velocity magnitude in knots of the IMAX + 1 layers.
- 6) WANGLE is a subscripted variable (IMAX + 1 values) representing the wind velocity direction in degrees, reckoned counterclockwise from the x axis.

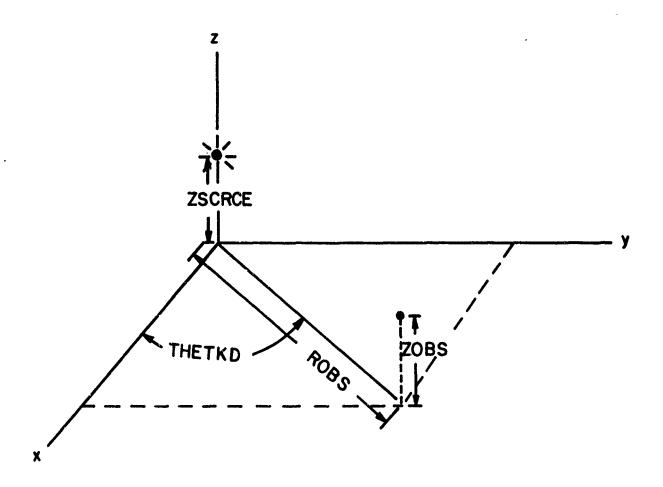


Figure 3-11. Sketch showing the geometrical meaning of some of the input data for INFRASONIC WAVEFORMS.

- 7) LANGLE is an integer. If it is 0 or negative, the computer is being told that set 1 (VKNTX and VKNTY) is supplied. If it is positive, set 2 (WINDY and WANGLE) is being supplied.
- 8) ZI(I) is the height above the ground of the top of the I-th layer of finite thickness. Its dimensions should be km. Exactly IMAX values should be supplied.
- 9) HI(I) is the thickness in km of the I-th layer of finite thickness. IMAX values are supplied.

The manner in which the computer is instructed as to when set 3 rather than sets 1 or 2 is being supplied depends on the value of a control integer NSTART which has previously been input. Briefly, NSTART being 1 implies sets 1 or 2 are being input, while NSTART = 2 implies set 3 is being read. This is discussed further in Sec. 3.5.

The source model is specified by two parameters YIELD and ZSCRCE:

- 1) YIELD is the yield of the explosion in KT.
- 2) ZSCRCE is the height above the ground in km of the explosion.

The observer location is specified by parameters ROBS, ZOBS, and THETKD:

- 1) ROBS is the magnitude of the horizontal distance in km between source and observer.
- 2) THETKD is the angle in degrees, reckoned counterclockwise, which the horizontal component of the vector from source to observer makes with the x axis.
 - 3) ZOBS is the height in km above the ground of the observer.

The meaning of these parameters is further illustrated by Fig. 3-11.

3.4 INPUT PARAMETERS CONTROLLING THE METHOD OF COMPUTATION AND OUTPUT

A major portion of the computation is concerned with the determination of the dispersion curves (phase velocity versus angular frequency) of the guided modes. Just which modes and which segments of modes are found and used in subsequent calculations depends on the search region in the phase velocity vs. frequency plane. This rectangular search region is specified by the following parameters:

1) OM1 is the lower angular frequency limit (rad/sec) of the search region.

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- 2) OM2 is the upper angular frequency limit (rad/sec) of the search region.
- 3) V1 is the lower phase velocity limit (km/sec) of the search region.
- 4) V2 is the lower phase velocity limit (km/sec) of the search region.

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Generally, one should select VI to be larger than the maximum wind speed in the model atmosphere. It is also advisable that one not take OMI identically equal to 0, as this could conceivably lead to machine overflow and termination of a given run.

The details of the search for modes within the rectangular search region depend on the initial choice of the number of points at which the sign of the normal mode dispersion function is tabulated. As is explained in Sec. 2.7, the numerical computation begins with the generation of an array of points, lying on a rectangular grid, covering the search region. The total number of intersection points in this grid is determined by two integers:

- 1) NOMI is the number of equally spaced constant frequency lines comprising the vertical lines of the grid.
- 2) NVPI is the number of equally spaced constant phase velocity lines comprising the horizontal lines of the grid.

Both NOMI and NVPI should be between 2 and 100, inclusive. In our own calculations, we have generally taken both of these integers to be 30.

The modes found in the search region are numbered consecutively, starting from the lower left corner of the region. (Phase velocity increases upwards and frequency increases to the right.) A key input parameter in this respect is the maximum number of modes MAXMOD which are to be tabulated and used in the subsequency waveform synthesis. If, for example, MAXMOD is 5, the program will not tabulate or use modes 6, 7, etc. The maximum value of MAXMOD permitted by the current version of the program is 10. In our computations, we generally use 10 unless we have some reason to believe that the higher order modes will not contribute appreciably to the wave form during the time interval of interest.

For the tabulation and graphing of pressure waveforms versus time, it is necessary to specify the time interval of the computed

waveform and the time increment between successive times at which the pressure is tabulated. The parameters specifying these quantities are listed below:

- 1) TFIRST is the earliest time in seconds relative to time of detonation at which computations are performed.
- 2) TEND is the latest time in seconds relative to time of detonation at which computations are performed.
- 3) DELTT is the time increment in seconds for which successive waveform points are tabulated.

In choosing these quantities, care should be taken to insure that the number of time points (TEND-TFIRST)/DELTT is less than 1000, since otherwise incorrect values could be obtained through storage spillover. For all realistic cases which we have considered, it appears sufficient to take DELTT > 6 sec. It is meaningless to take DELTT much less than (1/20) of 1/0M2. The choice of TFIRST and TEND is generally made with the intent of including the main pulse, which travels with speeds of the order of the sound speed at the ground. The nature of the theory suggests that the computations will generally not be too reliable at times much later than this. Some trial and error may be required to deterwine the optimum choice of TFIRST and TEND in relation to the observer distance ROBS. The examples treated in the following chapter may be of some assistance in this respect. Also, the experimental waveforms should in principle give a clue to the proper choice.

The nature and extent of the output is specified by a number of additional input parameters. If one wants a maximum of printout of intermediate values, he specifies NPRNT = 1 (or any other positive integer); if he wants a minimum, he specifies NPRNT = 0 (or any negative integer). In the latter case, the input is listed, the tabulation of waveform pressure versus time is given, and the waveforms are plotted. In any nonroutine operation of the program, it is probably advisable to set NPRNT = 1. However, this does lead to a tremendous amount of printout, and, if the current run only represents a slight modification of a previous run, one may want to set NPRNT = -1.

The program also allows for the option to <u>punch</u> out intermediate results on cards. The format of the punched cards is such that they may be used in later runs of the program as input in order to save machine time. If one desires this option, he should set NPNCH = 1. Otherwise, he should set NPNCH = 0. In general, it is advisable to avoid requesting NPNCH = 1 unless one plans an

immediate use of the cards. Otherwise, the bookkeeping chores of keeping track of a large number of cards may get out of hand. However, the computer time saved (which may be of the order of 10 minutes of 360 time) is not negligible, and one may sometimes wish to exercise this option.

To limit the number of plots on the CALCOMP graph and the number of modal waveforms tabulated on the printout, an input parameter IOPT is used. If IOPT is 1,2,..., 10, only the contribution to the waveform from mode number IOPT is calculated, printed, and plotted. If IOPT is 11, the computer calculates, prints, and plots all modal waveforms, as well as the total waveform. If IOPT is 12, all modal waveforms are computed, but only the total waveform is tabulated and plotted. Normally, one might wish to set IOPT = 11 and obtain all possible auxiliary results. However, in routine operation, when the qualitative properties of the individual modal waveforms are a priori known, one might set IOPT = 12. In some special cases, when one is interested in only one particular mode, he might set IOPT equal to 1,2,3,..., or 10.

3.5 PREPARATION OF THE INPUT DECK

The program is written such that all input data should be supplied in the NAMELIST format, which is a standard feature of FORTRAN IV for the IBM 360 and the IBM 7094. We find that NAMELIST is particularly convenient because it enables us to supply only the data which is needed for a given calculation and because it minimizes the possibility of keypunching errors during preparation of the input deck. For a description of NAMELIST we refer the reader to any of the FORTRAN IV manuals.

The main program has ten NAMELIST statements, each defining the data which may be read in when the computation executes a READ statement with a particular NAME. The NAMES of the possible data sets are numbered NAM1, NAM2, ..., NAM10.

For convenience of reference, these namelist statements are reproduced below:

NAMELIST /NAM1/ NSTART, NPRNT, NPNCH

NAMELIST /NAM2/ LANGLE, IMAX, T, VKNTX, VKNTY, WINDY, WANGLE, ZI

NAMELIST /NAM3/ IMAX, CI, VXI, VYI, HI

NAMELIST /NAM4/ THETKD, V1, V2, OM1, OM2, NOMI, NVPI, MAXMOD

NAMELIST /NAM5/ IMAX, CI, VXI, VYI, HI, THETKD, MDFND, KST,

KFIN, OMMOD, VPMOD

NAMELIST /NAM6/ ZSCRCE, ZOBS

NAMELIST /NAM7/ CMMOD, VPMOD, MDFND, KST, KFIN, AMP, ALAM, FACT

NAMELIST /NAM8/ YIELD

NAMELIST /NAM9/ MDFND, KST, KFIN, OMMOD, VPMOD, AMPLTD, PHASQ

NAMELIST /NAM10/ TFIRST, TEND, DELTT, ROBS, IOPT

In any given run with the program, the <u>first card</u> in the data card pack should be a NAM1 card. This card should generally be of the form

&NAM1 NSTART= NPRNT= NPNCH = &END

with desired values supplied for the parameters NSTART, NPRNT, NPNCH. The order of these three quantities is irrelevant. Furthermore, the name, equal sign, and value of any of them may be omitted if one desires to use the value of 0 for any of them.

The cards following the first depend on the value of NSTART. Unless one is supplying data in the form of intermediate results computed during previous runs, he would take NSTART =1. Given that NSTART=1, the data cards following should be those corresponding to NAM2, NAM4, NAM6, NAM8, and NAM10, in that order. Only nonzero values or values of quantities which will be used in the computation need be supplied. Thus, for example, if one sets LANGLE=0 (See Sec. 3.3.), then he need not list the values of WINDY or WANGLE in the NAM2 data group. Values of subscripted variables should be listed in the format (for example)

VKNTX = 0., 0., 2.0, 2.0, 5.0, 7.5, 5.0, VKNTY =

signifying that VKNTX(1)=0.,VKNTX(2)=0.,VKNTX(3)=2.0, etc. Note that, even though the first two numbers are 0, they could not be omitted, since otherwise the computer would consider 2.0 to be VKNTX(1). However, a long string of identical numbers can be abbreviated by writing 6*0., for example, for a string of six zeros. It must be emphasized that elements with indices greater than the largest index for that variable used in the computation need not be supplied. In other words, just because 100 spaces of storage are alotted to VKNTX does not imply that 100 numbers need be listed in the input.

If NSTART=2, one supplies NAM3, NAM4, NAM6, NAM8, NAM10. If NSTART=4, one supplies NAM7, NAM8, NAM10. If NSTART=5, one supplies NAM9,NAM10. This procedure is described in greater detail in the first two pages of the deck listing of the main program in Appendix B. The option of taking NSTART=2, 3, 4, or 5 simply allows one to

make use of intermediate results calculated in previous runs of the program. The data in NAM3, NAM5, NAM7, or NAM9 would generally have been punched in NAMELIST format during a previous run. We did not define all of the input variables in these latter lists in the preceding two sections since, in normal operation, those variables omitted would be specified by the computer (through the punching process) rather than by the user. The variables in NAM3 are a possible exception, as NAM3, through the NSTART=2 option, simply provides the possibility of supplying the parameters defining the model atmosphere in a manner other than that implied by NSTART=1. This has been discussed in Sec. 3.3.

A list of all possible input variables and their definitions is given on pages 3, 4, 5, of the deck listing of the main program in Appendix B.

The last card read in corresponding to a given problem is always the NAM10 card. The very next card should always be a NAM1 card. If the problem previously considered is the last problem to be computed in the run, one specifies NSTART=6 in the NAM1 list and needs not specify the values of NPRNT or NPNCH. If not, he specifies NSTART=1,2,3,4, or 5 and gives his data cards in one of the sequences and formats described above. The rules for providing data for successive problems are similar to those for the first with one exception. If the user fails to provide a value for any quantity, the value assumed by the computer for that quantity will be that value currently stored in the machine which may not necessarily be zero. Also, even though the user may wish to use all the values previously input through a (for exemple) NAM2 list, he must put a NAM2 card in the portion of the deck corresponding to the current problem. Such a card would be of the form

&NAM2 (blanks) &END

It is in successive problems that the option of taking NSTART=2, 3, 4, or 5 may find its greatest utility. For example, if one wished to study the effect of yield with all other variables fixed, he could take his data for the second and successive problems in the form

&NAM1	NSTART≈4	∝END
&nam7		&END
8man3	YIELD=2000	&END
&NAM10		&END

```
ENAM1 NSTART=1.
                    NPRNT=1.
                                NPNCH= -1 EEND
ENAM2
IMAX =
71=1.,2.,4.,6.,8.,10.,12.,14.,16.,18.,20.,25.,30.,35.,40.,45.,55.,
     65. . 75. . 85. . 95. . 105. . 115. . 125. . 135. . 145. . 155. . 165. . 175. . 185. . 195. .
     205 . . 225 . .
T=292..288..270..260..249..236..225..215..205..198..205..215..227..
     237.,249.,265.,260.,240.,205.,185.,184.,200.,250.,400.,570.,730.,
     925., 1080. . 1180. . 1255. . 1320. . 1390. . 1460. . 1600. .
LANGLE = 1.
WINDY=3...3...9...9...19...25...30...27...21...15...12...14...4...4...16...34...42...
     42. +40. +15. +10. +20. +60. +40. +20. +9*0. +
WANGLE=-45. -45. ,6+0.,22.,45.,200. ,180. .180. .7*0.,180. .13+C.,
&END
SNAM4
THETKD = 35.
V1 = 0.25, V2 = 0.6.
OM1 = 0.005.
                DM2 = 0.1.
NOM1 = 30.
               NVPI = 30.
PAXPOD = 8.
EEND
          ZSCRCE = 3.0.
                             2085 = 0.0
                                             EEND
ENAM6
BHANS
         Y ! ELD # 10. E3
                            & END
SNAM10
           ROBS = 5600 ..
TFIRST = 16.E3.
                    TEND = 21.E3.
DELTT = 15..
   TOPT = 11.
EFND
```

Figure 3-12. A listing of the input data used in an effort to match the microbarogram recorded at Berkeley, California, following a blast at Johnson Island on 30 October, 1962. The synthesized waveform is shown in Figure 3-10 and is compared with the empirical record in Figure 4-23.

The value of YIELD would vary for successive problems. It should be noted that the above would save considerable computer time when compared with the option of taking NSTART=1.

To illustrate some of the points discussed above, a listing of a sample input deck is given in Fig. 3-12. The resulting output should include that shown in Figs. 3-1 through 3-10.

3.6 FURTHER DESCRIPTION OF THE OUTPUT

In Figs. 3-1 through 3-10 we show a selected portion of the output generated by the program with the input deck listed in Fig. 3-12. This output is representative of what might be obtained during normal usage of the program.

Figure 3-1 gives the computer printout of the basic model atmosphere used in the calculation as derived from the input data. Its format should be self-explanatory.

Figure 3-3 gives the initial table or pictorial display of the normal mode dispersion function sign at points in the phase velocity versus angular frequency plane. The +'s and -"s denote the sign, while the X's imply that the upper boundary condition could not be satisfied. The row correspond to different values of the phase velocity VPHSE. These values in km/sec are listed in the first column. The columns correspond to different angular frequencies OMEGA. The w values corresponding to the rows (from left to right) are listed below the figure in the order in which one would read a book (left to right, then down a row. The sequence 1234 etc. of numbers directly below the figure is intended merely to facilitate counting. The number given for the phase velocity direction should be the same as the input value of THETKD.

Figure 3-4 represents an expanded version of the display given in Fig. 3-3. This is the result of the expansion process to fully resolve the modes which was described in Sec. 2.7. Since the rows and columns are now unequally spaced, the apparent graphs of the dispersion curves are not in a uniform scale.

Figure 3-5 gives a portion of the tabulation of the dispersion curves for the modes found during the search process. Note that only the segment of a mode which lies within the search region is tabulated. It also should be noted that the increments in OMEGA (in rad/sec) and VPHSE (km/sec) are not uniform. This is an attribute of the computational process which was selected in order to obtain good resolution of both nearly horizontal and nearly vertical segments of the dispersion curves.

Figs. 3-6, 3-7 and 3-8 each give the same information as in 3-5 plus tabulations of quantities which may be of interest to the user and which vary along the dispersion curves. It may be questioned whether the printout in Fig. 3-5 is necessary, but we decided on this superfluous output because of the fact that the information in Fig. 3-5 has a wider applicability than that in Figs. 3-7 and 3-8. Also, the user might wish to display the dispersion curve tabulations alone without having to explain away the presence of other data.

As in the case of the dispersion curves, the data listed in Fig. 3-6 is a function of the model atmosphere only. PHI1 and PHI2 are the ϕ_1 and ϕ_2 , respectively, introduced in Section 2.6. The values of these "potentials" are calculated at the ground and at the top of each finite layer in the model atmosphere, and these values are used in later calculations. Since the profiles of these functions might give the user some insight into the physical significance of the various modes in the computation, Fig. 3-6 shows a tabulation of profile parameters, as defined in that printout, for each point on the dispersion curves previously tabulated.

The factor AMP, which is tabulated in Figure 3-7, is defined by Eq. (2.5.4d) and depends on heights of burst and observer but is independent of yield. Also shown in this figure are the parameters FACT and ALAM (λ_0) which are defined in Sec. 2.5.

Figure 3-8 shows the form of the tabulation of AMPLTD and PHASE, which are defined in Sec. 2.5 and depend upon the yield of the source in addition to the atmospheric model and the heights of burst and observer.

Fig. 3-9 gives a portion of the printout of the total and modal acoustic pressures calculated in consequence of the input data shown in Fig. 3-12, while Fig. 3-10 is a reduction of the corresponding CALCOMP plot. In both the tabulation and the plot, pressures are given in microbars and time in seconds after the blast. On the plot, the modes are drawn in ascending order beginning at the top, and their total is at the bottom. The common pressure scale is determined automatically such that the maximum amplitude of the total waveform will be about 2 inches on the plot. Note that these formats for the tabulation and plot are consequences of having set IOPT = 11 in the namelist NAM10. A description of other possible output formats for predicted acoustic response may be found in the last paragraph of Section 3-4.

For each input case (i.e., for each NAM10 read), the code will print all input data and will generate a tabulation and plot

of a waveform; however, whether the outputs shown in Figs. 3-1 and 3-3 through 3-8 are printed will depend upon the current values of NPRNT and NSTART. If NPRNT is less than 1, none of them will be printed; otherwise, all are printed which correspond to points in the calculation past the point of entry specified by NSTART. For example, suppose that NPRNT = 1 and NSTART = 4. The first calculations made for this case are those involving the source strength (YIELD), so that the only printouts will be the input data, a tabulation of the type shown in Fig. 3-8, and a tabulation of responses (as determined by the value of IOPT).

Chapter IV

SOME NUMERICAL STUDIES

4.1 INTRODUCTION

In this chapter, we present some numerical studies which have been made during the past year using the computer program INFRA-SONIC WAVEFORMS, which we have described in the preceding two chapters. These studies were concerned with checking out the program, comparing its predictions with previous calculations by Harkrider (1964), and in exploring some general trends. These studies are relatively modest and only scratch the surface.

In these studies we refer to the individual modes using a nomenclature devised by Press and Harkrider (1962). For convenience of reference, we review this nomenclature here. In any plot of numerically obtained dispersion curves, i.e., of phase velocity versus frequency, the modal curves fall into two clearly defined groups - regardless of the value of θ_k . A sample plot is shown in Fig. 4-1. The identification GR_0 , GR_1 , GR_2 , etc. for the so-called "gravity modes" and S_0 , S_1 , S_2 , etc. for the so-called "sound modes" should be evident from the figure. In labeling these modes the first step is always to identify GR_0 and S_0 . These are two adjacent modes which are widely separated at low frequencies, GR_0 having a low frequency phase velocity of the order of the sound speed at the ground and S_0 having one which is considerably higher, of the order of the largest sound speed in the atmospheric profile. The two modes invariably become very close at a frequency of the order of a representative Brunt frequency in the lower atmosphere. However, the two modes do not cross. (The probable reason for this absence of an intersection is explained in Sec. 2.7).

Once GR_0 and S_0 are identified, the remaining modes are labeled in the order in which they appear. Thus S_1 , S_2 , S_3 , etc., are the modes corresponding to curves which would be encountered by one scanning upwards and to the right starting from S_0 , while R_1 , GR_2 , GR_3 , etc., are the modes encountered by one scanning downwards and to the left from GR_0 .

4.2 A COMPARISON WITH MARKRIDER'S RESULTS

Since the program is capable of synthesizing waveforms when the model atmosphere is without winds, it should in principle be

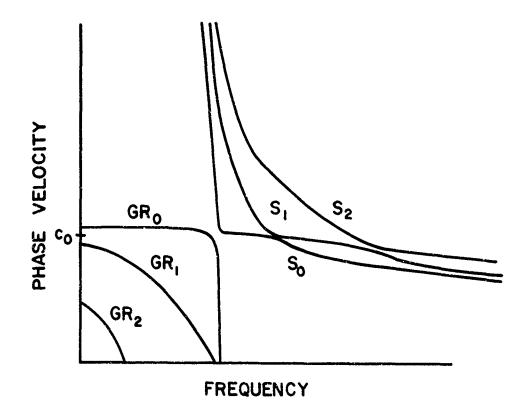


Figure 4-1. Sketch showing the labeling scheme used in this report for the acoustic-gravity modes.

capable of reproducing computations carried out by Harkrider (1964). Furthermore, any comparison of our calculations with Harkrider's should serve as a means of discovering any major coding errors in the program. We were therefore considerably disappointed when we first made such a comparison and discovered substantial discrepancies. Two fruitless months were spent in checking and rechecking the program and the theory before we finally discovered that the discrepancy was due primarily to differences in formulation. Such differences in the formulation evolve around how one incorporates a model of a nuclear explosion into the theory.

To explain this difference, we discuss below some of the differences between the mathematical expressions used by Hark-rider and those presented in Chapter II. In order to avoid a lengthy review of the Earkrider theory, we use his nomenclature below. For brevity, we do not define all the symbols used, as those not defined here are defined in Harkrider's paper.

The Harkrider theory gives the pressure waveform due to any given individual mode as being of the form

$$p = \{B\}e^{-\lambda}s^{a}s^{o}\rho_{B}^{o}(D)\{I_{1} + I_{2}\}$$
 (4.2.1)

where

$$I_{1} = 2 \int_{0}^{\sigma_{1}} \{L\} \{A_{A}\} \{M\} \{E\} \cos[\omega(t - \tau_{A})] d\omega \qquad (4.2.2a)$$

$$I_{2} = 2 \int_{\sigma_{1}}^{\infty} \{L\} \{A_{A}\} \{H\} \cos\{\omega[\tau - (\tau_{A} + \tau_{\chi})]\} d\omega \qquad (4.2.2b)$$

$$\{u\} = (2/\pi)^{1/2} (a_e \sin \theta)^{-1/2} a_s p_{as}$$
 (4.2.2c)

$$\{L\} = [p_s(D)/p_o]_{ii_j}$$
 (4.2.2d)

$$\{M\} = (b_s^2 + \omega^2)^{-1} k_j^{1/2}$$
 (4.2.2e)

$$\{E\} = \exp\{(a_s/\alpha_s)(\sigma_1^2 - \omega^2)^{1/2}\}\$$
 (4.2.2f)

The quantity σ_1 is $(\gamma/2)(g/\alpha)$ at the burst altitude. Note that the subscript s refers to the source and that α is the sound speed at the source. The quantity θ_e is the radius of the earth, while the quantity a is a scaling length which increases with yield Y as Y $\frac{1}{3}$; λ_s is σ_1/α_s ; D is source altitude.

The formula corresponding to Eq. (4.2.1) according to the formulation presented in Chapter II is

$$p = \{B\}\{1/\rho_s^o(D)\}\{1\}p_s^o/p_s^o$$
 (4.2.3)

where

$$\hat{I} = 2 \left[\{ K \} \{ AMP \} \{ N \} \cos \left[\omega \left(t - \tau_A + t_{as} \right) \right] d\omega \right] \qquad (4.2.4a)$$

$$\{ik\} = -(\alpha_s^2/\alpha_o)[\rho^{\circ}(z)\rho_s^{\circ}(D)]^{1/2}$$
 (4.2.4b)

The quantity $\{AMP\}$ is as defined in Eq. (2.5.4d).

With some minor discrepancies, it would appear from a comparison of the two derivations that

$$\{\kappa\}\{AMP\}\cong \{L\}\{A_A\}$$
 (4.2.5)

What discrepancies do appear would be due to the fact that we use an energy source model rather than a mass source model. To check whether or not this is the case and as a check on the program, we compared our $\{AMP\}$ with Harkrider's A when source and observer are on the ground (i.e., z=0 and $D^A=0$). In this case we should have

$$A_{\Lambda} = -\rho_{o}^{\bullet}\alpha_{o}^{\bullet}\{AMP\}$$

In Fig. 4-2, we show a plot of {AMP} in km⁻¹ vs. period in minutes for this case for the U.S. Standard atmosphere with no winds. This should be compared with Fig. 7 in Harkrider's 1964 paper. Although the units are not the same, the general shapes of the curves are remarkably similar. To check on the quantitative agreement, we took $\alpha = 1/3$ km/sec and $\rho = 12.6 \times 10^{-4}$ gm/cm³. The maximum value of $-\rho^{\circ}\alpha$ {AMP} for the GR₀ mode is then found from Fig. 4-2 to be .0126 x 10⁻³ (gm/cm³)/sec. The corresponding number in harkrider's graph (as best we can read it) is .013. Since Harkrider does not specify the units on this graph, we checked with him concerning this and found that 1 unit on the

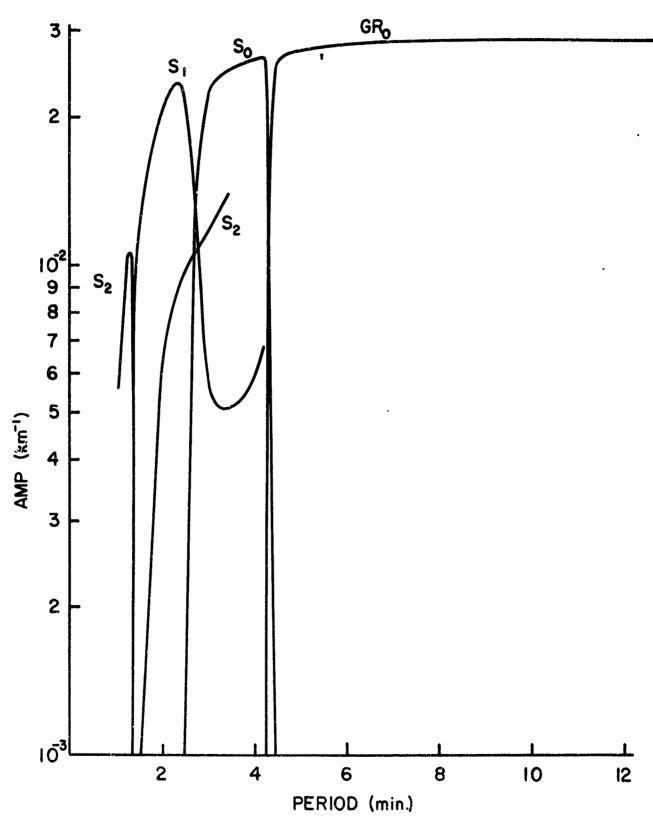


Figure 4-2. Plot of AMP vs. period for modes GR_0 , S_0 , S_1 , and S_2 . AMP is defined in Eq. (2.5.4d).

graph corresponds to 10^{-3} (gm/cm³)/sec. Thus the agreement would appear to be substantial.

The analysis above still leaves several additional formal differences which may or may not be of some importance, especially for megaton class explosions. We enumerate these explicitly below:

- 1) The factor $e^{-\lambda}s^{a}s$ in Eq. (4.2.1) does not appear in Eq. (4.2.3).
- 2) The factor {E} in Eq. (4.2.2a) for $\omega < \sigma_1$ does not appear in our Eq. (4.2.4a).
- 3) The quantity τ_χ in Eq. (4.2.4b) for $\omega > \sigma_1$ does not appear in our Eq. (4.2.4a).
- 4) The τ_A in Eqs. (4.2.2a) and (4.2.2b) is replaced by $\tau_A \tau_{as}$ in Eq. (4.2.4a).

Each of these differences may be traced to the methods in which the source model was incorporated in the theory. In Harkrider's theory, he matched his formal solution to the cube root scaled waveform (extrapolated from 1 KT) which would be received at a distance a directly below the source, the distance a varying with cube root scaling. In the theory in Chapter II, the source was taken as a point source with a time dependence chosen such that the calculation would agree with low yield explosion data were the atmosphere homogeneous. It is difficult to say with certainty just which formulation is the more nearly correct. However, one consequence of liarkrider's method is an effective attenuation of high frequencies as yield is increased - much more so than is indicated by the available data. (This would not have been the case were the reference point at the same altitude as the source.)

We consider the fourth distinction to be of no consequence as it only changes the time origin without altering the shape of the waveform. The other three should be relatively minor for low yields but may lead to large discrepancies for megaton class explosions.

To check the assumption that the first three distinctions listed above are responsible for any major numerical discrepancies between the results computed using INFRASONIC WAVEFORMS and those given by Harkrider, we attempted to reproduce the theoretical barograms in Harkrider's Fig. 13 for the direct wave as observed at 8000 km from a 4 MT explosion at a burst height of 2.13 km. We did this first using our program with no alterations and then

modifying (temporarily) the program to include the factors 1-3 discussed above. The results are shown in Figs. 4-3 through 4-8.

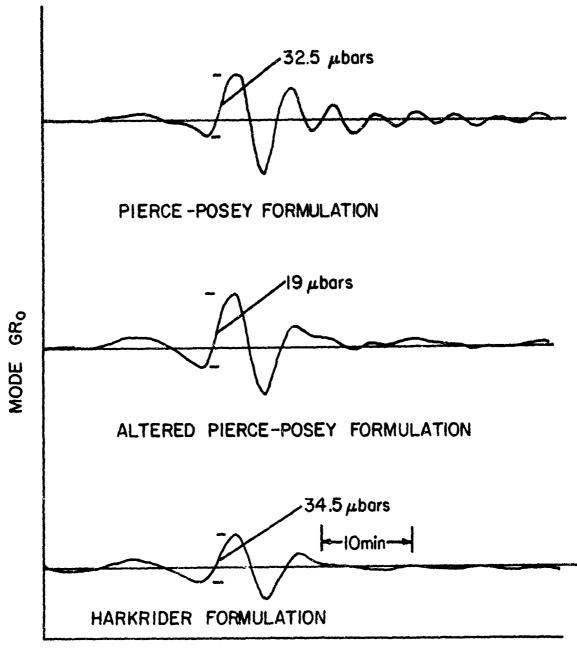
Each figure shows the graphs for a given mode (or the total response) as determined by three different methods. The top graph in each figure was calculated by the unaltered Pierce-Posey code. The second graph was calculated by the Pierce-Posey code with the factors $\exp[-\lambda a]$ and E and the phase shift τ included as noted above. The bottom curve is the corresponding graph from Harkrider's Fig. 13.

If we compare the unaltered modes with Harkrider's we note that the mode shapes are quite similar. However, three significant differences do exist:

- 1) Our GR_O dies off more slowly than does Harkrider's.
- 2) Our acoustic modes are much stronger relative to GR₀ than are Harkrider's.
- 3) All of our acoustic modes arrive approximately 3 minutes later relative to GR_Ω than do Harkrider's.

In our altered calculations, GR_0 dies out more rapidly, the acoustic modes are weaker relative to GR_0 than before, and the acoustic modes arrive slightly earlier relative to GR_0 . This clearly indicates that the factors and phase shift considered are the major sources of differences between Harkrider's synthesized waveform and ours. Our altered total response is almost identical with his up to about 26900 sec., where our S_3 begins to dominate the sum. Since S_3 is not included in Harkrider's sum, agreement could not be expected in this region.

The fact that the altered waveforms for each mode have amplitudes of about 2/3 those reported in Harkrider's figure may be attributed in part to the absence of the factor $\mathfrak{p}^\circ/\mathfrak{p}^\circ$ in Harkrider's original formulation. However, we understand that this has been corrected in the version of his program currently in operation. This would lower Harkrider's amplitudes by a factor of .76 and would bring the two sets of computations to a fair agreement. We are not sure of the cause of the remaining discrepancy but think it might be due to either our use of an energy source rather than a mass source or to a different choice for ambient density at the ground. The similarity in shape of the two waveforms suggests that the major cause of the discrepancy has been amply accounted for.



TIME

Figure 4-3. Comparison of mode CR as computed by Pierce and Posey and by Harkrider. Here and in Figs. 4-4 through 4-8, no two curves are neccessarily on the same pressure scale, but all use a common time scale. The value of a representative trough-to-peak pressure variation is given for each curve.

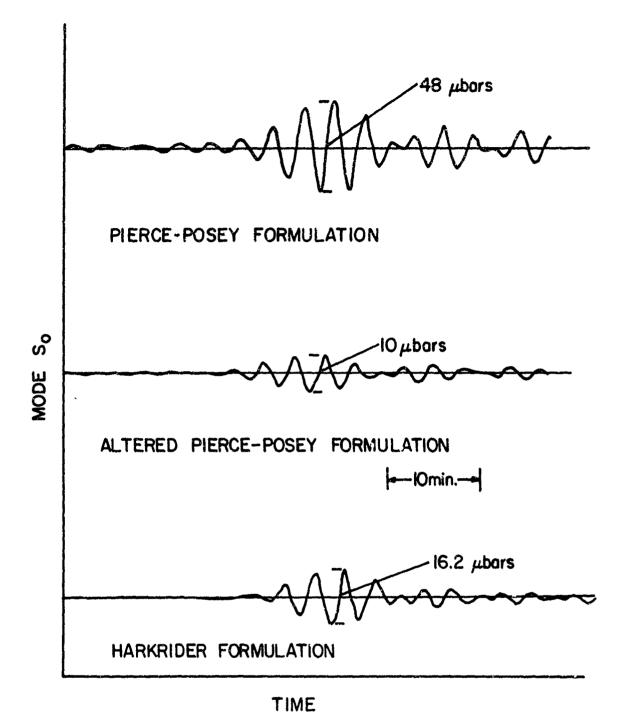
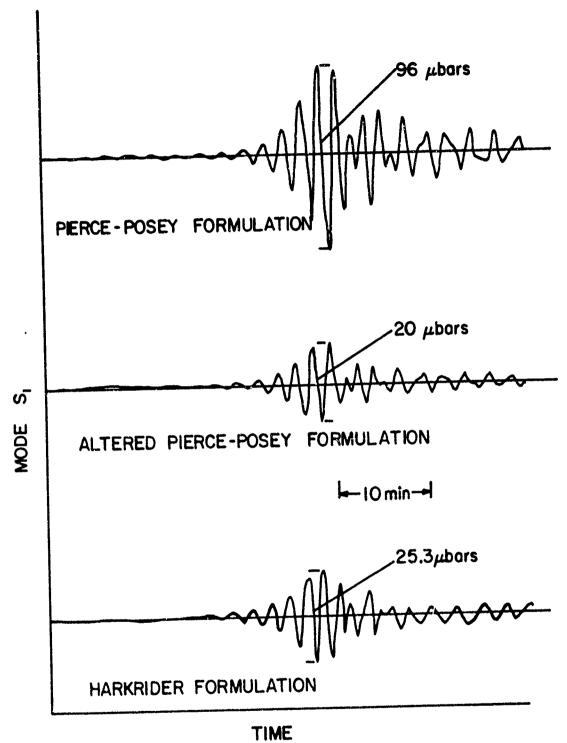


Figure 4-4. Comparison of mode S_0 as computed by Pierce and Posey and by Harkrider.



Comparison of mode \mathbf{S}_1 as computed by Pierce and Posey and by Pigure 4-5.

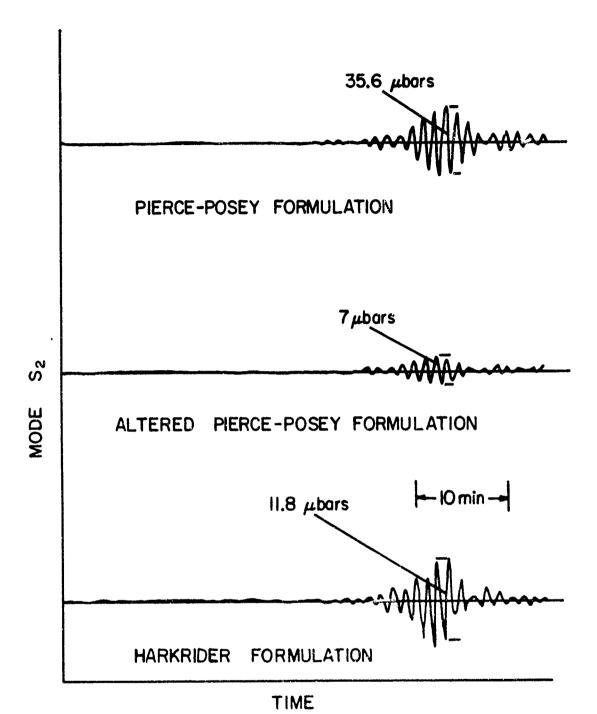
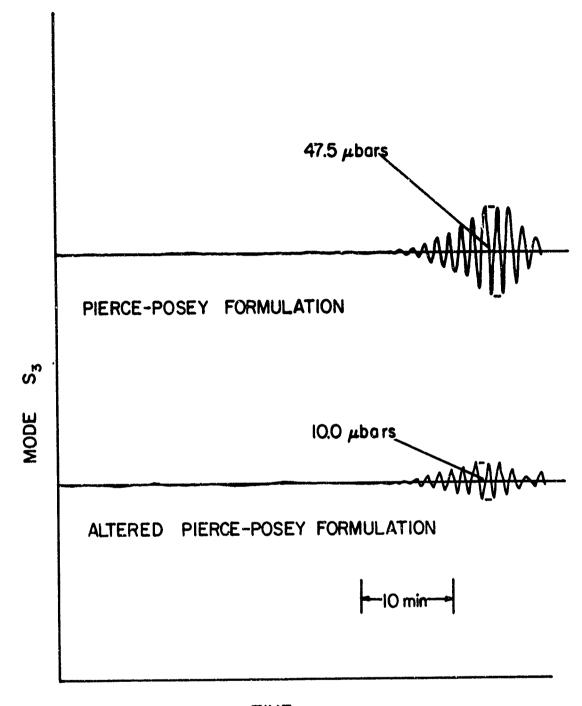
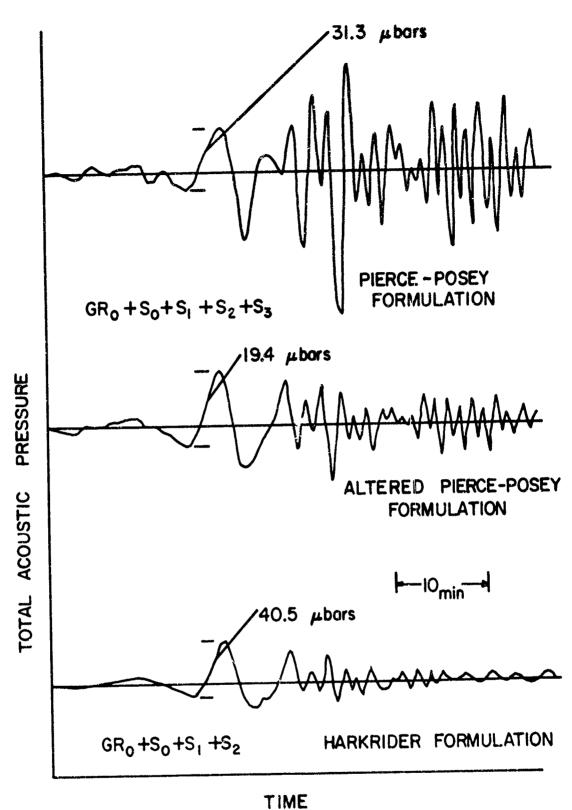


Figure 4-6. Comparison of mode \mathbf{S}_2 as computed by Pierce and Posey and by Harkrider.



TIME

Figure 4-7. Mode S_3 as computed by Pierce and Posey.



ure as computed by Pier

Figure 4-8. Total acoustic pressure as computed by Pierce and Posey's INFRASONIC WAVEFORMS, by the same code modified as indicated in Sec. 4.2, and by Harkrider's code.

4.3 GEHERAL TRENDS

The computer code INFRASONIC MAVEFORMS has been utilized to study the effects of the various parameters of the source (yield, height of burst) and of the atmospheric model (temperature and wind profiles, upper boundary condition) upon theoretical microbarograms. For the sake of simplicity and economy, models of only four to seven finite layers plus the upper half-space were used in this initial study. The temperature profile shown in Fig. 4-9 with no winds was chosen as a standard for the purposes of comparison. Notice that this profile exhibits certain features of the ARDC standard atmosphere: there are two sound channels, one centered at 25 km and one at 85 km, with the model's minimum temperature in the upper channel. Most runs were able using a yield of 10 MT, height of burst of 3 km and a range of 2000 km. The synthesized microbarogram for the standard conditions is given in Fig. 4-10 together with graphs of the modes summed to arrive at the total response.

The Upper Boundary Condition

As the altitude increases, the composition and density of the atmosphere changes considerably. As the composition changes, the application of the perfect gas law becomes less appropriate, and as the medium becomes increasingly rarified, the equations of hydrodynamics lose their applicability. However, under the assumption that practically all of the energy of a given disturbance is below 100 km, it would seem that the details of the atmospheric structure above the ionosphere should have little effect upon the waveform observed on the ground. This hypothesis was confirmed by a series of runs in which the atmosphere below 110 km was held constant, while the temperature profile above this height was varied. While dominant frequencies and amplitudes were, in general, unaffected, the details of the individual modal waveforms did vary, and two definite trends were observed.

If only the temperature in the upper half-space (T_∞) is varied, one sees that the two extremes, T small ("almost" a free boundary) and T large ("almost" a rigid boundary) produce microbarograms which look very similar (Fig. 4-11). But, if one compares the tables of the normal mode dispersion function signs for the two cases (Fig. 4-12), it is clear that in the process of going from one extreme to the other, the dispersion curves have shifted, since the sign of the normal mode dispersion function at any given point in the frequency-phase velocity plane has been reversed. Examination of intermediate cases reveals that the shift has been upward for increasing T_∞ ; i.e., the dispersion curve normally associated with the GR $_0$ mode in the free case moves upward and assumes the shape and position of the curve normally associated

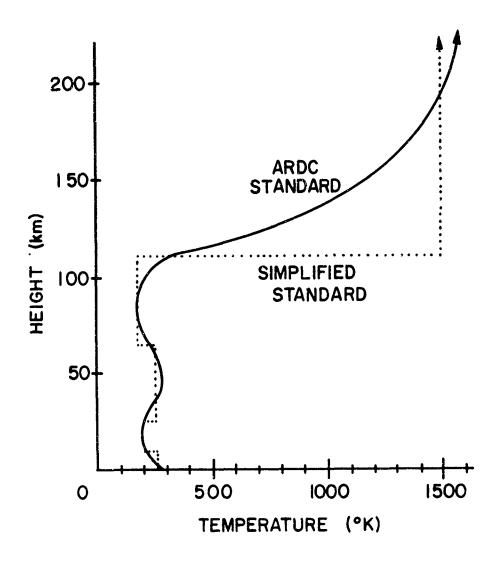


Figure 4-9. Temperature profiles of the ARDC standard atmosphere and of the standard simplified atmosphere used in Section 4.3.

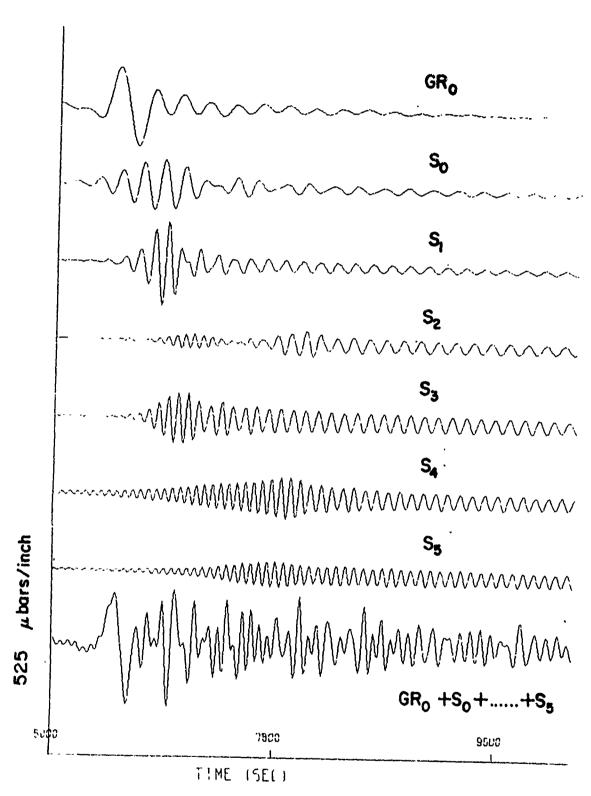


Figure 4-10. Synthesized microbarogram and modal contributions for an observer on the ground 2000 km from a 10 MT explosion 3 km above the ground in the simplified model atmosphere of Fig. 4-9.

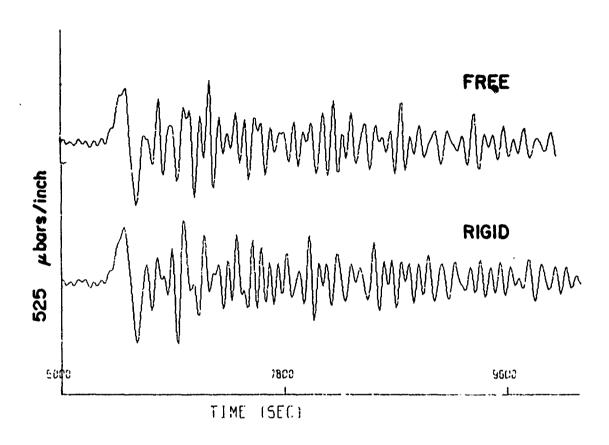


Figure 4-11. Synthesized microbarograms corresponding to free and rigid upper boundary conditions.

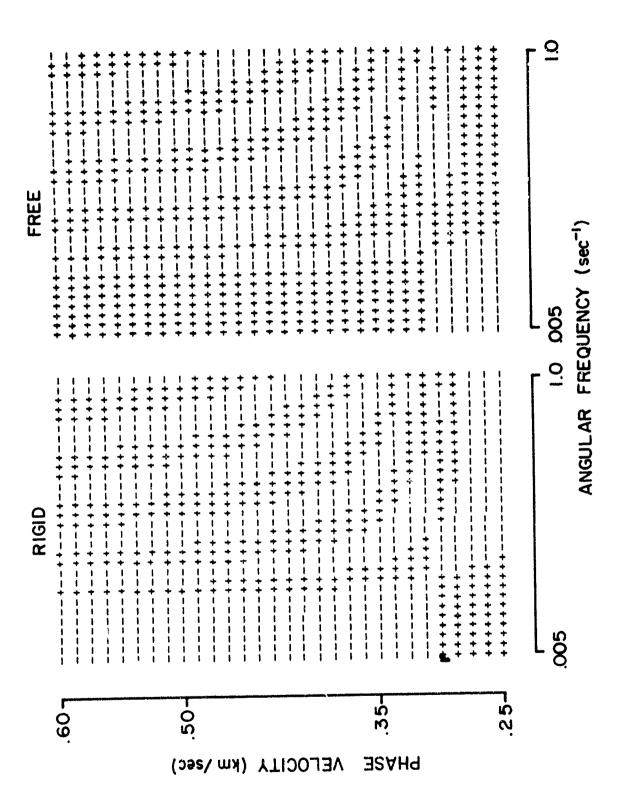


Figure 4-12, Tables of normal mode dispersion function signs for the cases of free and rigid upper boundary conditions.

with the S $_0$ mode. For an intermediate case, for which the modes are in the midst of their transitions, the modal disturbances bear little resemblance to those for the extremes, yet their total (Fig. 4-13) does resemble that for the extremes, at least for the first half hour. The suggestion made here is that because the dispersion curves are strongly dependent upon T_∞ , but the waveform is not, the modes which arise are primarily mathematical conveniences with limited physical significance. This contradicts the viewpoint prevalent in much of the current literature.

Secondly, as soon as the temperature in any layer is of the order of three times any relative maximum for the atmosphere below that layer, a rigid boundary condition at the bottom of that layer is approximated. For example, the two waveforms presented in Fig. 4-14 show almost negligible difference, although they were produced by two different models, one with $T_{\infty} = 800^{\circ}$ K beginning at 130 km and the other with temperatures of 800° K from 130 to 150 km, 1000° K from 150 to 200 km, and 1500° K above 200 km. It is clear that the additional layers in the second model had little effect upon the predicted microbarogram.

The Temperature Profile

The computer code being used in this study synthesizes micro-barograms by summing the theoretical contributions from guided modes. In general, there are three types of ducting mechanisms which might produce guided modes: (a) Lamb mode ducting, (b) sound channel ducting, and (c) discontinuity ducting. (See Figs. 4-15 through 4-17.) A Lamb mode exists in an isothermal atmosphere due simply to the presence of the ground. Its energy density decays exponentially with altitude. A sound channel exists at any altitude where the sound speed profile has a relative minimum. The third phenomenon which might contribute to ducting is a tendency in some circumstances for wave energy to be concentrated near discontinuities or in the region of large gradients of the sound speed.

Since we are generally concerned with the waveform observed at the ground due to a source near the ground, one would guess that the most important influence would be from Lamb mode ducting, with the effect of a sound channel being to strengthen or weaken the Lamb mode, depending upon its altitude and strength. The only large sound speed gradients in the atmosphere are at great heights. Thus, our earlier consideration of the effect of the upper boundary condiction tells us that this mechanism could not significantly contribute to ducting, except that a free or rigid boundary prohibits radiation of energy away from the earth and produces microbarograms (Fig. 4-11) which decay more slowly than those for intermediate cases (Fig. 4-13).

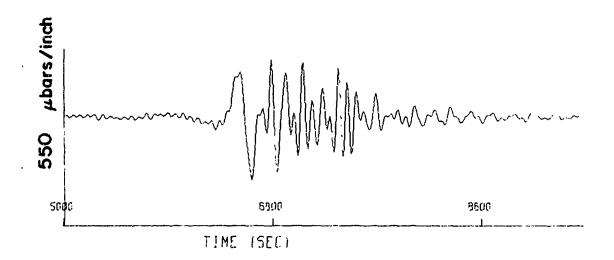


Figure 4-13. Pressure waveform for a case intermediate to the free and rigid upper boundary conditions. Here, T_{∞} = 300° K.

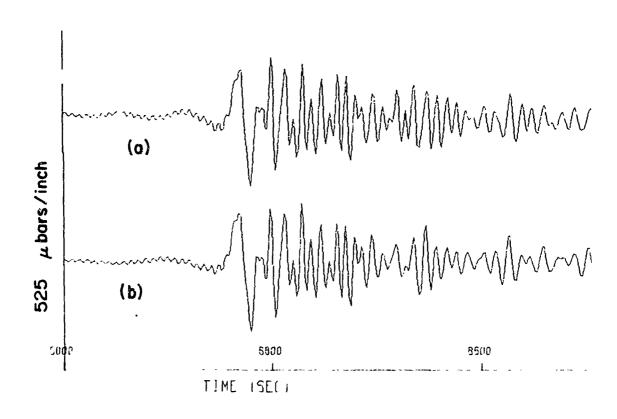


Figure 4-14. Synthesized microbarograms for (a) an atmosphere with $T_{\infty} = 800^{\circ}$ K beginning at 130 km and (b) an atmosphere with temperatures of 800° K from 130 to 150 km, 1000° K from 150 to 200 km and 1500° K above 200 km.

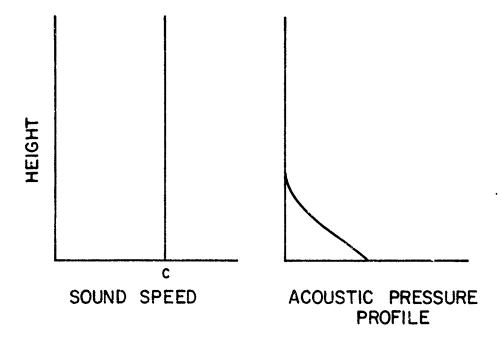


Figure 4-15. Sketch illustrating the mechanism of Lamb mode ducting. In an isothermal atmosphere, the Lamb mode has its maximum pressure at the ground and decays exponentially with height.

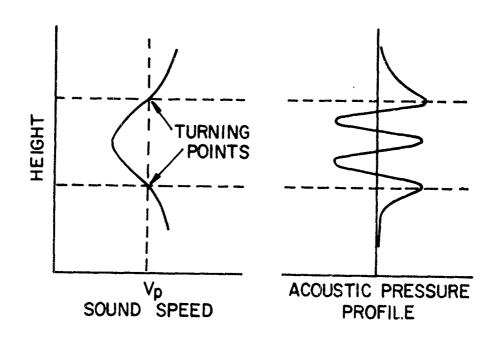


Figure 4-16. Sketch illustrating the mechanism of sound channel ducting. The energy of the disturbance is concentrated in the region of a relative sound speed minimum.

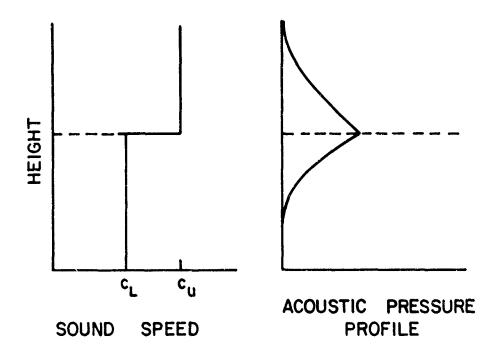


Figure 4-17. Sketch illustrating the phenomenon of discontinuity ducting. The pressure has its maximum value at the discontinuity in sound speed and decays exponentially with distance from it.

The hypothesis that Lamb mode ducting is the principal mechanism of propagation for the acoustic-gravity wave under consideration is discussed in more detail in Chapter VI. Here the effects of the two sound channels in the standard atmosphere are investigated. Since we assume that the atmosphere has constant composition and obeys the perfect gas law, the sound speed is proportional to the square root of the absolute temperature. The sound speed profile of our standard model is shown in Fig. 4-18, along with the sound channel variations studied. Variation 1 eliminates the lower channel, 2 increases the sound speed in the upper channel so that the minimum is in the lower channel, and 3 eliminates the upper channel.

Examination of the microbarograms (Figs. 4-19, 20, 21) corresponding to the three variations reveals a strong dependence upon both sound channels, since all three waveforms are different and none resembles the standard. By looking at the GR_0 , S_0 and S_1 modes, we see that their shapes and relative sizes seem to depend most strongly on the location of the minimum sound speed in the model. That is, the modes for variation 1 most resemble those of the standard, while the modal patterns of variations 2 and 3 resemble each other. Also, the entire GR_0 mode is almost the same for all cases, indicating that it is probably governed most strongly by Lamb ducting. Node S_0 shows its largest contribution to the ground level microbarogram in the two cases, variations 2 and 3, when the model has its minimum sound speed in the lower channel. This might mean that S_0 tends to concentrate its energy near the minimum sound speed, although to put much emphasis on this possibility would be somewhat inconsistent with our earlier conclution that the modes are of limited physical significance.

The Wind Profile

In studying the effects of winds, we find it convenient to define an equivalent sound speed, c = c + v·i, where c is the sound speed, v is the wind velocity vector, and i is a horizontal unit vector in the direction of propagation. Two windy models which were used to produce theoretical microbarograms (Fig. 4-22) both have c profiles the same as the standard atmosphere, but one, variation 4, has a c profile equal to the c profile of variation 1, and the other, variation 5, has a c profile equal to the c profile of variation 2. Notice that, even though winds are actually treated in a much more sophisticated manner than simply using c in the place of c (see Chapter II), the results imply that the sophistication has only slight effect on the predicted waveforms. The microbarograms for the vindy atmospheres, variations 4 and 5, very strongly resemble the records for the windless models having the same c profiles (variations 1 and 2, respectively). Thus, as long as the wind speed in every layer is

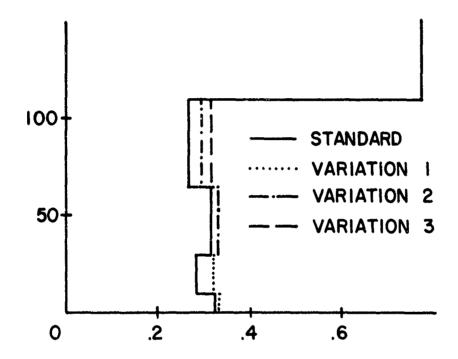


Figure 4-18. Sound speed profile for the standard temperature profile shown in Figure 4-9 and three variations studied.

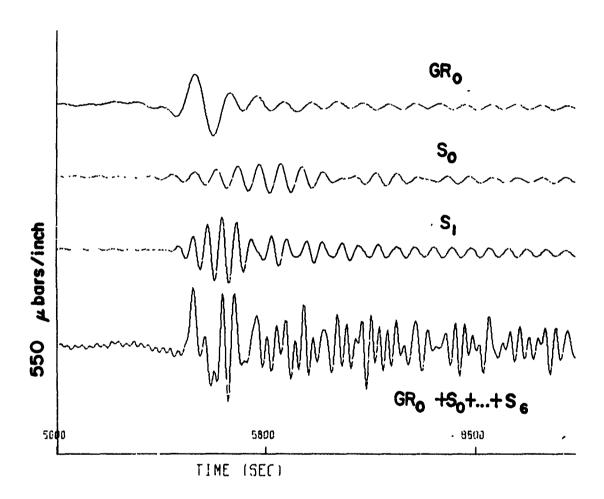


Figure 4-19. Microbarogram and three of the modes calculated using sound speed variation 1 (See Fig. 4-18).

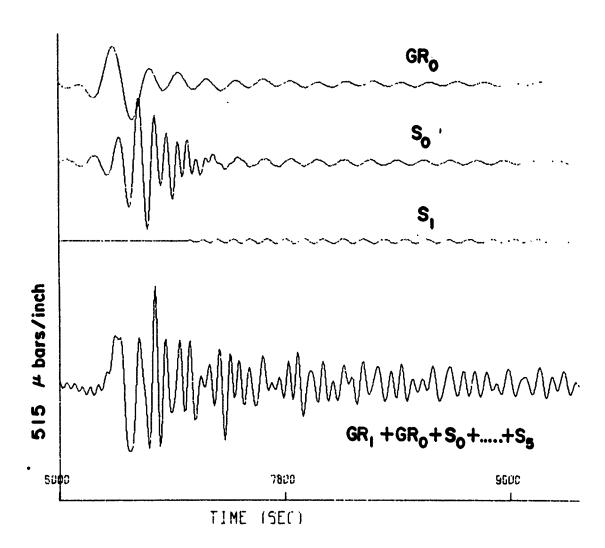


Figure 4-20. Microbarogram and three modes calculated using sound speed variation 2 (See Fig. 4-18).

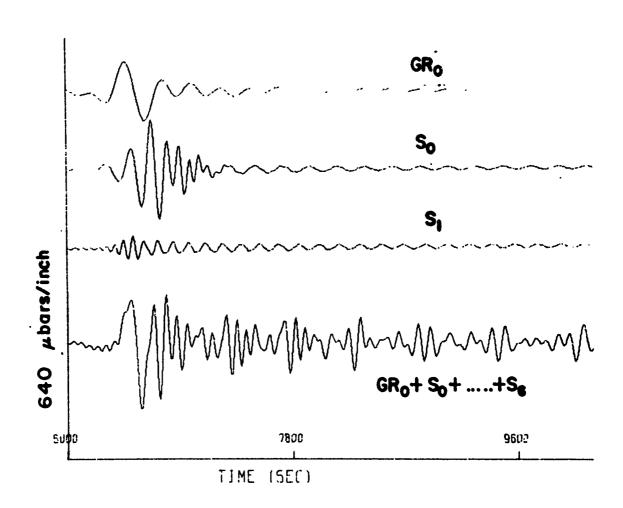


Figure 4-21. Microbarogram and three modes calculated using sound speed variation 3 (See Fig. 4-18).

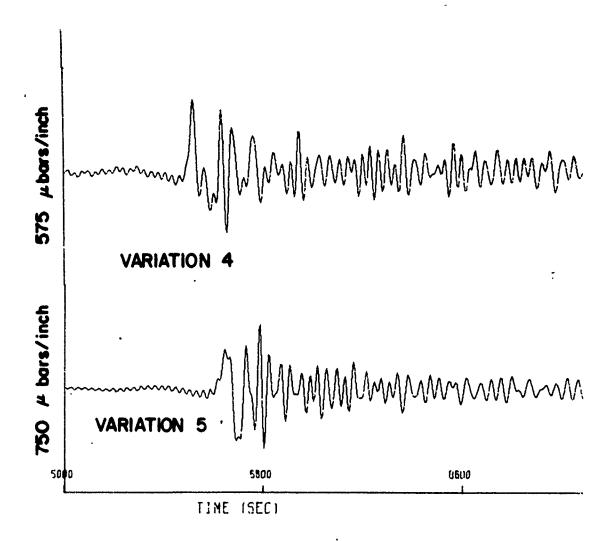


Figure 4-22. Microbarograms synthesized using the windy atmospheric models referred to as variations 4 and 5 in the text.

much less than the speed of sound for that layer, the major effect of the wind is simply to change the effective sound speed profile. In retrospect, it would appear that one need not incorporate winds into the computer code; instead he may use the device described above.

Source Parameters

COMMONIA ACTUAL ACTUAL

Test runs in which the source parameters were varied indicated (1) that, for bursts well below the sound speed minimum in the lower channel, the height of burst has relatively little effect on the shape of the generated wave and only slight effect on its amplitude and (2) that the yield of the explosion has little influence upon either the wave's shape or the ratio P' = (wave amplitude/yield). In one example studied, P' fell by 4% as the yield went from 18 MT to 30 MT. Iliff (private communication, 1970) has studied both of these types of variations in considerably more detail using INFRASONIC WAVEFORMS and finds that the height of burst effect is very significant at altitudes above 10 km. In particular, the wave amplitude on the ground tends to increase with height of burst up to an altitude of the order of 40 km for megaton class explosions and then decreases with increasing altitude. Also, the ratio P' shows the smallest variation with yield for the earliest portion of the waveform; the variation may be considerable for the later arrivals.

4.4 A COMPARISON WITH EMPIRICAL DATA

On 30 October, 1962, the United States exploded a thermonuclear bomb of the megaton range near Johnson Island. The collection of observed microbarograms published by Donn and Shaw [1967] contain several records made following this blast, one of which, the Berkeley record, appears exceptionally free of noise and appears representative of what might be expected for a waveform under ideal circumstances. (This judgment is not solely that of the authors, since this waveform was chosen by others for the cover of the program of the Symposium on Acoustic Gravity Waves, Boulder, Colorado, July, 1968.) Thus, it was felt that this was the waveform which we might have the best chance of matching with a theoretical synthesis.

In preparing the input for the program INFRASONIC WAVEFORMS, the most important decision is the choice of a model atmosphere. Unfortunately, there are three categories of atmospheres which strongly affect the waveform received: the atmosphere near the source determines the relative excitation of the modes, the atmosphere along the path of the disturbance determines how the wave propagates, and the atmosphere above the observer determine.

the ground strengths of the modes. Moreover, none of these atmospheres is constant over time or has winds and temperatures which are functions of altitude alone. Thus, in light of the fact that our model can neither be representative of the entire range of atmospheric profiles above the path nor display the inconsistency and horizontal inhomogeneity of any real atmosphere, exact agreement between theory and experiment would not be expected. Nevertheless, general agreement might be hoped for.

An atmospheric model was constructed to represent the average conditions between Johnson Island and Berkeley for the month of October. The temperature profile (Fig. 3-1) was taken from Valley's Handbook of Geophysics and Space Environments, Figures 2.2, 2.4, and 2.5, and the wind profile (Fig. 3-1) was taken from Valley's Figure 4.11 and Table 4.21 and from the 1965 COSPAR International Reference Atmosphere, p. 46.

Since the actual yield and height of burst for the source was not known, they were set arbitrarily at 10 MT and 3 km, respectively. A range of 5600 km and direction of propagation of 35° north of east were used. For a copy of the complete input data, see Fig. 3-12.

The synthesized waveform agrees surprisingly well with the observation (Fig. 4-23), both having the same time of arrival, a 5.5 minute period for the first major cycle, and the same dominant periods and relative amplitudes for about 35 minutes. Since Donn and Shaw did not give the amplitude of their record, an amplitude comparison cannot be made here. On the first major cycle of the synthesis, there is a variation of about 300 μ bars from peak to peak.

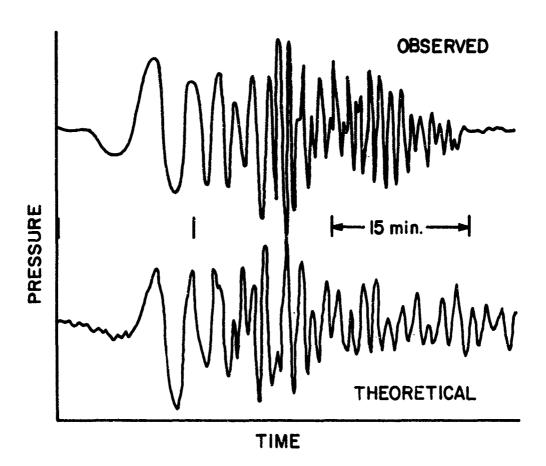


Figure 4-23. Comparison of theoretical and observed micro-barograms for Berkeley, California, following a nuclear blast near Johnson Island, 30 October, 1962. A listing of the complete input data for the synthesis is given in Fig. 3-12.

Chapter V

AN APPROXIMATE METHOD BASED ON

CAGNIARD'S INTEGRAL TRANSFORM TECHNIQUE

5.1 CAGNIARD'S METHOD

Cagniard's method is a technique utilizing mathematical properties of functions of a complex variable which allows one, under certain circumstances, to invert Fourier transforms. The technique dates back to Lamb's classic paper (1904) on the propagation of elastic transients on the surface of an elastic halfspace, but its significance was not realized until the 1930's when Cagniard, Pekeris, and Smirnov and Sobolov independently discovered that the technique may be applied to a much more general type of problem and developed the mathematical techniques in a more suitable form. The resulting method is generally called Cagniard's method, probably because of the fact that Cagniard's book (1939, 1962) was the first treatise on the subject to become known by the general seismological community.

Cagniard's method is generally acknowledged to be extremely complicated. This is due partly to the amount of algebra involved in using the method, to the fact that it does involve some intricate mathematical ideas, but primarily (in the authors' opinion) due to the rigorous style with emphasis on generality in Cagniard's book. The method was very little used until the mid 1950's when C.H. Dix attempted to give a simpler explanation of the method and demonstrated the fact that it leads to feasible quantitative predictions. Since the late 1950's a large number of papers have appeared on the subject with a wide scope of applications besides seismology.

In general terms, one may consider Cagniard's method to be concerned with the evaluation of integrals of the form

$$\psi(\overset{+}{x},t) = \int_{-\infty}^{\infty} \dots \int_{-\infty}^{\infty} e^{i\overset{+}{k}} \cdot \overset{+}{x} \int_{-\infty+i\varepsilon}^{\infty+i\varepsilon} e^{-i\omega t} F(\overset{+}{k},\omega) \ d\omega \ d^{n}k \quad (5.1.1)$$

where the number of dimensions of \vec{k} may, for all practical purposes, be restricted to 1 or 2. For certain restricted types of kernel functions $F(\vec{k},\omega)$, Cagniard's method provides a sequence of mathematical manipulations which allows one to exactly transform the above to an expression of the form

$$\psi(\overset{\rightarrow}{\mathbf{x}},t) = \int_{-\infty}^{\infty} f(\tau)I(t-\tau,\overset{\rightarrow}{\mathbf{x}}) d\tau \qquad (5.1.2)$$

where $I(t-\tau,x)$ is a relatively simple (compared to (5.1.1)) expression to evaluate. In some cases it may be single closed expression, or it may involve one or two integrations with finite limits. This is a substantial achievement as integrals such as (5.1.1) generally defy direct numerical integration because of the infinite limits and the fact that the integrands are highly oscillatory.

Integrals of the form of Eq. (5.1.1) arise often in studies of wave propagation in stratified media — particularly for waves generated by sources which are point and line sources. Thus one may wonder as to just what types of stratification does the method apply. As best we can tell, from an examination of cases for which the method has been applied previously, the principal restriction on $F(k,\omega)$ is that it must be expressible as a sum of one or more terms of the form

$$F(\vec{k},\omega) \approx \hat{f}(\omega)e^{i\omega T}D(\vec{k},\omega)$$
 (5.1.3)

where $\hat{f}(\omega)$ is a function of ω , and where T and D are functions of \hat{k} and ω which may each be considered (subject to some mathematical fine points) as a function of \hat{k}/ω . The identification described above can be made, in particular, for a point source in a layered stratified medium, where each discrete layer is such that, were it extended to infinite thickness, propagation of any plane wave pulse in the layer would be nondispersive. This type of identification would seem evident from various mathematical formulas given in Brekhovskikh's treatise (1960) on waves in stratified media.

5.2 THE APPROXIMATION OF NEGLECT OF VERTICAL ACCELERATION

It is apparent that Cagniard's method cannot be applied to the propagation of acoustic-gravity waves per sé since these waves are inherently dispersive. The counterpart of a homogeneous medium for such waves is an isothermal atmosphere and it was demonstrated by Hines (1960) that plane waves in such a medium are dispersed. Thus, Cagniard's method would appear inapplicable to an integral such as that appearing in Eq. (2.3.1).

However, it appears that there is one rather simple approximation under which Eq. (2.3.1) may be put into a form which is amenable to Cagniard's method. This is where one neglects the vertical acceleration term ρ D we in Eq. (2.1.4a). Whether or not neglecting this term is justified is somewhat debatable. However, its neglect leads to such considerable simplification that one feels compelled to explore its consequences.

We were led to the observation described above by a paper written by Row in 1966. Row sought to obtain the transient wave generated by a point source in an unbounded isothermal atmosphere with the neglect of the effects of the ground. The theory developed led to a single integral over angular frequency where the integrand was essentially the Green's function determined by Pierce (1963) and by Dikii (1962) for a harmonic point source. In order to evaluate the integral, Row used the artifice of formally equating $\omega_{\rm B} = (\gamma - 1)^{1/2} {\rm g/c}$ and $\omega_{\rm A} = \gamma {\rm g/(2c)}$, which amounts to taking $\gamma = 2$. On examination of Row's result, we found that it could also be approximately interpreted as arising from the neglect of vertical acceleration. It was natural then to ask if this idea could not also be used in other situations where the atmosphere was not isothermal. Pursuing this point led to the discovery that Cagniard's method applied when the vertical acceleration is neglected.

While the approximation may seem somewhat drastic, there are several factors involved which suggest that the physical significance of the results may not be entirely negated and that its inherent inadequacies may be offset by the fact that it leads to a theory which does not necessitate using some of the approximations pecular to the multi-mode theory described in Chapter II (such as neglect of branch line integrals, neglect of leaky modes, and the truncation of integrals over ω).

In the first instance, the approximation of neglecting vertical acceleration would seem to be most appropriate at lower frequencies. Since the first major cycle in empirical waveforms normally has a period in the range of 5 minutes, it would seem that some low-frequency approximation might be applicable in the calculation of the earliest portion of the wavetrain.

While the approximation does lead (as is demonstrated in subsequent sections) to an instantaneous propagation in the vertical direction (which is clearly wrong), we might consider this shortcoming to be not too serious since we are concerned with propagation to large horizontal distances. Furthermore, what calculations we have performed for the theory outlined in Chapter II suggest that the vertical acceleration near the ground at large distances are very small compared to the longitudinal accelerations for the earliest part of the wave. One clear cut advantage of the method is that it leads to a calculable solution which is clearly causal -- which is not true for the theory embodied in the computer program INFRASONIC WAVEFORMS. This would also suggest that we might do better for the earliest part of the waveform with the Cagniard's method theory. Of course, the final test of this would be in the comparison of results with experiment.

5.3 FORMAL DESCRIPTION OF CAGNIARD'S METHOD FOR ACOUSTIC-GRAVITY WAVES

We consider the same problem as posed in Sec. 2.1. The only distinction is that we replace Eq. (2.1.4a) by the two equations

$$\rho_{O}[D_{\mu}\vec{u}_{\mu} + (\vec{u}.\nabla)\vec{v}] = -\nabla_{\mu}P \qquad (5.3.1a)$$

$$dp/dz = -g\rho (5.3.1b)$$

corresponding to the approximation discussed in the preceeding section. Then, the solution of (5.3.1), (2.1.4b), and (2.1.4c) is of the form, for acoustic pressure p,

$$p = \int_{-\infty}^{\infty} f_E(\tau)G(t - \tau, x, y, z, z_0)d\tau$$
 (5.3.2)

where the Green's function G represents the response to a point impulsive source $(x_0 = 0, y_0 = 0)$.

The Fourier integral expression for G is essentially the same as Eq. (2.3.1), one distinction being that $f_E(\omega)$ is replaced by $1/2\pi$.

Thus we have

$$G(t,x,y,z,z_0) = \frac{1}{2\pi} \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} e^{i\vec{k}\cdot\vec{x}} \left\{ \int_{-\infty+i\varepsilon}^{\infty+i\varepsilon} \hat{G}(\omega,\vec{k},z,z_0) e^{-i\omega t} d\omega \right\} dk_x dk_y \quad (5.3.3)$$

where

$$\hat{G} = \left[\frac{\rho_o(z)}{\rho_o(z_o)}\right]^{\frac{3}{2}} \frac{1}{\pi[\omega - \vec{k}.\vec{v}(z_o)]} \left\{\frac{\Psi(z,z_o)}{Z_{\ell}(0)Y_{u}(0)}\right\}$$
(5.3.4)

with

$$\Psi(z,z_0) = [Z_u(z_0) - gY_u(z_0)]Z_{\ell}(z)$$
 $z_0 > z$ (5.3.5a)

=
$$[2_{\ell}(z_0) - gY_{\ell}(z_0)]Z_{\ell}(z)$$
 $z_0 < z$ (5.3.5b)

$$Y = \Phi_1/c$$
 (5.3.6a)

$$Z = g\Phi_1/c - c\Phi_2$$
 (5.3.6b)

Subscripts ℓ and ℓ have been omitted from the last two equations for brevity. The above are essentially the same as Eqs. (2.3.12), (2.3.13), and (2.6.1). The only formal appearance of the effect of the neglect of

vertical acceleration is in the ordinary differential equations (residual equations) satisfied by Φ_1 and Φ_2 . These are

$$\frac{d}{dz} \begin{bmatrix} \phi_1 \\ \phi_2 \end{bmatrix} = \begin{bmatrix} A_{11} & A_{12} \\ A_{21} & A_{22} \end{bmatrix} \begin{bmatrix} \phi_1 \\ \phi_2 \end{bmatrix}$$
 (5.3.7)

where

$$A_{11} = gk^2/\Omega^2 - \gamma g/2c^2$$
 (5.3.8a)

$$A_{12} = 1 - c^2 k^2 / \Omega^2$$
 (5.3.8b)

$$A_{21} = g^2 k^2 / \Omega^2 c^2$$
 (5.3.8c)

$$A_{22} = -A_{11}$$

Note that these are the same as Eqs. (2.6.3) except that A_{21} does not have the term $-\Omega^2/c^2$ present in Eq. (2.6.3c). The quantities (Φ_{10},Φ_{20}) and (Φ_{1u},Φ_{2u}) are particular solutions of the above residual equations — only that the first satisfy the upper boundary condition $(\Phi_{10}=0$ at Z = 0) while the second set satisfies the upper boundary $(\Phi_{11}=0)$ and $(\Phi_{21}=0)$ analytic and bounded for $(\Phi_{21}=0)$ analytic and bounded for $(\Phi_{21}=0)$ analytic and $(\Phi_{21}=0)$ are particular solutions of the above residual equations — only that the first satisfy the upper boundary $(\Phi_{21}=0)$ analytic and bounded for $(\Phi_{21}=0)$ analytic and bounded for $(\Phi_{21}=0)$ and $(\Phi_{21}=0)$ analytic and $(\Phi_{21}=0)$ and $(\Phi_{21}=0)$ analytic and $(\Phi_{21}=0)$ analytic a

The analysis preceding Eqs. (2.4.2) and (2.4.3) shows that we may select $G(\omega,k)$ to be such that

$$\hat{G}(\omega,\vec{k}) * = \hat{G}(-\omega^*, -\vec{k}^*)$$
 (5.3.9a)

$$\hat{G}(\omega, \vec{k}) = -\hat{G}(-\omega, -\vec{k}) \tag{5.3.9b}$$

A third symmetry property follows from the fact that the new set of coefficients depend on ω and k only through the combination k^2/Ω^2 , or alternately, only through the combination k/ω . If we examine the consequences of this we find that we may take

$$\hat{G} = \frac{1}{\left[\omega - \vec{k} \cdot \vec{v}(z_0)\right]} D(\omega, \vec{k})$$
 (5.3.10)

where

$$D(\omega^*, \vec{k}^*) = D(\omega, \vec{k})^*$$
 (5.3.11a)

$$D(-\omega,-k) = D(\omega,\vec{k}) \tag{5.3.11b}$$

$$D(\alpha \omega, \alpha \vec{k}) = D(\omega, \vec{k})$$
 (5.3.11c)

for any real α .

Other relevant properties of D are that it is finite or else zero as $\omega \to \infty$ for all real k. None of its branch lines in the ω plane (when k is fixed and real) extend to infinity. One may show that the only branch points are those associated with the upper half-space and are located for real k at $\omega = \omega_1$ and $\omega = \omega_2$ where

$$\omega_{1,2} = \vec{k} \cdot \vec{v} + 2c_{\infty} [(\gamma-1)^{\frac{1}{2}}/\gamma] |\vec{k}|$$
 (5.3.12)

Thus, there are only two branch points -- both on the real axis. The branch line is taken as extending directly along the real axis between the two points.

The poles of D in the ω plane for real k may be denoted by $\omega_n(k)$. Near any such pole,

$$D \approx \frac{D_n(\vec{k})}{\omega - \omega_n(\vec{k})}$$
 (5.3.13)

where D (\vec{k}) is the residue. The quantity $\omega_n(\vec{k})$ should be of the form

$$\omega_{n}(\vec{k}) = |\vec{k}| v_{n}(\theta_{k})$$
 (5.3.14)

where θ_k is the direction of k. This follows from Eq. (5.3.11c). Also, Eq. (5.3.11b) would imply that

$$v_n(\theta_k + \pi) = -v_n(\theta_k)$$
 (5.3.15)

The Eq. (5.3.11a) would imply that \mathbf{v}_n is entirely real. Finally, we can show that \mathbf{D}_n is real, and that it is of the form

$$D_n = |\vec{k}| A_n(\theta_k) \tag{5.3.16}$$

where

$$A_n(\theta_k) = A_n(\theta_k) * \tag{5.3.17}$$

$$A_n(\theta_k + \pi) = -A_n(\theta_k)$$
 (5.3.18)

If D is D on the real axis just above the branch line and D is D on the real axis just below the branch line, we may show (k real) that

$$D_{a}(\omega, \vec{k}) = D_{b}*(\omega, \vec{k})$$

If we use polar coordinates for k, then

$$D_{\mathbf{a}}(-\omega, \mathbf{k}, \theta_{\mathbf{k}}) = D_{\mathbf{a}}(\omega, \mathbf{k}, \theta_{\mathbf{k}} + \pi)$$

follows from Eq. (5.3.11b)

With these preliminaries, we may now describe Cagniard's method (or at least the authors' version of the method) as it applies to the problem. For t < 0, G vanishes. For t > 0 we deform the integration contour to enclose the entire lower halfspace in the clockwise sense. This contour is then shrunk to enclose all poles and the branch line (Fig. 5-1) and the residue theorem is utilized to pick up the contribution from the poles. This gives us

$$G = \left[\frac{\rho_{o}(z)}{\rho_{o}(z_{o})}\right]^{\frac{1}{2}} \frac{1}{\pi} \left[I_{BL} + \sum_{n} I_{n}\right]$$
 (5.3.19)

where the branch line contribution is given by

$$I_{BL} = \int_{0}^{\infty} k \, dk \int_{0}^{2\pi} d\theta_{k} \, e^{i\vec{k} \cdot \vec{x}} \int_{\omega_{1}}^{\omega_{2}} e^{-i\omega t} \left\{ \frac{i(D_{a} - D_{a}^{*})}{\omega - \vec{k} \cdot \vec{v}(z_{0})} \right\} d\omega \quad (5.3.20)$$

and a particular pole contribution is given by

$$I_{n} = 2\pi \int_{0}^{\infty} k \, dk \int_{0}^{2\pi} d\theta_{k} \, e^{i\vec{k} \cdot \vec{x}} \left\{ \frac{kA_{n}e}{kv_{n} - v(z_{0}) \cdot k} \right\}$$
 (5.3.21)

In the above we neglect the pole associated with the zero of $\omega - \vec{k} \cdot \vec{v}(z)$. The integral along the branch line is interpreted as a principal value.

As for the branch line contribution, we let ω = vk and change the ω variable of integration to one over v. Then we perform the k integration first. Doing this gives

$$I_{BL} = \int_{0}^{2\pi} d\theta_{k} \int_{v_{1}}^{v_{2}} dv \left\{ \frac{i(D_{a} - D_{a}^{*})}{v - e_{k}^{*} v(z_{0})} \right\} \int_{0}^{\infty} e^{ik[R \cos(\theta - \theta_{k}) - vt]} k dk \quad (5.3.22)$$

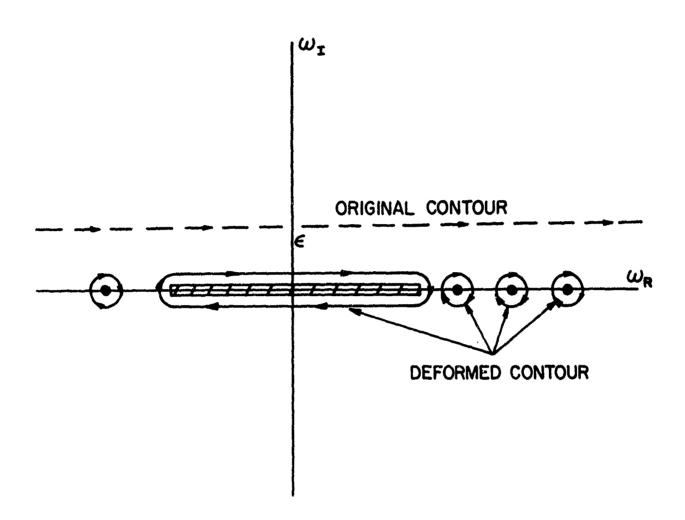


Figure 5-1. Sketch showing contour deformation in the complex $\boldsymbol{\omega}$ plane for positive-times.

where

$$v_{1,2} = e_k^{\dagger} \cdot v_{\infty}^{\dagger} + 2c_{\infty}[(\gamma - 1)^{\frac{1}{2}}/\gamma]$$
 (5.3.23a)

$$\stackrel{+}{e_k} = (\cos \theta_k) \stackrel{+}{e_x} + (\sin \theta_k) \stackrel{+}{e_y}$$
 (5.3.23b)

It should be noted that $\mathbf{v_1}$ and $\mathbf{v_2}$ are functions of θ_k . Also, D is a function of \mathbf{v} and θ_k .

The pole contributions may similarly be expressed as

$$I_{n} = 2\pi \int_{0}^{2\pi} d\theta_{k} \frac{A_{n}}{\left[v_{n} - v(z_{0}) \cdot \dot{e}_{k}\right]} \int_{0}^{\infty} e^{ik\left[R \cos(\theta - \theta_{k}) - v_{n}t\right]} k dk \quad (5.3.24)$$

Here R is the net horizontal distance from the source.

Next, we may show, using various properties described above, that the contribution to the integrand in either (5.3.22) or (5.3.24) from θ_k + π is just the complex conjugate of that from θ_k . Thus we set

$$I_{BL} = 2 \text{ Re} \int_{\theta-\pi/2}^{\theta+\pi/2} d\theta_{k} \int_{v_{1}}^{v_{2}} dv \left\{ \frac{i(D_{a} - D_{a}^{*})}{v - e_{k}^{*} v(z_{0})} \right\} \int_{0}^{\infty} e^{ik[R \cos(\theta-\theta_{k}) - vt]} k dk$$
(5.3.25)

$$I_{n} = 4\pi Re \int_{\theta-\pi/2}^{\theta+\pi/2} d\theta_{k} \frac{A_{n}}{\left[v_{n} - v(z_{o}) \cdot e_{k}\right]} \int_{0}^{\infty} e^{ik\left[R \cos(\theta-\theta_{k}) - v_{n}t\right]} k dk$$

At this point we introduce some minor approximations which would not be approximations at all were there no winds. We formally replace

in Eq. (5.3.25). The justification for this is that $(D_n - D_n^*)/v$ is even in the absence of winds. Also, for the pole contribution, the terms I_n can be paired (I_n, I_n) in the absence of winds where $v_n = v_n$. The residues A_n would have the property that $A_n = A_n$ and thus we might interpret the quantity A_n/v_n as being even in n, and consequently we might let

$$\sum_{n}^{-ikv} (A_n/v_n) e^{-ikv_n t} + \sum_{n \ge 0} 2(A_n/v_n) \cos kv_n t$$

These ideas lead to the expressions

$$I_{BL} = 2 \text{ Re} \int_{\theta-\pi/2}^{\theta+\pi/2} d\theta_k \int_{v_1}^{v_2} dv \frac{i(D_a - D_a^*)}{v - e_k^* \cdot v(z_0^*)} \int_0^{\infty} e^{ikR \cos(\theta - \theta_k^*)} \cos(kvt) k dk$$

$$I_{n} + I_{-n} = 8\pi \text{ Re } \int_{\theta-\pi/2}^{\theta+\pi/2} d\theta_{k} \frac{A_{n}}{[v_{n} - \dot{v}(z_{0}) \cdot \dot{e}_{k}]} \int_{0}^{\infty} e^{ikR \cos(\theta-\theta_{k})} \cos(kv_{n}t) k dk$$

Another approximation we introduce in the same spirit is to set $\theta_k = \theta$ in the argument of v_1 , v_2 , D_a , e_k , v_n , and A_n . This is justified in the absence of winds and would seem to be appropriate with winds included since the integrand contribution is heaviest near $\theta_k = \theta$. With this approximation we have

$$I_{BL} = \int_{v_1}^{v_2} dv \left[\frac{i(D_a - D_a^*)}{v - e_k \cdot v(z_o)} \right]_{\theta_k = \theta} M(R,vt)$$

$$I_n + I_{-n} = 4\pi \left[\frac{A_n}{[v_n - v(z_o) \cdot e_k]} \right]_{\theta_k} = \theta M(R, v_n t)$$

where

$$M(R,vt) = 2 Re \int_{0}^{\pi} \int_{0}^{\infty} e^{ikR \sin \theta} \cos (kvt) k dk d\theta$$

$$= v^{-1} (d/dt) \left\{ 2 Re \int_{0}^{\pi} \int_{0}^{\infty} e^{ikR \sin \theta} \sin (kvt) dk d\theta \right\} (5.3.26)$$

The indicated integral can be shown to be

2 Re
$$\int_{0}^{\pi} \int_{0}^{\infty} e^{ikR \sin \theta} \sin(kvt) dk d\theta = \frac{2\pi U(vt - R)}{[(vt)^{2} - R^{2}]^{\frac{1}{2}}}$$
 (5.3.27)

where U is the Heaviside step function.

Finally, we combine the results above and obtain

$$p = p_{BL} + \sum_{n \ge 0} p_n$$
 (5.3.28)

where

$$p_{BL} = -2 \left[\frac{\rho_{o}(z)}{\rho_{o}(z_{o})} \right]^{\frac{1}{2}} \int_{v_{1}}^{v_{2}} \frac{1}{|v|} \left\{ \frac{i(D_{a} - D_{a}^{*})}{v - e_{k}^{*} v(z_{o}^{*})} \right\}_{\theta} \left\{ \int_{-\infty}^{t - R/|v|} \frac{f'_{E}(\tau) d\tau}{[v^{2}(t - \tau)^{2} - R^{2}]^{\frac{1}{2}}} \right\} dv$$
(5.3.29a)

$$p_{n} = -8\pi \left[\frac{\rho_{o}(z)}{\rho_{o}(z_{o})} \right]^{\frac{1}{2}} \frac{1}{v_{n}} \left\{ \frac{A_{n}}{v_{n} - v(z_{o}) \cdot e_{k}^{+}} \right\}_{\theta} \int_{-\infty}^{t-R/v_{n}} \frac{f'_{E}(\tau) d\tau}{\left[v_{n}^{2}(t-\tau)^{2} - R^{2}\right]^{\frac{1}{2}}}$$
(5.3.29b)

In the above expression, v_n is considered as being positive and the sum over n is over only those "modes" having positive phase velocities.

The physical interpretation of the above solution is that the total waveform is the sum of a "lateral wave" (the branch line integral) plus a sum of guided mode waveforms. Each guided mode is nondispersive and has a speed \mathbf{v}_n . The shapes of various guided mode waveforms are similar.

The relative simplicity of the results must be emphasized. The τ integration is over finite limits and should be easily performed on a digital computer. The only lengthy problem would be that of finding the v_n and A_n for the guided modes. However, this could be done with only a slight modification to the existing program INFRASONIC WAVEFORMS. The lateral wave might be more difficult to evaluate (since it involves two integrations) but we would expect its contribution to be small for most cases of interest. We should also point out that there is no apparent restriction on the atmospheric profiles for which the above theory might be applied.

5.4 THE ISOTHERMAL ATMOSPHERE AS AN EXAMPLE OF THIS METHOD

The only example which we have explored in any depth using the method of the previous section is that where the ambient atmosphere is isothermal. In this event the function D appearing in Eq. (5.3.10) is given by

$$i\mu |z-z_0| i\mu |z+z_0|$$

 $D = -i\{Me + Ne\}$ (5.4.1)

$$M = \frac{g}{2\mu} \left\{ \frac{\omega_A}{c} \pm i\mu \right\}$$
 (5.4.2a)

$$N = \frac{g}{2\mu} \frac{\left[i\mu - c^{-1} \left(\omega_A^2 - \omega_B^2\right)^{\frac{1}{2}}\right]}{\left[-i\mu - c^{-1} \left(\omega_A^2 - \omega_B^2\right)^{\frac{1}{2}}\right]} \left[i\mu + \omega_A/c\right]$$
 (5.4.2b)

$$\mu = \left[\frac{\omega_{\rm B}^2 k^2}{\omega^2} - \frac{\omega_{\rm A}^2}{c^2} \right]^{\frac{1}{2}}$$
 (5.4.2c)

The plus sign in (5.4.2a) corresponds to z>z, while the minus sign corresponds to z>z. The quantity μ has a branch line between $-(\omega_B/\omega_A)c|k|$ and $(\omega_B/\omega_A)c|k|$. Its phase is between 0 and π in the upper half of the ω plane.

The only poles are at $\omega=\pm c|k|$ and lie on the real axis to the left and right of the branch line. The residue at the positive pole is $|k|A_1$ where

$$A_1 = g(1 - \gamma/2)e (g/c^2) |z + z_0|$$
(5.4.3)

Thus, from Eqs. (5.3.28) and (5.3.29), we have

$$p = p_{BL} + p_1 ag{5.4.4}$$

where

$$P_{b.} = -4 \left[\frac{\rho_{o}(z)}{\rho_{o}(z_{o})} \right]^{\frac{1}{2}} \int_{0}^{(\omega_{B}/\omega_{A})c} Q \left\{ \int_{-\infty}^{t-R/v} \frac{f'_{E}(\tau) d\tau}{\left[v^{2}(t-\tau)^{2}-R^{2}\right]^{\frac{1}{2}}} \right\} dv \quad (5.4.5a)$$

$$p_{1} = -8\pi \left| \frac{\rho_{0}(z)}{\rho_{0}(z_{0})} \right|^{\frac{1}{2}} (g/c) (1 - \gamma/2)e^{-(1 - \gamma/2) (g/c^{2})|z + z_{0}|}$$

$$x \int_{-\infty}^{t-R/c} \frac{f'_{E}(\tau) d\tau}{\left[c^{2}(t-\tau)^{2}-R^{2}\right]^{\frac{1}{2}}}$$
 (5.4.5b)

Here

$$Q = (2/v^2) \operatorname{Re} \left\{ \overline{\operatorname{Me}}^{-iK^{1}} - z_0 \Big| + \overline{\operatorname{Ne}}^{-iK|z + z_0|} \right\}$$
 (5.4.6)

$$\overline{M} = -\frac{g}{2K} \{ (\gamma/2)(g/c^2) \otimes iK \}$$
 (5.4.7a)

$$\overline{N} = -(g/2K) \left\{ \frac{-iK - (1 - \gamma/2)g/c^2}{iK - (1 - \gamma/2)g/c^2} \right\} [-iK + (\gamma/2)g/c^2]$$
 (5.4.7b)

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$$K = g[(\gamma - 1)/v^2 - (\gamma/2)/c^2]^{\frac{1}{2}}/c$$
 (5.4.7c)

In the event the presence of the ground is neglected, there is no guided wave p_1 and the term with \bar{N} does not appear in (5.4.6).

We have carried out a modest amount of calculations using the above formulas, taking $f_E(t)$ to be a delta function. The quantity p_1 then, for t > R/c, has a t and R dependence given by

$$p_1 \approx \frac{ct}{[c^2t^2 - R^2]^{3/2}}$$
 (5.4.8)

and thus falls off as $1/t^2$ at large t. The direct wave is oscillatory in general. The nature of the oscillation can be described if we let v = R/t and examine the factor $\exp[-iK|z - z_0|]$. Thus

$$p_{BL} \approx \{amplitude\} \cos \{g|z-z_0|[(\gamma-1)t^2/R^2-(\gamma/2)c^{-2}]^{\frac{1}{2}} + phase factor\}$$
(5.4.9)

The angular frequency as a function of time is then

$$\omega \approx \frac{g|z - z_0| (\gamma - 1)t/R^2}{c[(\gamma - 1)t^2/R^2 - (\gamma/2)c^{-2}]^{\frac{1}{2}}}$$
 (5.4.10)

which is large at early times and which asymptotically (large t and fixed R) approaches

$$\omega \approx \frac{\mathbf{g}}{c} \frac{|z-z_0|}{R} (\gamma - 1)^{\frac{1}{2}}$$
 (5.4.11)

which is essentially the same as Row's ω . The difference is that the R above is horizontal distance rather than total slant path distance. As long as $|z-z_0|/R << 1$, our result agrees with Row's.

Chapter VI

THE SINGLE MODE THEORY

6.1 INTRODUCTION

The calculations presented in Chapter IV and by previous authors (Scorer, Pekeris, harkrider, etc.) suggest that the earliest portion of the waveform (say, the first three cycles) received at large distances may be considered as associated with a single composite mode. This point of view has, in particular, been espoused with considerable eloquence by Garrett and by Bretherton in some very recent papers on the subject. We find this point of view to be appealing by virtue of the fact that it may lead to a satisfactory method for taking into account some effects which are neglected in the formulation of the multi-mode theory presented in Chapter II. Such effects would include far field nonlinear effects, departures of the atmosphere from perfect stratification, attenuation by viscosity and thermal conduction, and large scale irregularities in the earth's terrain.

Another virtue of a single-mode theory would be its inherent simplicity. The computational procedure represented by INFRA-SONIC WAVEFORMS, regardless of how good one regards the theory on which it is based, is sufficiently complicated that its consequences can only be explored by numerical experiment. large number of possible parameters which must be specified in order to construct a single waveform make it very difficult to draw any succinct simple cause and effect relationships between any one of these parameters (for example, yield) and particular features of the waveform. This would probably be a minor handicap from a practical standpoint, given the existence of the computer program, if we possessed a reasonable knowledge of the atmosphere's state at the time the explosion took place. In practice, however, this is not the case, as the atmosphere is always imperfectly known at any given time. The usual experimental situation is where a number of waveforms are recorded at various points and where a limited knowledge of the explosion and of the atmosphere is possessed. The typical analysis problem would be to use this data and whatever else is known to determine a refined description of the atmosphere and/or the explosion. Borrowing a term from exploration geophysics, this might be designated the inverse problem of infrasonic wave propagation. In principle, given an adequate theory and a numerical procedure for synthesizing waveforms, we can

solve this inverse problem (or at least find a possible range of solutions and a most probable solution) by trial and error in repetitive calculations with systematic variation of input parameters. Obviously, this could be a very expensive and time-consuming process. Thus, a strong case can be made for an attempt to find a simple model where the number of input parameters is greatly reduced.

Insofar as the theory embodied in INFRASONIC WAVEFORMS is concerned, the possibility of using it to solve the inverse problem is severely limited by the fact that it is restricted to perfectly stratified atmospheres. The data showing amplitude variations with observer location exhibited by Wexler and hass following the largest Soviet explosion strongly suggest that departures from stratification are of considerable significance. On the other hand, the present theory is already so complicated that it appears prohibitively difficult to extend it to include departures from stratification. A possibility would be a tradeoff - altering the theory to take the non-stratification into account at the expense of the accuracy which might be expected were the atmosphere perfectly stratified. In this respect, the single mode theory might represent a very convenient compromise.

6.2 LAMB'S MODE

In 1910, Horace Lamb demonstrated that a single guided mode exists for the isothermal atmosphere with no winds. In retrospect, the existence of this mode is very curious as the normal criterion for ducting in conventional (gravity neglected) acoustics would seemingly preclude its existence.

The formulas for Lamb's mode are trivially extended to include constant horizontal wind. For convenience of reference, we summarize the result here. The acoustic pressure p, density ρ , horizontal fluid velocity deviation u, and vertical fluid velocity w are given by

$$p = e^{-gz/c^2} F(x_n, t)$$
 (6.2.1a)

$$\rho = c^{-2}e^{-gz/c^2} F(\vec{x}_H, t)$$
 (6.2.1b)

$$\vec{u} = e^{-gz/c^2} \vec{v}(\vec{x}_H, t)/\rho_0(z)$$
 (6.2.1c)

$$\mathbf{w} = 0 \tag{6.2.1d}$$

where F and U satisfy

$$[\partial/\partial t + \overrightarrow{v} \cdot \nabla_{\underline{i}}] \overrightarrow{U} = -\nabla_{\underline{i}} F$$
 (6.2.2a)

$$[\partial/\partial t + \overset{+}{v} \circ \nabla_{H}]F + c^{2}\nabla_{H} \circ \overset{+}{U} = 0$$
 (6.2.2b)

or

$$[\partial/\partial t + \dot{\nabla} \nabla_{H}]^{2}F - c^{2}\nabla_{H}^{2}F = 0$$
 (6.2.3)

which is the two dimensional wave equation for nondispersive propagation. In the above, x_H is horizontal displacement and Y_H is the horizontal component of the gradient. Note that c and v (horizontal wind) are considered constant in the above.

The plane wave solution of (6.2.3) is

$$F = F_0 e^{-i[\omega t - \overrightarrow{k} \cdot \overrightarrow{x}]}$$

where ω and \overrightarrow{k} satisfy the dispersion relation

$$(\omega - \vec{k} \vec{v})^2 = c^2 k^2$$

Since this gives \vec{k}/ω as being independent of frequency, the propagation is nondispersive.

The relative simplicity of Eqs. (6.2.2) and (6.2.3) must be emphasized. Although the disturbance is in a three dimensional space, these equations only involve two spatial coordinates. Furthermore, the coefficients in these equations are constant — a substantial simplification for propagation in an inhomogeneous medium.

It would appear that, if a single-mode theory of infrasonic propagation were to be developed, the mode selected should be that which, for more realistic atmospheres, is the counterpart of Lamb's mode for an isothermal atmosphere. This follows since the principal disturbance contributing to the waveform observed at ground level is one which moves very nearly with the ground speed, which is only slightly dispersive, and which has very little vertical movement (as contrasted with horizontal movement) associated with it. Carrett and Bretherton have succeeded in finding this mode for a stratified atmosphere which is nearly isothermal and which has nearly constant winds. We give a modified derivation (with slightly different results) below:

The residual equations, (2.3.8), for disturbances of given \vec{k} and ω may be rewritten in the form

$$\frac{\mathrm{d}}{\mathrm{d}z} (Z\phi) = \phi S_{12} Y \tag{6.2.4a}$$

$$\frac{d}{dz} (Y\phi^{-1}) = \phi^{-1}S_{21}Z \qquad (6.2.4b)$$

where ϕ may be taken as

$$\phi = p_0^{-1/\gamma}(z)\rho_0^{1/2}(z) \tag{6.2.5}$$

Since Y = 0 at the ground altitude z_0 , we may place these in the form of coupled integral equations as

$$z = \phi^{-1}[F + \int_{z_g}^{z} \phi S_{12}Y dz]$$
 (6.2.6a)

$$Y = \phi \int_{z_{g}}^{z} \phi^{-1} S_{21}^{2} Z dz$$
 (6.2.6b)

where F is independent of z. To the above we add, as a restriction on ω and k, the guided condition that $Y\phi^{-1} \to 0$ as $z \to \infty$, i.e.

$$\int_{z_{g}}^{\infty} \phi^{-i} S_{11}^{2} dz = 0$$
 (6.2.7)

By successive iteration starting with Y = 0 in Eq. (6.2.6a) we find that these have the formal solution

$$Z = \phi^{-1}[1 + L_{12}L_{21} + L_{12}L_{21}L_{12}L_{21} + L_{12}L_{21}L_{12}L$$

$$Y = \phi[L_{21} + L_{21}L_{12}L_{21} + L_{21}L_{12}L_{21}L_{12}L_{21} + \dots]F$$
 (6.2.8b)

$$[L_{21} + L_{21}L_{12}L_{21} + L_{21}L_{12}L_{21}L_{12}L_{21} + ...]_{z=\infty} = 0$$
 (6.2.8c)

where \mathbf{L}_{12} and \mathbf{L}_{21} are operators, defined such that for any function

Q(z) appearing to their right

$$L_{12}Q = \int_{z_g}^{z} \phi^2 S_{12}Q dz$$
 (6.2.9a)

$$L_{21}^{Q} = \int_{z_{g}}^{z} \phi^{-2} S_{21}^{Q} dz \qquad (6.2.9b)$$

The subscript $(z=\infty)$ in Eq. (6.2.8c) implies that the upper limit of the last integration is ∞ .

The lowest order approximation to the dispersion relation would be $[L_{12}]_{\infty} = 0$ or

$$\int_{z_{g}}^{\infty} \phi^{-2}[(k^{2}/\Omega^{2}) - c^{-2}] dz = 0$$
 (6.2.10)

To further approximate this, we expand

$$\frac{\mathbf{k}^2}{\Omega^2} = \frac{\mathbf{k}^2}{(\omega - \mathbf{k}^* \mathbf{v})^2} \approx \frac{\mathbf{k}^2}{\Omega_{\mathrm{L}}^2} \left[1 + 2\mathbf{k}^* (\mathbf{v} - \mathbf{v}_{\mathrm{L}})/\Omega_{\mathrm{L}} \right]$$
 (6.2.11)

where

$$\Omega_{L} = \omega - \vec{k} \cdot \vec{v}_{L}$$

and where \overrightarrow{v}_L is any representative wind speed. We consider \overrightarrow{v}_L independent of z. Since we have some latitude in the definition of \overrightarrow{v}_L , we define \overrightarrow{v}_L such that

$$\int_{z_g}^{\infty} \phi^{-2} (\overrightarrow{v} - \overrightarrow{v}_L) dz = 0$$

or

$$\dot{\vec{v}}_{L} = \frac{\int_{\phi^{-2} \dot{V} dz}^{\phi^{-2} dz}}{\int_{\phi^{-2} dz}^{\phi^{-2} dz}}$$
(6.2.12)

Then, substituting (6.2.11) into (6.2.10), we find

$$k^2/\Omega_L^2 = 1/c_L^2$$
 (6.2.13)

where

$$\frac{1}{c_{\rm L}^2} = \frac{\int_{\phi^{-2} c^{-2} dz}^{\phi^{-2} dz}}{\int_{\phi^{-2} dz}^{\phi^{-2} dz}}$$
(6.2.14)

In what follows we refer to $\overset{\rightarrow}{\mathbf{v}_{L}}$ as the <u>average wind velocity</u> and to c_{L} as the <u>average sound speed</u> for the <u>Lamb mode</u>.

One should note that Eq. (6.2.13) is exactly the same dispersion relation as was obtained for Lamb's mode in an isothermal atmosphere with constant winds.

From Eqs. (6.2.8a,b), keeping just the first order terms in $c^2-c_L^2$ and $v-v_L$ and using (6.2.13), we find

$$Z = \phi^{-1} [1 + (\Omega_L^2 - \omega_{BL}^2) (A + \vec{B} \cdot \vec{k} / \Omega_L)] F$$
 (6.2.15a)

$$Y = \varphi[C + \vec{D} \cdot \vec{k}/\Omega_L]F \qquad (6.2.15b)$$

where A, \overrightarrow{B} , C, \overrightarrow{D} are functions of z, given by

$$A = \int_{z}^{z} \phi^{2} C dz \qquad (6.2.16a)$$

$$\vec{B} = \int_{\mathbf{z}}^{\mathbf{z}} \phi^2 \vec{D} \, d\mathbf{z}$$
 (6.2.16b)

$$C = \int_{z_{g}}^{z} \phi^{-2} (c_{L}^{-2} - c^{-2}) dz$$
 (6.2.16c)

$$\vec{D} = (2/c_L^2) \int_{z_g}^{z} \phi^{-2} (\vec{v} - \vec{v}_L) dz$$
 (6.2.16d)

We have also defined the average Brunt's frequency $\omega_{BL}^{}$ for the Lamb mode by the relation

$$\omega_{\rm BL}^2 = (\gamma - 1)g^2/c_{\rm L}^2 \tag{6.2.17}$$

If we examine the next highest order correction (which is second order in $c^2-c_L^2$ and $v-v_L$) to the dispersion relation (6.2.8c), we find, after some algebra and the use of the definitions of v_L and c_L , that

$$[k^{2}/\Omega_{L}^{2} - c_{L}^{-2}] \int_{z_{g}}^{\infty} \phi^{-2} dz + (3c_{L}^{-2}\Omega_{L}^{-2}) \int_{z_{g}}^{\infty} \phi^{-2} [k \cdot (v - v_{L})]^{2} dz$$

$$- (\Omega_{L}^{2} - \omega_{BL}^{2}) \int_{z_{g}}^{\infty} \varphi^{2} [C + \vec{D} \cdot \vec{k} / \Omega_{L}]^{2} dz = 0$$
 (6.2.18)

This is essentially the same as the dispersion relation derived by Garrett. It should be noted that the presence of the last term makes the mode dispersive. The integral should be convergent since $C(\infty)$ and $\widetilde{D}(\infty)$ are both zero.

To the same order of approximation, we may write the dispersion relation for a wave traveling with wave normal in the direction of \hat{k} in the form

$$\omega = k(c_L + v_{Lk} + a_{kk}) - k(k^2 - k_{BL}^2)h_{kk}$$
 (6.2.19)

$$v_{l,k} = \overset{\rightarrow}{v_l} \overset{\rightarrow}{e_k} \tag{6.2.20a}$$

$$a_{kk} = [3/(2c_L)] \frac{\int_{0}^{\infty} [v - v_L) \cdot e_k^{\dagger} [2\phi^{-2}] dz}{\int_{0}^{\infty} dz}$$
 (6.2.20b)

$$k_{\rm BL}^2 = \omega_{\rm BL}^2/c_{\rm L}^2$$
 (6.2.20c)

$$h_{kk} = (1/2)c_L \frac{\int \phi^2 [C + \vec{D} \cdot \vec{e}_k/c_L]^2 dz}{\int \phi^{-2} dz}$$
 (6.2.20d)

Here $\overset{\rightarrow}{e_k}$ is the unit vector in the direction of \vec{k} . One should note that a_{kk}^k and a_{kk}^k may each be considered as the Cartesian components of a tensor.

If we had a hypothetical pulse propagating in the e_k direction, such that all frequency components can be considered as being plane (or line) waves (in the horizontal plane) with the same wave number direction e_k , this pulse could be represented as a Fourier integral in the form

$$\psi(t,s) = 2 \text{ Re} \int_{0}^{\infty} \hat{\psi}(k) e^{-i(\omega t - ks)} dk$$
 (6.2.21)

where $s = \overset{\rightarrow}{e_k} \overset{\rightarrow}{\circ} x$ is distance in the direction of \vec{k} and ω is considered as a function of k. Then, if $\omega(k)$ is given by (6.2.19), it must follow that the wave variable ψ satisfies the equation

$$\partial \psi / \partial t + [c_L + v_{Lk} + a_{kk}] \partial \psi / \partial s + h_{kk} (\partial^2 / \partial s^2 + k_{BL}^2) (\partial \psi / \partial s) = 0$$

$$(6.2.22)$$

which may be recognized as an equation which in many other contexts is generally called the <u>linearized Korteweg-de Vries</u> equation.

6.3 FAR FIELD NONLINEAR EFFECTS

In this section we generalize the linearized Korteweg-de Vries equation governing pulse propagation in the Lamb mode to include accumulative nonlinear effects. We assume at the outset that such effects are weak and that their primary effect is to distort the waveform. In this respect, we consider that the only appreciable nonlinear effect is represented by the fact that \mathbf{c}_{τ} and \mathbf{v}_{τ} should

be the height averaged sound speed and wind velocity, given the fact that the ambient medium is altered by the presence of the wave disturbance. Thus we replace

$$c_L \rightarrow c_L^{NL}$$
 (6.3.1a)

$$v_{Lk} \rightarrow v_{Lk}^{NL}$$
 (6.3.1b)

in the dominant terms (zeroth order in $\vec{v}-\overset{\rightarrow}{v_L}$ and $c^2-c_L^2$) in (6.2.22).

To determine $c_L^{\mbox{\scriptsize NL}}$ we set

$$c^2 \rightarrow \frac{\gamma(p_0 + p)}{(\rho_0 + \rho)} \tag{6.3.2}$$

in Eq. (6.2.14) such that, to the first order,

$$(c_L^{IIL})^{-2} = \frac{1}{c_L^2} + \frac{\int_{\phi}^{-2} \left\{ \frac{1}{c^2} \left[\frac{p}{p_0} - \frac{\rho}{\rho_0} \right] \right\} dz}{\int_{\phi}^{-2} dz}$$

The fact that ϕ also depends on c is not important as it leads to nonlinear terms of first order in $c^2-c_L^2$ which are considered small. To obtain the lowest order nonlinear correction, we may approximate

$$\frac{1}{c^{2}} \left[\frac{p}{p_{0}} - \frac{\rho}{\rho_{0}} \right] = \frac{1}{c^{2}} \frac{(\gamma - 1)}{\gamma} \frac{p}{p_{0}} \approx \frac{1}{c^{2}} \frac{(\gamma - 1)}{\gamma} F \frac{1/\gamma - 1}{\rho_{0}}$$

using Eqs. (2.3.4a), (6.2.5), (6.2.15a) and various relations appropriate to the case when the atmosphere is isothermal. Using some additional approximations, we find

$$c_L^{NL} = c_L \{1 + [(\gamma - 1)/(2\gamma)] \vee p(z_g) / p_o(z_g)\}$$
 (6.3.3)

$$v = \frac{\int_{z_{g}}^{\infty} [p_{o}(z)/p_{o}(z_{g})]^{(3/\gamma - 2)} dz}{\int_{z_{g}}^{\infty} [p_{o}(z)/p_{o}(z_{g})]^{(2/\gamma - 1)} dz}$$
(6.3.4)

In a similar manner, we compute

$$v_{Lk}^{NL} = \frac{\int_{z_g}^{\infty} (\vec{v} + \vec{u}) \cdot \vec{e}_k \phi^{-2} dz}{\int_{z_g}^{\infty} (\vec{v} + \vec{u}) \cdot \vec{e}_k \phi^{-2} dz} \approx v_{Lk} + \frac{\int_{z_g}^{\infty} [p/c\rho_0] \phi^{-2} dz}{\int_{z_g}^{\infty} \phi^{-2} dz}$$

$$\approx v_{Lk} + c_L \gamma^{-1} v[p(z_g)/p_0(z_g)] \qquad (6.3.5)$$

where v is the same as in Eq. (6.3.4).

With Eqs. (6.3.3) and (6.3.5), the modified pulse propagation equation (6.2.22) becomes

$$\frac{\partial \psi}{\partial t} + \left\{ c_{L} + v_{Lk} + a_{kk} + c_{L} [(\gamma + 1)/2\gamma] v[p(z_{g})/p_{o}(z_{g})] \right\} \frac{\partial \psi}{\partial s} + h_{kk} (\frac{\partial^{2}}{\partial s^{2}} + k_{BL}^{2}) (\frac{\partial \psi}{\partial s}) = 0$$
(6.3.6)

This equation will be nonlinear, since p(z) is a function of ψ , regardless of what we choose ψ to represent. [For example, we could take ψ to be p(z).] The above equation is generally referred to as the Korteweg-de Vries equation.

6.4 DISSIPATION EFFECTS

We next consider the modification to Eq. (6.3.6), i.e., the Korteweg-de Vries equation, due to the dissipation caused by viscosity and thermal conduction in the atmosphere. Specifically, we derive an extra term which represents the correction due to the effects of these phenomena. In carrying through the deri-

vation we neglect nonlinear effects - with the assumption that terms which are both nonlinear and which involve viscosity and thermal conduction are of negligible influence on the waveform.

There are essentially two broad types of dissipation which may be considered - bulk dissipation and wall dissipation. The former is the dissipation which occurs when any wave propagates in an unbounded medium, while wall dissipation is that which occurs due to the presence of the ground. The former takes place primarily at high altitudes because of the decrease of ambient density with height, while the latter takes place close to the ground in a thin boundary layer. A priori, we assume that bulk dissipation is the more important and we accordingly neglect wall dissipation. We have not, however, investigated this quantitatively as yet, and we plan to do so in later studies. In what follows we proceed on the assumption of negligible wall dissipation.

The general procedure we adopt is to first write out the equations of hydrodynamics with viscosity and thermal conduction included and then derive the linearized first order equations for acoustic perturbations to an ambient state. This ambient state is taken to be height stratified and time independent as described in Sec. 2-1. The source term is neglected at the outset, since we are here concerned with propagation at distances somewhat removed from the source location.

The modified equations then become

$$\rho_{o}[D_{t}\vec{\mathbf{u}} + \vec{\mathbf{u}} \cdot \nabla \vec{\mathbf{v}}] = -\nabla p - g\rho \vec{\mathbf{e}}_{z} + (\partial \sigma_{ij}^{*}/\partial \mathbf{x}_{i})\vec{\mathbf{e}}_{j}$$
 (6.4.1a)

$$D_{+}\rho + \nabla \cdot (\rho_{0}\overrightarrow{u}) = 0 \qquad (6.4.1b)$$

$$(D_{t}p + \dot{u} \cdot \nabla p_{o}) - c^{2}(D_{t}\rho - \dot{u} \cdot \nabla \rho_{o}) = D_{E}$$
 (6.4.1c)

whore

$$\sigma_{ij}^{\prime} = \eta[\partial u_{i}/\partial x_{j} + \partial u_{j}/\partial x_{i} - (2/3)\delta_{ij}\nabla \cdot \dot{u}] + \zeta\delta_{ij}\nabla \cdot \dot{u}$$
 (6.4.2a)

$$D_{E} = 2\eta(\gamma - 1)(\partial_{\mathbf{v}}^{\dagger}/\partial z) \cdot [\partial_{\mathbf{u}}^{\dagger}/\partial z + \nabla u_{z}] + (\gamma c_{\mathbf{v}})^{-1} \nabla \cdot \{\kappa \nabla [(\gamma p - c^{2}\rho)/\rho_{o}]\}$$
(6.4.2b)

Here η is the dynamic viscosity, ζ is the bulk viscosity, c is the specifie heat per unit mass at constant volume and κ is the thermal conductivity. The above result neglects fluctuations in

 c_{y} , η , ζ , and κ due to the presence of the disturbance. The remaining symbols have the same meaning as used in Chapter 2.

If we next consider a planar disturbance of fixed angular frequency ω and fixed horizontal wave number k, such that

$$p = \hat{p}(z)e^{-i\omega t}e^{i\vec{k}\cdot\vec{x}}$$
 (6.4.3)

with analogous relations for density ρ , vertical fluid velocity $\hat{\mathbf{w}}$, etc., and impose the condition $\hat{\mathbf{w}}(\mathbf{z}) = 0$ at $\hat{\mathbf{z}} = \mathbf{z}$, we find, after a lengthy analysis, that

$$-\gamma(\hat{\omega}/\Omega)p_0^{-1/\gamma} = \int_{z_0}^{z} p_0^{(1/\gamma - 1)} \{-i[1 - c^2k^2/\Omega^2]\hat{p} - \hat{Q}\} dz \quad (6.4.4)$$

where

$$\hat{Q} = (c^{2}/\Omega^{2})\{(\partial/\partial z)[\eta(ik^{2}\theta + \partial[\vec{k} \cdot \vec{u}]/\partial z)]$$

$$-[(4/3)\eta + \zeta]k^{2}\vec{k} \cdot \vec{u} + i\zeta k^{2}\partial w/\partial z\}$$

$$+ (1/\Omega)\{2\eta(\gamma - 1)(\partial \vec{v}/\partial z) \cdot [\partial \vec{u}/\partial z + i\vec{k}\theta]$$

$$+ (\gamma c_{v})^{-1}(\partial/\partial z)[\kappa(\partial/\partial z)\{\gamma \hat{p} - c^{2}\hat{p})/\rho_{o}\}]$$

$$- (\gamma c_{v})^{-1}k^{2}\kappa(\gamma \hat{p} - c^{2}\hat{p})/\rho_{o}\}$$
(6.4.5)

A priori, we expect Q to be small. Thus it would seem appropriate to neglect all quantities in this expression which are known to be small for the unattenuated Lamb mode. In particular, we neglect all terms involving $\hat{\mathbf{w}}$. Also, since we expect

$$\left|\frac{\partial \mathbf{v}}{\partial \mathbf{z}}\right| << \mathbf{kc}$$

we neglect all terms involving $\partial \vec{v}/\partial z$. In addition, it would appear to be sufficient to take the plane wave relations

$$\hat{\rho} = \hat{\rho}/c^2$$
 ; $\hat{k} \cdot \hat{u} = \Omega \hat{\rho}/\rho_0$

and thus to express Q entirely in terms of p. Thus we obtain

$$\hat{Q} = (c^2/\Omega^2) \{ (\partial/\partial z) \eta [\partial(\Omega \hat{p}/\rho_0)/\partial z] - [(4/3) \eta + \zeta] k^2 \Omega \hat{p}/\rho_0 \}$$

$$+ [(\gamma - 1)/(\Omega c_V)] \{ \partial/\partial z [k\partial/\partial z (\hat{p}/\rho_0)] - k^2 \kappa \hat{p}/\rho_0 \}$$

Next, since η and κ are relatively slowly varying with height, and Ω is also slowly varying, and since, in the Lamb mode,

$$\frac{\partial}{\partial z}(\hat{p}/p_0) \approx [(\gamma - 1)g/c^2]\hat{p}/p_0$$

we can further approximate the above by

$$\hat{Q} = [\{c^2/\Omega\}\{[(\gamma - 1)^2g^2/c^4]\eta - [(4/3)\eta + \zeta]k^2\} + [(\gamma - 1)/(\Omega c_V)]\{[(\gamma - 1)^2g^2/c^4] - k^2\}\kappa]\hat{p}/\rho_0$$
(6.4.6)

If we desire a dispersion relation for the Lamb mode which includes dissipation, we may obtain one by simply taking the guided condition $\widehat{wp}_{0}^{-1/\frac{\gamma}{2}} + 0$ as $z + \infty$. From Eq. (6.4.4) we would have

$$\int_{0}^{\infty} p_{0}^{(1/\gamma)-1} \{-i[1-c^{2}k^{2}/\Omega^{2}]\hat{p} - \hat{Q}\} dz = 0$$
 (6.4.7)

Then, to obtain a lowest order dispersion relation, we simply set $\Omega = \Omega_{\rm L}$ and take

$$\hat{p}(z) = (D)(1/c^2)e^{-\int_{0}^{z} (g/c^2) dz}$$
(6.4.8)

as is appropriate to the Lamb mode in lowest order. Here D is any constant. In this manner, we obtain

$$1 - c_{L}^{2} k^{2} / \Omega_{L}^{2} = -i2 \mu_{d} (k^{2} - k_{d}^{2}) / \Omega_{L}$$
 (6.4.9)

$$2\mu_{\rm d} = \frac{\int \{c^2[4/3 \, \eta + \zeta] + (\gamma - 1)\kappa/c_{\rm v}\}\phi^{-2}\rho_{\rm o}^{-1} \, dz}{\int \phi^{-2} \, dz}$$
 (6.4.10a)

$$k_{\rm d}^2 = \frac{\left[(\gamma - 1)^2 (g^2/c^2) [\eta + (\gamma - 1)\kappa/c_{\rm v}] \phi^{-2} \rho_{\rm o}^{-1} dz \right]}{\left[c^2 [(4/3)\eta + \zeta] + (\gamma - 1)\kappa/c_{\rm v}] \phi^{-2} \rho_{\rm o}^{-1} dz}$$
(6.4.10b)

and where

$$-(2 - \gamma) \int_{0}^{z} (g/c^{2}) dz$$

$$\phi^{-2} = (1/c^{2})e$$
(6.4.11)

is the same as used previously.

Then to first order in $\boldsymbol{\mu}_d$ we find

$$\Omega_{L} = c_{L}k - i\mu_{d}(k^{2} - k_{d}^{2}) \qquad (6.4.12)$$

which corresponds to the wave equation

$$\frac{\partial \psi}{\partial t} + (c_L + v_{Lk}) \frac{\partial \psi}{\partial s} - \mu_d \left(\frac{\partial^2}{\partial s^2} + k_d^2 \right) \psi = 0 \qquad (6.4.13)$$

This should be compared with Eq. (6.3.6). It should be noted that the term

$$-\mu_{d}\left(\frac{\partial^{2}}{\partial s^{2}} + k_{d}^{2}\right)\psi$$

represents the presence of dissipation. Thus we have a correction term to add to that equation. The general relation would be

$$\frac{\partial \psi}{\partial z}$$
 + {(c_L + v_{Lk} + a_{kk} + c_L[(\gamma + 1)/2\gamma]\nu p(0)/p₀(0)}\delta\psi /\delta s

+
$$h_{kk}(\partial^2/\partial s^2 + k_{SL}^2)(\partial \psi/\partial s) - \mu_d(\partial^2/\partial s^2 + k_d^2)\psi = 0$$
 (6.4.14)

In analogy with the usual nomenclature, we might term this the Korteweg-de Vries-Burgers' equation for propagation in the Lamb mode.

The presence of the term k_d^2 is an interesting byproduct of the height stratification of the Lamb mode. Formally, it represents a negative damping and arises from the fact that there is a continuous transfer of energy from high altitudes to low altitudes (or conversely, depending on the wave's phase) due to the fact that the amplitudes of u and p/ρ increase with altitude. In order for the wave to maintain the stratification associated with the Lamb mode, one must assume that this energy is continuously being extracted from the ambient medium. This k_d^2 term is important only for very low frequency propagation and would seem to imply that the mode is weakly unstable at sufficiently low frequencies.

We cannot ascertain whether this is a real instability or merely a fiction of our mathematical technique. However, in any event, the growth of the instability, if it did exist, would be of such a slow rate that it probably would not be possible to detect it in practice.

6.5 HORIZONTAL RAY PATHS

The discussion up to now has assumed the ambient atmosphere to be independent of horizontal coordinates x and y. If this is not so, we expect that much of the preceding can be salvaged if the variation with these coordinates is sufficiently slow. The propagation at long distances would still locally appear as propagation of planar waves (almost constant direction for the horizontal wave numbers k). Thus we might assume the energy (or whatever we might associate with the wave) propagates along horizontal ray paths.

Let us consider a particular characteristic feature of the waveform which is received at some time $\tau(x)$ at locations having a position x on the ground. (The vector x has only x and y components.) A line of constant $\tau(x)$ may be termed a wavefront. In the absence of dispersion, dissipation, and nonlinear effects (all of which we assume to be small) this wavefront moves out from the source with a speed c_{τ} (the height-averaged speed) when viewed by someone moving with the local height-averaged wind velocity v_{t} . Thus if someone moved with speed

$$\frac{d\vec{x}}{dt} = c_L \vec{e}_k + \vec{v}_L \tag{6.5.1}$$

he would always be on a wavefront (assuming he was initially on a wavefront). Here \mathbf{e}_k is the unit outward pointing normal to the wavefront

$$\dot{\vec{e}}_{k} = \nabla \tau / |\nabla \tau| \qquad (6.5.2)$$

Since, for small dt, one must have

$$\tau(x) + dt = \tau(x + [dx/dt]dt)$$

from the identification of dx/dt as wavefront velocity, it follows that

$$\nabla \tau \cdot dx / dt = 1$$

$$\nabla \tau \cdot \{c_{\tau} \nabla \tau / |\nabla \tau| + \overrightarrow{v}_{\tau}\} = 1$$

This gives us the following partial differential equation for T (the eikonal equation)

$$(\nabla \tau)^2 = \frac{(1 - \nabla \tau \cdot v_L^{\dagger})^2}{c_L^2}$$
 (6.5.3)

or, if we abbreviate

$$\vec{k} = \nabla \tau \tag{6.5.4}$$

we have

$$k^2 = (1 - \vec{k} \cdot \vec{v}_L)^2/c_L^2$$
 (6.5.5),

Since k has the units of inverse velocity, we refer to it as the wave slowness vector.

We next consider just how this parameter \vec{k} would vary with time when viewed by someone moving with the speed $c_L e_k + v_L$.

$$\frac{d\vec{k}}{dt} = \left\{ \frac{d\vec{x}}{dt} \cdot \nabla \right\} \vec{k} = \left\{ (c_L \vec{e}_k + \vec{v}_L) \cdot \nabla \right\} \nabla \tau$$

$$= \left\{ \frac{c_L^2 \nabla \tau}{1 - \nabla \tau \cdot \vec{v}_L} \right\} \cdot \nabla (\nabla \tau) + \vec{v}_L \cdot \nabla (\nabla \tau)$$

where we have used Eqs. (6.5.2) and (6.5.3). Let us note that

$$[\nabla \tau \cdot \nabla] \nabla \tau = \frac{\partial \tau}{\partial \mathbf{x}_{\alpha}} \frac{\partial^{2} \tau}{\partial \mathbf{x}_{\alpha} \partial \mathbf{x}_{\beta}} \stackrel{\stackrel{+}{\mathbf{e}}}{=} \frac{1}{2} \frac{\partial}{\partial \mathbf{x}_{\beta}} [\nabla \tau]^{2} \stackrel{\stackrel{+}{\mathbf{e}}}{=} \frac{1}{2}$$

$$= \frac{1}{2} \nabla [(\nabla \tau)^{2}] = \frac{1}{2} \nabla \left\{ \frac{(1 - \nabla \tau \cdot \mathbf{v}_{L})^{2}}{c_{L}^{2}} \right\}$$

$$= -\frac{(1 - \nabla \tau \cdot \overrightarrow{v_L})^2}{c_L^3} \nabla c_L - \frac{(1 - \nabla \tau \cdot \overrightarrow{v_L})}{c_L^2} \nabla [\nabla \tau \cdot \overrightarrow{v_L}]$$

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Thus,

$$\frac{d\vec{k}}{dt} = -\frac{(1 - \vec{k} \cdot \vec{v}_L)}{c_L} \nabla c_L - \nabla (\vec{k} \cdot \vec{v}_L) + \vec{v}_L \cdot \nabla \vec{k}$$

$$= -\frac{(1 - \vec{k} \cdot \vec{v}_L)}{c_L} \nabla c_L - k_\alpha \nabla v_{L\alpha} - v_{L\alpha} [\partial k_\alpha / \partial x_\beta - \partial k_\beta / \partial x_\alpha] \stackrel{\dagger}{e}_{\beta}$$

The last term vanishes since $\nabla x \hat{k} = 0$. Using an identity from vector analysis, we then obtain

$$\frac{d\vec{k}}{dt} = -\frac{(1 - \vec{k} \cdot \vec{v}_L)}{c_L} \nabla c_L - (\vec{k} \cdot \nabla) \vec{v}_L - \vec{k} \times (\nabla x \vec{v}_L)$$
 (6.5.6)

The above relation plus the Eq. (6.5.1), which we rewrite as

$$\frac{d\vec{x}}{dt} = \frac{c_L^{2\vec{k}}}{1 - \vec{k} \cdot \nabla \vec{v}_L} + \vec{v}_L$$
 (6.5.7)

gives us two coupled vector equations (or four coupled scalar equations) which, given v_L and c_L as functions of x, and, given k and x at some time t, enable us to determine a ray trajectory x(t), k(t), as a function of time t. The curve x(t) represents what we might term a horizontal ray path in the x,y plane. There are, in actuality, a family of such paths. We distinguish various members of the family by a parameter θ (whose precise definition is deferred to later) and accordingly write $k(t,\theta)$ and $x(t,\theta)$.

The basic assumption we make here is that propagation along a horizontal ray path is such that the dispersion, nonlinear distortion, and dissipation of the pulse is governed by only the state of the atmosphere immediately above the path. Thus we set the acoustic variables as being of the form

$$p = P(s,\theta,z)\psi(s,t,\theta) \qquad (6.5.8a)$$

$$\dot{\mathbf{u}} = \dot{\mathbf{U}}(\mathbf{s}, \boldsymbol{\theta}, \mathbf{z}) \psi(\mathbf{s}, \mathbf{t}, \boldsymbol{\theta}) \tag{6.5.8b}$$

$$\rho = Q(s,\theta,z)\psi(s,t,\theta) \qquad (6.5.8c)$$

where s is a parameter characterizing distance along the path (although not precisely equal to distance) and where ψ satisfies the partial differential equation (6.4.14)(i.e., the Korteweg-de Vries-Burgers equation) with the coefficients being considered as functions of s and θ .

A definition of s may be obtained from the fact that an increment ds represents a distance in the direction of e. Thus, if one follows a horizontal ray path with the speed given by (6.5.7) one should have s changing at the rate

$$\frac{ds}{dt} = \dot{e}_k \cdot \frac{d\dot{x}}{dt} = c_L + v_{Lk}$$

Thus, if dl is the increment of distance along the path, we have

$$\frac{ds}{d\ell} = \frac{c_L + v_{Lk}}{|c_L \dot{e}_k + \dot{v}_L|} = \frac{c_L + v_{Lk}}{[c_L^2 + 2c_L v_{Lk} + v_L^2]^{1/2}}$$
(6.5.9)

It would appear that, in the usual case where $v_L^2 << c_L^2$, it would be adequate to take ds/dl = 1.

The remaining question we need consider is how the amplitude quantities P, U, and Q vary with height z and with the parameter s. It would appear that the former variation should be that appropriate in the lowest order for the Lamb mode, at the appropriate point on the ground. Thus we might take

$$P = p_0^{1/\gamma} A(s, \theta) \qquad (6.5.10a)$$

$$\vec{v} = [p_0^{1/\gamma}/\rho_0] \{\vec{k}(s,\theta)/(1 - \vec{v}_L \cdot \vec{k})\} A(s,\theta) \qquad (6.5.10b)$$

$$Q = [p_Q^{1/\gamma}/c_L^2]A(s,\theta)$$
 (6.5.10c)

where the ambient pressure and density are considered as functions of z, s, and θ . The quantity $k(s,\theta)$ is the wave slowness vector computed for the point in question from the ray tracing equations. One should note that we have assumed the ratios of \tilde{U} , P, and Q to be always appropriate for a planar wave propagating in the Lamb mode. This would seem to be adequate at moderate distances from the source.

The s variation of the remaining factor $A(s,\theta)$, is determined from the geometrical acoustics law recently espoused by Bretherton and Garrett that a wave propagating in slowly varying inhomogeneous

moving media should propagate such as to conserve wave action, in the absence of nonlinear effects and dissipation. By wave action, one means simply the wave energy divided by the frequency of the wave, as would be seen by someone moving with the fluid. If dispersion is small this law simply means that

$$\nabla_{\mathbf{H}} \cdot \left\{ \frac{(\overset{\rightarrow}{\mathbf{v}}_{\mathbf{g}} + \overset{\rightarrow}{\mathbf{v}}_{\mathbf{L}}) < E >}{1 - \overset{\rightarrow}{\mathbf{k}} \cdot \overset{\rightarrow}{\mathbf{v}}_{\mathbf{L}}} \right\} = 0$$
 (6.5.11)

where $\overset{\rightarrow}{\mathbf{v}}$ is the group velocity and E is the energy density (per unit ar£, of earth surface) in the wave as would be computed for a homogeneous medium by someone moving with the local wind speed. The brackets imply a time average. Neglecting dispersion, we have

$$\vec{v}_{r} = [c_{L}^{2}/(1 - \vec{k} \cdot \vec{v}_{L})]\vec{k}$$
 (6.5.12)

$$E = \int_{z_{g}}^{\infty} \{ (1/2) \rho_{o} \vec{u}^{2} + (1/2) p^{2} / [\rho_{o} c^{2}] \} dz \qquad (6.5.13)$$

with the neglect of the very small kinetic energy of vertical motion associated with the Lamb mode and with the neglect of the correspondingly small change in gravitational potential energy. Here z is the height of the earth's surface. Since, in the absence of nonlinear terms and dissipation, ψ is just a constant times cos [$\omega t - ks + \chi$] where χ is a constant phase for constant frequency waves and since the remaining factors are independent of time, it would appear that $\leq \infty$ may be taken proportional to

$$\langle E \rangle \cong A^2 \int_{z_g}^{\infty} [p_o^{2/\gamma}/(\rho_o c_L^2)] dz$$

$$\approx A^2 c_L^{-2} \int_{z_g}^{\infty} [p_o^{2/\gamma}/\rho_o] dz \qquad (6.5.14)$$

Thus we have

$$\nabla_{ll} \cdot \left\{ \frac{\Lambda^2 (\overset{\rightarrow}{\mathbf{v}_g} + \overset{\rightarrow}{\mathbf{v}_L}) c_L^{-2}}{1 - \overset{\rightarrow}{\mathbf{k}} \cdot \overset{\rightarrow}{\mathbf{v}_L}} \int_{\mathbf{z}_g} [p_o^{2/\gamma}/\rho_o] dz \right\} = 0$$

If we now integrate this relation over a narrow segment of a ray tube bounded by two adjacent rays and apply Gauss' theorem, we obtain (after some algebra)

$$\frac{d}{ds} \left\{ \left[\int_{z_g}^{\infty} [p_o^{2/\gamma}/\rho_o] dz \right] (A^2/c_L^3) (c_L + v_{Lk})^2 J \right\} = 0 \qquad (6.5.15)$$

where J is the Jacobian

$$J = \begin{vmatrix} \frac{\partial x}{\partial s} & \frac{\partial y}{\partial \theta} - \frac{\partial x}{\partial \theta} & \frac{\partial y}{\partial s} \end{vmatrix}$$
 (6.5.16)

in the event the earth's surface is considered flat.

We may also extend the above analysis to take into account earth curvature by simply replacing J by

$$J = r_e \sin(r/r_e) | [(\partial r/\partial s)(\partial \phi/\partial \theta) - (\partial r/\partial \theta)(\partial \phi/\partial s)] |$$
(6.5.17)

where r is great circle distance from the source, r is the radius of the earth, and ϕ is the azimuth angle location of the observer, taking the source as being on the axis.

Once J is determined as a function of s for fixed θ , we may regard Eq. (6.5.15) as an ordinary differential equation; the quantity in braces should be a constant along the ray path and, following a terminology used in sonic boom studies, may be termed the Blokhintzev invariant for the propagation. Note that z could be a function of x and y. Thus the formalism also takes into account the possibility of gradual variations in ground elevation.

6.6 EXCITATION OF LAMB'S MODE

In order to solve the various approximate equations derived in the previous section, some initial conditions are required. The various equations we have derived allow us to: (1) determine the horizontal ray paths given an initial point on the path; (2) determine the amplitude factor $A(s,\theta)$ given its value at the start

of the path; and (3) determine the waveform function $\psi(s,\theta,t)$ given its s dependence at some initial time. In the present section we seek to determine these various initial conditions for waves launched by a low altitude nuclear explosion.

Let the explosion be on the z axis such that x=0, y=0 at the source. Since all waves must originate from the source, it is clear that all horizontal ray paths should ensue from the point (0,0). The initial path direction could be any angle between 0 and 2π . We accordingly choose the angle θ to be the initial direction of k, reckoned counterclockwise with respect of the x axis. The initial value of k for any given path is then found from Eq. (6.5.5) to be given by

$$\vec{k}(0,\theta) = \frac{\vec{n}_{0}(\theta)}{c_{L} + \vec{v}_{L} \cdot \vec{n}_{0}(\theta)}$$
 (6.6.1)

where \vec{n} (θ) is that unit vector making an angle of θ with the x axis. The appropriate values of c_1 and \vec{v}_1 should be those corresponding to the source location. The remaining initial condition is

$$\dot{\mathbf{x}}(0,\theta) = 0 \tag{6.6.2}$$

for all θ . Thus, the horizontal ray paths are completely determined with the integration of Eqs. (6.5.6) and (6.5.7).

The initial conditions on $A(s,\theta)$ and $\psi(s,\theta,t)$ are obtained with reference to the intermediate field solution for a point source in a temperature— and wind-stratified atmosphere. Since the viewpoint adopted in the present chapter is that the only principal effect of the temperature variation and wind profile variations with altitude is to cause the Lamb mode to be dispersed and since the dispersion does not have appreciable effect until relatively large distances, it would appear sufficient to calculate the intermediate field on the supposition that the atmosphere is isothermal and has constant winds. In this event, the Eqs. (2.1.4) reduce to

$$D_{t}^{2}(D_{t}^{2} + \omega_{A}^{2})(p/\sqrt{\rho_{o}}) - c^{2}\nabla_{II}^{2}(D_{t}^{2} + \omega_{B}^{2})(p/\sqrt{\rho_{o}}) - c^{2}D_{t}^{2}(\partial^{3}/\partial z^{2})(p/\sqrt{\rho_{o}})$$

=
$$(4\pi c^2/\sqrt{\rho_0})D_t[D_t^2 - g(\partial/\partial z)][f_E(t)\delta(r - r_0)]$$
 (6.6.3)

with the boundary condition

$$dp/dz + (g/c^2)p = 0$$
 at $z = 0$ (6.6.4)

To isolate the Lamb mode, we write the overpressure as

$$p = p_0^{1/\gamma}(z)F(x,y,t) + \psi$$
 (6.6.5)

where the first term represents the contribution from the Lamb mode and ψ represents any remaining contribution. An orthogonality condition is readily derived which guarantees that

$$\int_{z_{g}}^{\infty} \psi p_{o}^{1/\gamma} / \rho_{o} dz = 0$$
 (6.6.6)

Thus we find the function F satisfies

$$(D_t^2 + \omega_D^2)(D_t^2 - c^2\nabla_H^2)F =$$

$$\frac{\int\limits_{z_g}^{\infty} (4\pi c^2) (p_o^{1/\gamma}/\rho_o) D_t (D_t^2 - g(\partial/\partial z)) [f_E(t)\delta(\vec{r} - \vec{r}_o) dz}{\int\limits_{z}^{\infty} (p_o^{2/\gamma}/\rho_o) dz}$$

or

$$(D_{t}^{2} - c^{2}\nabla_{II}^{2})F = 4\pi c^{2}QD_{t}[f_{E}(t)\delta(x - x_{o})\delta(y - y_{o})]$$
 (6.6.7)

$$Q = \frac{p_0^{1/\gamma}(z_0)/\rho_0(z_0)}{\int_{z_0}^{\infty} [p_0^{2/\gamma}/\rho_0] dz}$$
(6.6.8)

To simplify the analysis, we assume that the source is drifting horizontally with the wind speed. In a coordinate system moving with the source, the solution of (6.6.7) is readily found to be

$$F = 2Qc \int_{-\infty}^{c} \frac{f_E^{\dagger}(\tau) d\tau}{[c^2(t-\tau)^2 - R^2]^{1/2}}$$
 (6.6.9)

where R is the net horizontal distance from the source. The only distinction for the fixed coordinate system is that we replace R by R^* where

$$(R*)^2 = (x - vt)^2$$
 (6.6.10)

Since the excited pulse is of relatively short duration, we may consider the dominant contribution in the integration to come from values of τ near where $c(t-\tau) \approx R$. In this event, Eq. (6.6.9) simplifies to

$$F = (2c/R)^{1/2}Q \int_{-\infty}^{t-R/c} \frac{f_E^{\dagger}(\tau) d\tau}{[(t-\tau)-R/c]^{1/2}} = (2c/R)^{1/2}QG(t-R/c)$$
(6.6.11)

where

$$G(t) = \int_{-\infty}^{t} \frac{f_{E}^{*}(\tau) d\tau}{[t - \tau]^{1/2}}$$
(6.6.12)

is similar to the Whitham F-function utilized in the theory of sonic boom propagation.

The function G(t) can be evaluated with recourse to Eq. (2.1.5b). We find that

$$G(t) = Y_{KT}^{1/2} [p_0(z_0)/p_0(0)]^{1/2} [c(0)/c(z_0)]^{1/2} L_s P_s t_s^{1/2} M(t/T_y)$$

$$T_{Y} = [c(0)/c(z_{0})][p_{0}(0)/p_{0}(z_{0})]^{1/3}Y_{KT}^{1/3}t_{g}$$

$$M(X) = \int_{0}^{X} (1 - \xi)e^{-\xi}[X - \xi]^{-1/2} d\xi U(X)$$

$$= \{\sqrt{X} + (1 - 2X)e^{-X} \int_{0}^{\sqrt{X}} e^{y^{2}} dy\} U(X) \qquad (6.6.13)$$

The various symbols used above have the same meaning as in Chapter 2.

If the source time duration T_Y is sufficiently short or if the winds are sufficiently weak, such that at moderate distances R, one has R >> $|\vec{v}_L|T_Y$, then it would appear sufficient to take

$$R^* = c_L s/(c_L + v_{Lk})$$
 (6.6.14)

where s is the distance parameter defined by Eq. (6.5.9).

Since, with the above approximation, the only t dependence is the function M, it would appear that we can choose

$$\psi(t,s,\theta)_{t=0} = M(-s/[(c_L + v_{Lk})T_V])$$
 (6.6.15)

where the range of s is formally considered as encompassing negative as well as positive values.

The remaining quantity of interest, the amplitude factor A, is given by Eq. (6.5.15) as

$$A = \frac{B c_L^{3/2}}{J^{1/2}(c_1 + v_{1L})I^{1/2}}$$
 (6.6.16)

where J is the Jacobian and I is the integral

$$I = \int_{z_g}^{\infty} (p_o^{2/\gamma}/\rho_o) dz \qquad (6.6.17)$$

The constant B is a quantity which we may obtain with detailed comparison with the intermediate range solution. Since, for small s, we can show that

$$J = \frac{sc_L}{c_L + v_{Lk}}$$
 (6.6.18)

we identify

$$B = \left[\left\{ \frac{XY_{KT}^{1/2}(c_L + v_{Lk})}{I^{1/2}c_L^{3/2}} \right\} p_o^{\gamma}(z_o)/\rho_o(z_o) \right]_{x=0, y=0}$$
(6.6.19)

where

$$K = {\sqrt{2} L_s P_s (c_L t_s)^{1/2} [c(0)/c(z_o)]^{1/2} [p_o(z_o)/p_o(0)]^{1/2}}_{x=0, y=0}$$
(6.6.20)

Thus, in summary, we have the acoustic pressure given by

$$p = KY_{KT}^{1/2} D(x) D(x) D(x) [\Lambda(x)/\Lambda(x)] \psi(t,s,\theta) /J^{1/2}$$
 (6.6.21)

where

$$D(x) = \frac{p_{o}/\rho_{o}^{1/2}}{\left\{ \int_{z_{g}}^{\infty} [p_{o}^{2\gamma}/\rho_{o}] dz \right\}^{1/2}}$$
 (6.6.22a)

$$\Lambda(\vec{x}) = \rho_0^{1/2} [c_L^{3/2} / (c_L + v_{Lk})]$$
 (6.6.22b)

The quantity K is given by Eq. (6.6.20) while the Jacobian J is given by Eq. (6.5.16) or Eq. (6.5.17). The quantity ψ satisfies the Eq. (6.4.14), with the initial condition (6.6.15).

6.7 SOLUTION OF THE LINEARIZED KORTEWEG-DE VRIES EQUATION

The determination of the waveform profile $\psi(t,s,\theta)$ is probably the chief computational obstacle to the procedure outlined in the preceding sections. Here we outline the method of solution in the neglect of nonlinear and dissipation terms. This may be an adequate approximation for all cases of interest, although one cannot say this with certainty until he has some quantitative estimates of the effects of the neglected terms.

With the neglect of dissipation and nonlinear terms the Eq. (6.4.14) becomes

$$\partial \psi / \partial t + c_{\mu} \partial \psi / \partial s + D \partial^3 \psi / \partial s^3 = 0$$
 (6.7.1)

where

$$c_e = c_L + v_{Lk} + a_{kk} + h_{kk}k_{BL}^2$$
 (6.7.2a)

$$D = h_{kk}$$
 (6.7.2b)

or, to the same approximation,

$$\partial \psi / \partial t + c_e \partial \psi / \partial s - (D/c_e^3) \partial^3 \psi / \partial t^3 = 0$$
 (6.7.3)

To put this in a form appropriate to the case where c and D are slowly varying functions of s, we consider ψ to be a function of parameters t and s, where

$$\overline{t} = t - \int_{0}^{8} (1/c_e) ds$$
 (6.7.4a)

$$\frac{1}{s} = \int_{0}^{s} (D/c_{e}^{h}) ds \qquad (6.7.4b)$$

such that Eq. (6.7.3) becomes

$$\frac{\partial \psi}{\partial \overline{z}} - \frac{\partial^3 \psi}{\partial \overline{z}^3} = 0 \tag{6.7.5}$$

If ψ is specified when $\overline{s}=0$ as ψ (\overline{t}), then the solution to Eq. (6.7.5) may be found, after some analysis, to be given by

$$\psi(\overline{s},\overline{t}) = \frac{1}{\sqrt{\pi} (3\overline{s})^{1/3}} \int_{-\infty}^{\infty} Ai \left[\frac{\overline{t}_{o} - \overline{t}}{(3\overline{s})^{1/3}} \right] \psi_{o}(\overline{t}_{o}) d\overline{t}_{o}$$
 (6.7.6)

where Ai(x) is the Airy function defined by

Ai(x) =
$$\frac{1}{\sqrt{\pi}} \int_{0}^{\infty} \cos(v^3/3 + xv) dv$$
 (6.7.7)

In terms of s and t we have

$$\psi(s,t) = \frac{1}{\sqrt{\pi} \tau_D} \int_{-\infty}^{\infty} Ai \left(\frac{t_o + \tau_c - t}{\tau_D} \right) \psi_o(t_o) dt_o \qquad (6.7.8)$$

where $\boldsymbol{\tau}_{c}$ and $\boldsymbol{\tau}_{D}$ are functions of s given by

$$\tau_{c} = \int_{0}^{s} (1/c_{e}) ds$$
 (6.7.9a)

$$\tau_{\rm D} = \left\{ 3 \int_{0}^{8} (D/c_{\rm e}^{4}) \, ds \right\}^{1/3} \tag{6.7.9b}$$

For the problem of interest, we find from reasoning similar to that which leads to Eq. (6.6.15), that

$$\psi_o(t_o) = M(t_o/T_Y)$$

where the function M is as given by (6.6.13). Thus

$$\psi(s,\theta,t) = \frac{1}{\sqrt{\pi} \tau_D} \int_{-\infty}^{\infty} Ai \left(\frac{t_o + \tau_c - t}{\tau_D} \right) M(t_o/T_Y) dt_o$$

$$= \frac{1}{\sqrt{\pi} \tau_D} \int_{0}^{\infty} Ai \left(\frac{\tau_c - t}{\tau_D} + \mu \frac{T_Y}{\tau_D} \right) M(\mu) d\mu \qquad (6.7.10)$$

with a change of integration variable and recognition of the fact that M=0 for $\mu<0$.

It is of some interest to examine Eq. (6.7.10) in the limit of small yields as it is not immediately apparent that the well-known law of yield-amplitude proportionality holds for the single mode model. The correct behavior in this limit is somewhat subtle since the function $M(\mu)$ is not integrable. With reference to Eq. (6.6.13), we write

$$M(\mu) = \int_{0}^{\mu} [f(\xi)/(\mu - \xi)^{1/2}] d\xi \qquad (6.7.11)$$

where

$$f(\xi) = (1 - \xi)e^{-\xi}$$
 (6.7.12)

Then Eq. (6.7.10) becomes

$$\psi = \frac{T_{Y}/\tau_{D}}{\sqrt{\pi}} \int_{0}^{\infty} d\mu \int_{0}^{\infty} d\xi \operatorname{Ai}\left[\frac{\tau_{c} - t}{\tau_{D}} + \mu \frac{T_{Y}}{\tau_{D}}\right] f(\xi) \frac{U(\mu - \xi)}{(\mu - \xi)^{1/2}}$$

$$= \frac{T_{Y}/\tau_{D}}{\sqrt{\pi}} \int_{0}^{\pi} f(\xi) \int_{\xi}^{\pi} Ai \left(\frac{\tau_{c} - t}{\tau_{D}} + \mu \frac{T_{Y}}{\tau_{D}} \right) \frac{1}{(\mu - \xi)^{1/2}} d\mu d\xi$$

In the integral over μ we set μ - ξ = (α^2)(τ_D^2/T_Y^2) and obtain

$$\psi = \frac{2(T_{Y}/\tau_{D})^{1/2}}{\sqrt{\pi}} \int_{0}^{\infty} f(\xi) \left\{ \int_{0}^{\infty} Ai \left[\frac{\tau_{c} - t}{\tau_{D}} + \xi \frac{T_{Y}}{\tau_{D}} + \alpha^{2} \right] d\alpha \right\} d\xi \qquad (6.7.11)$$

We next expand the integrand in a power series in T_v/τ_n . Since

$$\int_{0}^{\infty} f(\xi) d\xi = 0$$
 (6.7.12)

the first non-zero term is

$$\psi = -\frac{2(T_{Y}/\tau_{D})^{3/2}}{\sqrt{\pi}} \left\{ \int_{0}^{\infty} f(\xi) \xi d\xi \right\} \left\{ \int_{0}^{\infty} At' \left[\frac{\tau_{C} - t}{\tau_{D}} + \alpha^{2} \right] d\alpha \right\}$$

or

$$\psi = (2/\sqrt{\pi}) (T_{Y}/\tau_{D})^{3/2} PP([t - \tau_{c}]/\tau_{D})$$
 (6.7.13)

where PP(x) is a function defined by

$$PP(x) = \int_{0}^{\infty} Ai^{\dagger}(\alpha^{2} - x) d\alpha \qquad (6.7.14)$$

According to Eq. (6.6.12), the overpressure varies with yield as $T_{\nu}^{1/2}$. However, the above shows that ψ varies with yield as $T_{\nu}^{1/2}$. But $T_{\nu}^{1/2}$ varies with yield as $T_{\nu}^{1/2}$. Thus the amplitude is directly proportional to yield and the waveform shape is independent of yield in the limit of small yields. The limit applies, strictly speaking, when T_{ν}/τ_{D} << 1 and is accordingly more appropriate at larger distances and for propagation with strong dispersion (large D).

6.8 SURMARY

Although the results are reasonably simple the derivation of the single mode theory given in the present chapter is somewhat intricate. It would therefore seem appropriate to pause here and summarize the various results scattered throughout the chapter from an operational point of view. The basic assumption is that the earliest portion of the wave which arrives with transit speeds of the order of the sound speed at the ground may be interpreted as being caused by a single guided mode, which is the real atmosphere's counterpart of Lamb's guided mode for the isothermal atmosphere. The dispersion of this mode is small, but important. However, this dispersion is neglected in determining the ground projected ray paths along which the mode travels.

The determination of these ground projected paths is the same as for two dimensional acoustics in a medium having sound speed c. (L for Lamb) and wind velocity v. Both c. and v. are in general functions of position on the earth's surface and are averages over height z of the sound speed and wind velocity profiles. The manner in which these averages should be taker turns out to be

$$c_{L}^{2} = \frac{\int_{z}^{z} [p_{o}^{2/\gamma}/\rho_{o}] dz}{\int_{z_{g}}^{z} \{p_{o}^{2/\gamma}/[\rho_{o}e^{2}]\} dz}$$
(6.8.1)

$$\vec{v}_{L} = \frac{\int_{z_{g}}^{z} \vec{v}[p_{o}^{2/\gamma}/\rho_{o}] dz}{\int_{z_{g}}^{z} [p_{o}^{2/\gamma}/\rho_{o}] dz}$$
(6.8.2)

where p and p are ambient pressure and density, γ is the specific heat ratio, and $z_{\rm g}$ is the ground level.

The rays all start out on a point on the ground directly below the source and are distinguished from each other by a parameter θ which ranges from 0 to 2π . A given ray may be characterized by giving the position $\mathbf{x}_{\mathbf{H}}(\mathbf{s},\theta)$ and wave slowness vector $\mathbf{k}(\mathbf{s},\theta)$ as functions of \mathbf{s} , where \mathbf{s} is a function of distance along the path (which is the same as distance in the limit of no winds).

Along or above a given path the acoustic pressure p is given by

$$p = KY_{KT}^{1/2}D(\vec{x})D(\vec{x}_{o})[\Lambda(\vec{x})/\Lambda(\vec{x}_{o})]\psi(t,s,\theta)/J^{1/2}$$
 (6.8.3)

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where

$$K = {\sqrt{2} L_s P_s (c_L t_s)^{1/2} [c(0)/c(z_o)]^{1/2} [p_o(z_o)/p_o(0)]^{1/2}}_{source}$$
(6.8.4a)

$$D(x) = \frac{p_{\bullet}^{\gamma}/\rho_{o}^{1/2}}{\left[\int_{z_{g}}^{\infty} [p_{o}^{2/\gamma}/\rho_{o}] dz\right]^{1/2}}$$
(6.8.4b)

$$\Lambda(\mathbf{x}) = \rho_0^{1/2} [c_L^{3/2}/(c_L + v_{Lk})]$$
 (6.8.4c)

$$L_s = 1 \text{ kilometer}$$
 (6.8.4d)

$$P_g = 1.61 \times 34.45 \times 10^3 \text{ dynes/cm}^2$$
 (6.8.4e)

$$t_s = 0.48 \text{ sec.}$$
 (6.8.4f)

$$J = r_a \sin(r/r_e)[\partial r/\partial s)(\partial \phi/\partial \theta) - (\partial r/\partial \theta)(\partial \phi/\partial s)]$$
 (6.8.4g)

$$\phi$$
 = azimuth angle of observer location (6.8.41)

$$\mathbf{v}_{\mathbf{l},\mathbf{k}} = \dot{\mathbf{v}}_{\mathbf{l}} \cdot \dot{\mathbf{k}} / |\dot{\mathbf{k}}| \tag{6.8.4j}$$

The quantity $\psi(t,s,\theta)$ satisfies a partial differential equation known as the Korteweg-de Vries-Burgers' equation

$$\partial \psi / \partial t + [c_e + \beta] \partial \psi / \partial s + D \partial^3 \psi / \partial s^3 - \mu_d [\partial^2 / \partial s^2 + k_d^2] \psi = 0$$
 (6.8.5)

where

$$c_e = c_L + v_{Lk} + a_{kk} + h_{kk}k_{BL}^2$$
 (6.8.6a)

$$\beta = c_L[(\gamma + 1)/(2\gamma)]vp(z_g)/p_o(z_g)$$
 (6.8.6b)

$$D = h_{kk} \tag{6.8.6c}$$

The remaining quantities a, h, h, ν , μ_d , \vec{k}_d , and \vec{k}_{BL} are defined in Eqs. (6.2.20), (6.3.4) and (6.4.10).

In the derivation of Eq. (6.8.5), it was assumed that the terms with coefficients β , D, and μ_d were all relatively small. It was also assumed that all the coefficients were slowly varying. Thus to the same order of approximation, one may set $\partial/\partial s = -c^{-1}\partial/\partial t$ in the higher order terms and obtain the alternate form

$$\partial \psi / \partial s + c_e^{-1} \partial \psi / \partial t - (\beta / c_e^2) \partial \psi / \partial t - (D / c_e^4) \partial^3 \psi / \partial t^3$$

$$- (\mu_D / c_e^3) (\partial^2 / \partial t^2 + c_e^2 k_d^2) \psi = 0 \qquad (6.8.7)$$

Either of the forms (6.8.5) or (6.8.7) may be used.

If one chooses to use Eq. (6.8.7), then $\psi(s,\theta,t)$ must be specified when s=0. The choice prescribed by the analysis is

$$\psi(0,\theta,t) = M(t/T_{V})$$
 (6.8.8)

where

$$M(x) = {\sqrt{x} + (1 - 2x)e^{-x}} \int_{0}^{\sqrt{x}} e^{y^{2}} dy U(x)$$
 (6.8.9a)

$$T_{Y} = \{ [c(z_g)/c(z_o)] [p_o(z_g)/p_o(z_o)]^{1/3} Y_{KT}^{1/3} t_s \}_{source}$$
 (6.8.9b)

We succeeded in solving the initial value problem when β = μ_d = 0 and found

$$\psi = \frac{T_{Y}/\tau_{D}}{\sqrt{\pi}} \int_{0}^{\infty} Ai \left(\frac{\tau_{c} - t}{\tau_{D}} + \mu \frac{T_{Y}}{\tau_{D}} \right) M(\mu) d\mu \qquad (6.8.10)$$

where

$$\tau_{c} = \int_{0}^{s} (1/c_{e}) ds$$
 (6.8.11a)

$$\tau_{D} = \left\{ 3 \int_{0}^{s} (D/c_{e}^{4}) ds \right\}^{1/3}$$
 (6.8.11b)

Furthermore, in the limit of small yields, we find

$$\psi = (2/\sqrt{\pi}) (T_{Y}/\tau_{D})^{3/2} PP([t - \tau_{c}]/\tau_{D})$$
 (6.8.12)

where

$$PP(x) = \int_{0}^{\infty} Ai'(\alpha^2 - x) d\alpha \qquad (6.8.13)$$

which demonstrates yield-amplitude proportionality.

In conclusion, the authors state that this approach appears extremely promising. An initial test of the theory will be to see how well its predictions agree with the computations performed using INFRASONIC WAVEFORMS for stratified atmospheres. If this works out, then we may expect to have a number of interesting areas to explore. One hope is that we may be able to explain data such as presented by Wexler and Hass in detail.

Appendix A

BIBLIOGRAPHY ON INFRASONIC WAVES

The following bibliography is a compendium of papers and books which have come to the attention of the authors as having some relation (either direct or indirect) to the long range propagation of mechanical radiation through the atmosphere. While no claims are made as to its completeness, it is the most comprehensive and up-to-date bibliography specifically restricted to this topic of which the authors are currently aware.

For ease of referral, the subject matter has been broken down into a number of categories as follows:

- 1. Books on acoustics, wave propagation, hydrodynamics and mathematical physics
- 2. Meteorology, including data on atmospheric structure
- 3. Theoretical papers on acoustic-gravity waves and gravity waves in the atmosphere
- 4. Theoretical papers on higher frequency atmospheric waves
- 5. Observations of infrasonic waves in the lower atmosphere
- 6. Observations of infrasonic waves in the ionosphere
- 7. Data concerning the properties of nuclear explosions
- 8. Related papers on the mathematical theory of wave propagation, and on mathematical techniques useful in wave propagation
- 9. Nonlinear effects on wave propagation, including shock waves
- 10. Instrumentation
- 11. Data analysis techniques

The classification scheme is not mutually exclusive, although we have generally classified each reference under only one heading.

This bibliography is an updated and expanded version of one given previously in 1967 by Pierce and Moo. Since we hope at some later date to issue, in turn, a revised version of the present bibliography, we request that readers notify the authors of any neglected papers, errors, etc.

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A.11 DATA ANALYSIS TECHNIQUES

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Appendix B

Deck Listing

of

INFRASONIC WAVEFORMS

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MAIN PROGRAM
                                                           7/23/68
                                                                                                           MAIN
                                                                                                           MAIN
                *************
                                                                                                          MAIN
C****
                                                                                                           MAIN
              PROGRAM TO SYNTHESIZE PRESSURE WAVEFORMS OF ACOUSTIC
                                                                                                          MAIN
              GRAVITY WAVES GENERATED BY NUCLEAR EXPLOSIONS IN THE
                                                                                                          MAIN
                                                                                                          MAIN
C.
                                                                                                          MAIN
MAIN
                                                                                                          MAIN
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                           ----ARSTRACT----
                                                                                                          MAIN
                                                                                                          MAIN
   TITLE - MAIN PROGRAM
                                                                                                          MAIN
            GENERAL PURPOSE PROGRAM FOR STUDYING THE PROPAGATION OF NUCLEAR EXPLOSION GENERATED ACQUISTIC GRAVITY WAVES IN THE ATMOSPHERE.
                                                                                                          MAIN
                                                                                                          MAIN
                                                                                                                   15
                                                                                                          MAIN
                                                                                                                   16
                     THE ATHOSPHERE IS APPROXIMATED BY A MULTILAYER ATMOSPHERE
                     WITH CONSTANT WIND VELOCITY AND TEMPERATURE IN EACH LAYER THE NUMBER OF LAYERS, WIDTHS OF LAYERS. AND PROPERTIES OF LAYERS MAY BE SELECTED BY THE USER. THE GROUND AT 2=0 IS ASSUMED FLAT AND RIGID. THE UPPERMOST LAYER OF THE ATMOSPHERE IS ASSUMED TO BE UMBOUNDED FROM ABOVE.
                                                                                                          MAIN
                                                                                                          MATM
                                                                                                                   19
                                                                                                          MAIN
                                                                                                                   20
                                                                                                          MATN
                                                                                                                   21
                                                                                                          MAIN
C
                                                                                                          MAIN
                     THE SOURCE IS SPECIFIED BY ITS HEIGHT OF BURST AND ENERGY VIELD. IT IS APPROXIMATED AS A POINT ENERGY SOURCE WITH TIME DEPENDENCE CONFORMING TO CUBE ROOT (HYDRODYNAMIC) SCALING DERIVED FROM THE EFFECTS OF NUCLEAR WEAPONS
                                                                                                          MAIN
                                                                                                          MAIN
C
                                                                                                          MAIN
c
                                                                                                          MAIN
                     (U.S. GOVERNMENT PRINTING OFFICE, 1962).
                                                                                                          MAIN
                                                                                                                  28
Ċ
                                                                                                          MAIN
                                                                                                                  29
                     THE OBSERVER LOCATION MAY BE SPECIFIED ARBITRARILY.
HOWEVER, THE COMPUTATION INCLUDES ONLY CONTRIBUTIONS FROM
FULLY DUCTED GUIDED MODES AND ACCORDINGLY GIVES A SOLUTIO
VALID (AT BEST) ONLY AT LARGE HORIZONTAL DISTANCES.
ALSO, THE PROGRAMMING IS BASED ON THE PREMISE THAT ONLY
                                                                                                          MAIN
                                                                                                                  30
C
                                                                                                          MAIN
                                                                                                          MATM
                                                                                                          MAIN
                                                                                                                  33
                                                                                                          MAIN
                     PORTIONS OF MODES MITH PHASE VELOCITIES GREATER THAN THE MAXIMUM WIND SPEED ARE TO BE INCLUDED INTO THE COMPUTATIO THE PROGRAM CANNOT THEREFORE BE APPLIED TO THE STUDY OF
                                                                                                          MAIN
                                                                                                         MAIN
                                                                                                                  36
                                                                                                                  37
                     COITICAL LAYER EFFECTS.
                                                                                                          MAIN
                                                                                                                  38
                                                                                                          MAIN
  LANGUAGE
                  - FORTRAN IV (360, REFERENCE MANUAL C28-6515-4)
                                                                                                          MAIN
                                                                                                                  40
                                                                                                          MAIN
                                                                                                                  41
   AUTHORS
                  - A.D.PIERCE AND J.POSFY. M.I.T., JUNE-1968
                                                                                                          MAIN
                                                                                                          MAIN
                           ----IISAGF----
                                                                                                          MAIN
                                                                                                                  44
                                                                                                          MAIN
         ALL DATA IS INPUT IN THE NAMELIST FORMAT. FACH SEQUENCE OF DATA
                                                                                                          MAIN
                                                                                                                  46
         MUST INCLUDE A NAM1 GROUP AT THE BEGINNING.
                                                                                                          MAIN
                                                                                                          MAIN
                                                                                                          MAIN
CENAMI
               NS 'RT= . NPRNT= . NPNCH=
                                                             SEND
                                                                                                                  49
                                                                                                          MATN
                                                                                                                  50
         THE REMAINDER OF THE DATA TO BE SUPPLIED DEPENDS ON THE VALUE
        OF NSTART.
                                                                                                          MAIN
                                                                                                          MAIN
                                                                                                                  53
                                                                                                          MAIN
              LANGLE=
THETK=
                                              . OM1=
CENAM2
                           . IMAX=
                                                                VKNT x=
                             7=
7085=
                                                                                                   ٤E
                                                                                                          MAIN
                                                             ETC.
CENAM4
                                                                                                         MAIN
CENAM6
              7SCRCF=
                                          SEND
                                                                                                         MAIN
                                                                                                                  57
CENAMA
               YIFLD=
                                                                                                          MAIN
                                                                                                                  58
                                                      . ROBS=
                                                                   . IOPT=
CENAM10
              TFIRST=
                              TEND=
                                        . DELTT=
                                                                                    & END
                                                                                                          MAIN
                                                                                                                  59
                                                                                                          MAIN
                                                                                                                  60
             *NSTART=2***
                                                                                                          MAIN
                                                                                                                  61
                                          ..., VXI=
CENAMS
               MAX=
                           . CT=
                                                                                                          MAIN
                                     . V?=
CENAMA
                                                          . FCT.
              THETK=
                           . V1=
                                               . OM1=
                                                                                    EFND
                                                                                                          MAIN
                           . ZOBS=
                                          SEND
C ENAM6
              ZSCRCE*
                                                                                                         MATN
                                                                                                                  64
                              & FND
CENAMB
               YTELD=
                                                                                                          MAIN
                                                                                                                  65
O IMAND T
              TFIRST=
                             TEND=
                                        . DELTT= . ROBS= . IOPT=
                                                                                    GENT
                                                                                                          MAIN
                                                                                                                        PROGRAM
                                                                                                                  66
                                                                                                         HAIN
                                                                                                                           MAIN
              NSTART=3++++
                                                                                                         MAIN
                                                                                                                  68
CENAMS
                                                                 .... ETC.
               IMAX=
                           • CI=
                                                                                                                  69
                                                                                    & EN D
                                                                                                         MAIN
                                                                                                                            PAGE
               7SCR CE=
CENAMO
                           . Z 08 S=
                                           EFND
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Service Committee Committe

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CÉNAMA.
              YIELD=
                              E END
                                                                   . INPT=
                           . TEND= . DELTT= : ROBS=
                                                                                    CEND
              TETOSTE
CENAMIO
                                                                                                          MAIN
                                                                                                          MIAN
CENANT
                                  **** VPMOD=
                                                       .... MDFMO= , ETĈ.
                                                                                                          MAIN
                                                                                                                  75
              CHÁC D=
                                                                                                          MAIN
CENAMS
              Y1ÈLD=
                              & END
                                                                                                                  76
77
                                       . DELTT=
                                                      , ROBS=
                                                                                                          MAIN
                                                                     IPPT
                                                                                    SEND
CENAMIO
              TFIRST=
                           . TEND=
                                                                                                          MAIN
        ****NSTART=5***
             MDFND= . KST=
TFIRST= . TEN
                          KST= . ... KFIN= . ..
                                                                                                          MAIN
                                                                                      . ETC.
                                                                   . 10PT=
                                                                                    SEND
                                                                                                          MÀIN
                                                                                                          MAIN
                                                                                                                  82
                                                                                                          MAIN
         ###ONSTART=6####
CINO ADDITIONAL DATA IS NEEDED. COMPUTATION TERMINATES.)
                                                                                                          MAIN
         FOR A COMPLETE LIST OF VARIABLES THAT ARE INCLUDED IN A GIVEN
                                                                                                          MAIN
         NAMPLIST GROUP, SEE NAMELIST STATEMENTS IN PROGRAM.
                                                                                  NOTE THAT
                                                                                                          MAIN
                                                                                                                  87
        DATA INPUT BY READIS.NAM1). READIS.NAM2). ETC.. NEED NOT INCLUDE VALUES OF ALL VARIABLES IN THE CORRESPONDING NAMELIST GROUP. ONE NEED ONLY INPUT THOSE VALUES NEEDED FOR THE CALCULATION AND WHICH ARE NOT ALREADY IN STORAGE.
                                                                                                         MAIN
                                                                                                                  88
                                                                                                          MAIN
                                                                                                                  89
                                                                                                          MAIN
                                                                                                                  90
                                                                                                          MATN
                                                                                                          MAIN
         DATA ASSOCIATED WITH NAMS, NAMS, NAMS, AND NAMS SHOULD IN GENERAL
                                                                                                          MAIN
         NOT BE SUPPLIED ARBITRARILY. BUT MAY BE OBTAINED FROM PREVIOUS
                                                                                                          MAIN
        RUNS OF THE PROGRAM. IF NSTART=1. NPNCH=1. DATA CARDS FOR NAM3. NAM5. NAM7. AND NAM9 ARE AUTOMATICALLY PUNCHED. IF NSTART=2. NPNCH=1. DATA CARDS FOR NAM5. NAM7. AND NAM9 ARE PUNCHED. IF NSTART=3. NPNCH=1. DATA CARDS FOR NAM7 AND NAM9 ARE PUNCHED. IF NSTART=4. NPNCH=1. DATA CARDS FOR NAM9 ARE PUNCHED. IF NSTART=4. NPNCH=1. DATA CARDS FOR NAM9 ARE PUNCHED.
                                                                                                          MATN
                                                                                                                  95
                                                                                                          MAIN
C
                                                                                                          MAIN
                                                                                                          MAIN
                                                                                                          MAIN
                                                                                                                  99
                                                                                                          MAIN 100
        THE NEXT RATCH OF DATA AFTER NAMIO SHOULD BE NAMI. THE LAST DATA CARD SHOULD BE NAMI WITH NSTART=6.
                                                                                                          MAIN 101
                                                                                                          MATN
                                                                                                                102
                                                                                                          MAIN
                                                                                                                103
                           ----EXTERNAL SUBROUTINES REQUIRED----
                                                                                                          MATH 105
         SUBROUT INE
                              TYPE
                                           CALLED SY
                                                                                                          MAIN 106
                                                                                                          MAIN 107
                                           ELINT. HMMM. NAPPDE. NMDFN
                                                                                                          MAIN 108
                              SIR
C
         AAAA
                              SUB
                                           TMPT
         AK I
         ALLMOD
                                           MATN
                                                                                                          HAIN 110
                              SUB
                               SUB
                                           PAMPDE
                                                                                                          MAIN 11;
                                                                                                          MAIN 112
C
         ATHOS
                              SUR
                                           MAIN
                                                   (Maiate CALCOMP ROUTINE)
                                                                                                          HAIN 113
         AXIS1
                              SUB
                                           TMPT
                                           ELINT
         BBBB
                              SUB
CCC
                                           BBBB.MMMK
                                                                                                          MAIN
                              FUNC
         CAI
         DXDY1
                                           TMPT
                                                   (M.I.T. CALCOMP ROUTINE)
                                                                                                          MAIN 116
                                           TOTINT
                                                                                                          MAIN 117
000
         EL INT
                               SUB
                                           TMPT (N.I.T. CALCOMP ROUTINE)
MODETR (EXTERNAL FOR ARG. OF RTMI)
MODETR (EXTERNAL FOR ARG. OF RTMI)
                                                                                                          MATN
                                                                                                                118
         ENDPLT
                               SUB
         FNMOD1
                              FUNC
                               FUNC
         FNMOD2
                                                                                                          MAIN 121
                               SUB
                                                                                                          MATH 122
         MMMM
                               SUB
                                           NAMPDE . RRRR
                                           ALLMOD
                                                                                                          MAIN 123
C
         MODETR
                               SUR
                               SUB
                                           MATN
         MODLST
                                                                                                          MAIN 125
Č
                               SUB
                                           TABLE
         MPOUT
         NAMPDE
                                                                                                          MAIN 126
                               SUR
                                           TMPT (M.I.T. CALCOMP ROUTINE)
FNMOD1.FNMOD2.LNGTHN.MPOUT.WIDEN
TMPT (M.I.T. CALCOMP ROUTINE)
                                                                                                          MAIN 127
         NEWPLY
                               SUB
00000
                                                                                                                128
                                                                                                          MAIN
         NMDFN
                              SUB
         NUMBR 1
                               SUB
                                           ALLMOD
                                                                                                          MAIN 130
         NXMODE
                               SUB
                               SUB
                                           MODETR
                                                                                                          MAIN 131
         PAMPOE
                               SUA
                                           MAIN
                                                                                                          MAIN
                                                                                                                 132
                                                                                                          MAIN 133
                               SHR
                                           SOURCE
         PHASE
                               SUB
                                                                                                          HAIN 134
                                           TMPT
                                                   (M.I.T. CALCOMP ROUTINE)
         PL OT 1
                                                                                                          MAIN 135
         PPAMP
                               SUR
                                            MAIN
                               SUB
                                                                                                          MAIN 136
MAIN 137
                                                                                                                        PROGRAM
          PRATHO
                                                                                                                           VIAM
         RARR
                               SUB
                                            NMDFN
                                           MODETR (IBM SCIENTIFIC SUBROUTINE)
                                                                                                          MAIN 138
         RTMI
                               SUB
                                           BBBR.MMMM
                               FUNC
         SAT
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TMPT (M.I.T. CALCOMP ROUTINE)

SCL GPH

SUR

MAIN 140

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SOURCE
                             SHA
                                         PPAMP
                                                                                                       PA 1N:141
                                                                                                       MATH 142
        SUSPCT
                             SIM
                                          TABLE
        SYMBLS
                                          THET
                                                  IN. I.T. CALCOMP ROUTINE)
                                                                                                       MAIN-143
                             SUS
        TARLE
                             SUB
                                                                                                       MATH 144
                                         MAIN
        TABERT
                             SUB
                                          MATN
        THET
                                         MAIN
                                                                                                       MAIN 146
        TOTINT
                                                                                                       MĀIN 147
                             SUB
                                         NAMPDE
                                                                                                      MAIN 148
        UPTRT
                             SUB
                                         TOT INT
        USEAS
                             SÚB
                                                                                                       MAIN 149
                                          TOTINT
        WIDEN
                             SUB
                                          TABLE
                                                                                                       MAIN 150
                                                                                                       MAIN 151
                                                                                                      MAIN 152
                          ----INPUTS THROUGH NAMELIST READ STATEMENTS----
                                                                                                      MAIN 153
                                                                                                      MAEN 154
  NAM1 -- NAMELIST GROUP 1
                                                                                                      MAIN 155
                        #FLAG DENOTING POINT IN MAIN PROGRAM AT WHICH COMPUTA-
TION BEGINS. POSSIBLE VALUES OF 1 THROUGH 5 CAUSE
NAM2. NAM3. NAM5. NAM7. OR NAM9 TO BE READ. NSTART#6
CAUSES TERMINATION OF PROGRAM EXECUTION.
        NSTART
                                                                                                      MAIN 156
                                                                                                      MAIN 157
                                                                                                      MAIN 158
                                                                                                      MAIN 159
                          FLAG FOR PRINTING OPTION. IF NPRNT .LE. O. A MINIMAL AMOUNT OF PRINTOUT WILL BE RETURNED.
        NPRNT
                         *FLAG FOR PRINTING OPTION.
                                                                                                      MAIN 160
                                                                                                      MAIN 161
        NPNCH
                         FLAG FOR PUNCHING OPTION.
                                                               IF NPNCH .LE. O. NO INFO
                                                                                                      MAIN 162
                          WILL BE PUNCHED ON CARDS.
                                                                                                      MAIN 163
                                                                                                      MAIN 164
  NAM2 -- NAMFLIST GROUP 2
                                                                                                      MAIN 165
                                                                                                      MAIN 166
                        SINTEGER WHICH SPECIFIES WHICH TYPE OF ATMOSPHERIC DAT IS INPUT. IF LANGEL .LE. O. THE WIND COMPONENTS IN KNOTS_ARE SPECIFIED, WHILE IF LANGE .GT. O. THE WIND
        LANGLE
                                                                                                      MAIN 167
                                                                                                      MAIN 168
                                                                                                      MAIN 169
                          MAGNITUDE AND DIRECTION ARE SPECIFIED FOR EACH LAYER.
                                                                                                      HAIN 170
        MAX
                         NUMBER OF LAYERS OF FINITE THICKNESS IN MULTILAYER
                                                                                                      MAIN 171
                          ATMOSPHERE
                                                                                                      MAIN 172
                        =TEMPERATURE IN DEGREES KELVIN IN THE I-TH LAYER.
=X (MEST TO EAST) COMPONENT OF WIND VELOCITY IN I-TH
        T(I)
                                                                                                      MAIN 173
        VKNTX(I)
                                                                                                      MATN
                                                                                                      MAIN
                            (SOUTH TO NORTH) COMPONENT OF WIND VELOCITY IN 1-TH
        VKNTY(I)
                                                                                                      MAIN 176
                                                                                                      MAIN 177
                         =WIND VELOCITY MAGNITUDE IN KNOTS IN I-TH LAYER.
**WIND VELOCITY DIRECTION IN DEGREES. RECKONED COUNTER
        WINDY(I)
                                                                                                      MAIN
                                                                                                             178
        WANGLE(1)
                                                                                                      MAIN
                          CLOCKWISE FROM X-AXIS.
                                                                                                      MAIN
                         *HEIGHT IN KILOMETERS OF THE TOP OF THE I-TH LAYER OF
        71(1)
                                                                                                      MATN 181
                          FINITE THICKNESS.
                                                                                                      MAIN 182
                                                                                                      MAIN 183
  NAM3 -- NAMELIST GROUP 3
                                                                                                      MAIN 185
                         =NUMBER OF LAYERS OF FINITE THICKNESS.
Ċ.
        TMAY
                                                                                                      MAIN 186
                         "SOUND SPEED IN KM/SEC IN IT-TH LAYER.
"X COMPONENT OF WIND VELOCITY IN I-TH LAYER (KM/SEC).
"Y COMPONENT OF WIND VELOCITY IN I-TH LAYER (KM/SEC).
                                                                                                      MAIN 187
        CI(I)
        AX 1 (1)
                                                                                                      MATN 188
                                                                                                      MAIN 189
                         =THICKNESS IN KM OF 1-TH LAYER OF FINITE THICKNESS.
        HILLS
                                                                                                      MAIN 190
                                                                                                      MAIN 191
C NAM4 -- NAMELIST GROUP 4
                                                                                                             192
                                                                                                      MAIN
                                                                                                      MAIN 193
        THETKO
                         #DIRECTION IN DEGREES TO OBSERVER. RECKONED COUNTER
                                                                                                      MAIN 194
                         CLOCKWISE FROM X AXIS.

=LOWER BOUND IN KM/SEC OF PHASE VELOCITY INTERVAL CON-
SIDERED FOR NORMAL MODE TABULATION
                                                                                                      MAIN 195
                                                                                                      MAIN 196
        ٧ı
                         =UPPER BOUND IN KM/SEC OF PHASE VELOCITY INTERVAL CON-
SIDERED FOR NORMAL MODE TABULATION
=MINIMUM ANGULAR FREQUENCY IN RAD/SEC CONSIDERED FOR
        ٧2
                                                                                                      MAIN 198
                                                                                                      MAIN 199
        OMI
                                                                                                      MAIN 200
                          NORMAL MODE TABULATION.
                                                                                                      MAIN
                         *MAXIMUM ANGULAR FREQUENCY IN RAD/SEC CONSIDERED FOR
        042
                                                                                                      MAIN 202
                         NORMAL MODE TABULATION. ... INITIAL NUMBER OF DISCRETE FREQUENCIES BETWEEN OM1
                                                                                                      MAIN 203
        NOMI
                                                                                                      MAIN 204
                           AND OM2. INCLUSIVE. AT WHICH NORMAL MODE DISPERSION
                                                                                                      MAIN 205
                                                                                                            206
                          FUNCTION IS STUDIED.
                                                                                                      MAIN
                                                                                                                    PROGRAM
                         =INITIAL NUMBER OF DISCRETE PHASE VELOCITIES BETWEEN V1 AND V2. INCLUSIVE, AT WHICH NORMAL MODE DISPERSION FUNCTION IS STUDIED.
        NVPI
                                                                                                      MAIN 207
                                                                                                                      MAIN
                                                                                                      MAIN 208
                                                                                                      MAIN 209
                                                                                                                        PAGE
        GOMKAH
                         *MAXIMUM NUMBER OF MODES TO BE TABULATED.
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ورجوا المجالية المجالة المتحادود -

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MAIN 211
                                                                                                                                                                   MAIN 212
    MAMS -- NAMELIST GROUP S
                                       =NUMBER OF LAYERS OF FINITE THICKNESS
=SOUND SPEED IN KM/SEC IN I-TH LAYER
=X COMPONENT OF WIND VELOCITY IN I-TH LAYER (KM/SEC)
=Y COMPONENT OF WIND VELOCITY IN I-TH LAYER (KM/SEC)
             IMAX
                                                                                                                                                                   MAIN 214
             CILLI
                                                                                                                                                                   MAIN 215
                                                                                                                                                                  MAIN 216
C.
             (1)1XV
(1)1YV
                                                                                                                                                                   MAIN 217
                                       THICKNESS IN KM OF I-TH LAYER OF FINITE THICKNESS DIRECTION IN DEGREES TO OBSERVER, RECKONED COUNTER
                                                                                                                                                                   MAIN 218
             THETKO
                                                                                                                                                                   MAIN 219
                                        CLOCKWISE FROM X AXIS =NUMBER OF NORMAL MODES FOUND
                                                                                                                                                                   MAIN 220
             NDFND
                                                                                                                                                                   MAIN 221
                                       =INDEX OF FIRST TABULATED POINT IN N-TH MODE
=INDEX OF LAST TABULATED POINT IN N-TH MODE.
             KSTINI
                                                                                                                                                                   MAIN 222
             KFININI
                                                                                                                                                                   MAIN 223
                                          GENERAL, KFIN(N)=KST(N+13-1.
                                                                                                                                                                   MAIN 224
                                       GENERAL, KFININ)=KST(N+1)-1.

=ARRAY STORING ANGULAR FREQUENCY ORDINATE (RAD/SEC) OF POINTS ON DISPERSION CURVES. THE NMODE MODE IS STORE FOR N BETWEEN KST(NMODE) AND KFIN(NMODE).

=ARRAY STORING PHASE VELOCITY ORDINATE (KM/SEC) OF POINTS ON DISPERSION CURVES. THE NMODE MODE IS STORE FOR H BETWEEN KST(MMODE) AND KFIN(NMODE).
             OMMODINE
                                                                                                                                                                  MAIN 225
                                                                                                                                                                   MAIN 227
             VPMODENT
                                                                                                                                                                   MAIN 228
                                                                                                                                                                  MAIN 229
                                                                                                                                                                   MAIN 230
    NAMS -- NAMELIST GROUP 6
                                                                                                                                                                   MAIN 232
                                                                                                                                                                   MAIN 233
                                       *HEIGHT IN KM OF BURST ABOVE GROUND
*HEIGHT IN KM OF OBSERVER ABOVE GROUND
              ZSCRCF
              ZOBS
                                                                                                                                                                   MAIN 236
    NAM7 -- NAMELIST GROUP 7
                                                                                                                                                                  MAIN
                                                                                                                                                                            237
                                                                                                                                                                   MAIN 238
                                       =ARRAY STORING ANGULAR FREQUENCY ORDINATE (RAD/SEC) OF POINTS ON DISPERSION CURVES. THE NHODE MODE IS STORE FOR N BETWEEN KST(NMODE) AND KFIN(NMODE).
=ARRAY STORING FHASE VELOCITY ORDINATE (KM/SEC) OF
              DMMOD (N)
                                                                                                                                                                  MAIN 240
                                                                                                                                                                  MAIN
                                                                                                                                                                            241
                                                                                                                                                                            242
             VPMOD(N)
                                                                                                                                                                   MAIN
                                          POINTS ON DISPERSION CURVES.
                                                                                                          THE NHODE MODE IS STORE
                                       POINTS ON DISPERSION CURVES. THE NMODE MODI
FOR N BETWEEN KST(NMODE) AND KFIN(NMODE)
***NUMBER OF NORMAL MODES FOUND
***INDEX OF FIRST TABULATED POINT IN N-TH MODE.
***INDEX OF LAST TABULATED POINT IN N-TH MODE.
                                                                                                                                                                  MAIN 244
                                                                                                                                                                  MAIN 245
C
              MOEND
                                                                                                                                                                            246
                                                                                                                                                                  MAIN
CCC
              KSTINY
              KFIN(N)
                                       GENERAL, KFIN(N)=KST(N+1)-1.

#AMPLITUDE FACTOR FOR GUIDED WAVE EXCITED BY POINT ENERGY SOURCE. UNITS ARE KM++(-1). THE J-TH ELEMENT CORRESPONDS TO ANGULAR FREQUENCY OMMOD(J) AND PHASE VELOCITY VPMOD(J). THE AMPLITUDE FACTOR IS APPROPRIATO THE NMODE-TH MODE IF J .GE. KST(NMODE) AND J .LE.
                                                                                                                                                                  MATN
                                                                                                                                                                            248
                                                                                                                                                                  MAIN 249
              AMP(J)
                                                                                                                                                                  MAIN 251
                                                                                                                                                                  MAIN
                                                                                                                                                                            252
                                                                                                                                                                  MAIN
 C
                                           KFININMODEL. A DETAILED DEFINITION OF AMPIJ) IS GIVE
                                                                                                                                                                  MAIN
                                        IN THE LISTING OF SUBROUTINE NAMPDE.

-A SCALING FACTOR DEPENDENT ON HEIGHT OF BURST, EQUAL TO CUBE ROOT OF IPRESSURE AT GROUND)/(PRESSURE AT BURST HEIGHT) TIMES (SOUND SPEED AT GROUND)/(SOUND DEED AT GROUND)/(SOUND)
                                                                                                                                                                  MAIN 255
              ALAM
                                                                                                                                                                  MAIN 256
                                                                                                                                                                  MAIN
                                                                                                                                                                            257
                                        SPEED AT BURST HEIGHTI. SEE SUBROUTINE PAMPDE. =A GENERAL AMPLITUDE FACTOR DEPENDENT ON BURST HEIGHT AND OBSERVER HEIGHT. A PRECISE DEFINITION IS GIVEN
                                                                                                                                                                  MAIN 259
              FACT
                                                                                                                                                                  MAIN 260
                                                                                                                                                                  MAIN
                                          IN THE LISTING OF SUBROUTINE PAMPDE.
                                                                                                                                                                  MAIN 262
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     NAMS -- NAMELIST GROUP S
                                                                                                                                                                            265
                                                                                                                                                                  MAIN
                                        -ENERGY YIELD OF EXPLOSION IN EQUIVALENT KILOTONS (KT)
                                                                                                                                                                  MAIN 266
              YTELD
                                          OF THT. 1 KT = 4.2X(10)++19 ERGS.
                                                                                                                                                                  MAIN 267
                                                                                                                                                                  MAIN 268
     NAM9 -- NAMELIST GROUP 9
                                                                                                                                                                  MAIN 269
                                                                                                                                                                  MATN 270
                                       =NUMBER OF NORMAL MODES FOUND
=INDEX OF FIRST TABULATED POINT IN N-TH MODE
=INDEX OF LAST TABULATED POINT IN N-TH MODE. IN
GENERAL, KFIN(N)=KST(N+1)-1
=ARRAY STORING ANGULAR FREQUENCY ORDINATE (RAD/SEC) OF
POINTS ON DISPERSION CURVES. THE NMODE MODE IS STORE
FOR N BETHEEN KST(NMODE) AND KFIN(NMODE).
=ARRAY STORING PHASE VELOCITY ORDINATE (KM/SEC) OF
POINTS ON DISPERSION CURVES. THE NMODE MODE IS STORE
FOR N BETWEEN KST(NMODE) AND KFIN(NMODE).
                                                                                                                                                                  MAIN
              HDFNO
              KST(N)
              KF IN(N)
                                                                                                                                                                  MAIN 273
                                                                                                                                                                  MAIN 274
                                                                                                                                                                  MAIN 275
              DMMOD (N)
                                                                                                                                                                                        PROGRAM
                                                                                                                                                                 MAIN 277
MAIN 278
                                                                                                                                                                                            MAIN
              VPMOD (N)
                                                                                                                                                                                              PAGE
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#AMPLITUDE FACTOR REPRESENTING TOTAL MAGNITUDE OF FOURIER TRANSFORM OF MAYEFORM CONTRIBUTION OF SINGLE GUIDED MODE AT FREQUENCY OMNOD(N). IT REPRESENTS THE AMPLITUDE OF MMODE-TH MODE IF N IS BETWEEN KST(NMODE) AND KFININMODE). INCLUSIVE. FOR PRECISE DEFINITION. SEE SURROUTINE PRAMP.
                                                                                                                                      MAIN 281
          AMPLTD(N)
                                                                                                                                      MAIN 282
                                                                                                                                      MAIN 283
                                                                                                                                      MAIN 284
                                                                                                                                      MAIN 285
HAIN 286
                                PHASE LAG AT FREQUENCY OMMOD(N) FOR NMODE MODE WHEN N BETWEEN KST(NMODE) AND KFIN(NMODE). RESPECTIVELY. THE INTEGRAND IS UNDERSTOOD TO HAVE THE FORM AMPLTO+COS(OMMOD+ITIME-DISTANCE/VPMOD)+PHASQ). FOR
          PHASO(N)
                                                                                                                                       MAIN 287
                                                                                                                                      MAIN 288
                                                                                                                                      MAIN 289
                                                                                                                                      MAIN 290
                                  PRECISE DEFINITION OF PHASO. SEE SURROUTINES THAT
                                                                                                                                      MAIN 291
                                                                                                                                      MAIN 292
                                                                                                                                      HAIN 293
   NAMIO -- NAMELIST GROUP 10
                                                                                                                                      MAIN 294
                                                                                                                                      HAIN 295
                                                                                                                                      MAIN
          TFIRST
                                =FIRST TIME RELATIVE TO TIME OF DETONATION FOR WHICH
                                #FIRST TIME RELATIVE TO TIME OF DETONATION FOR WHICH WAVEFORM IS COMPUTED. UNITS ARE IN SECONDS.
#APPROXIMATE TIME VALUE CORRESPONDING TO LAST POINT TABULATED FOR WAVEFORM (RELATIVE TO TIME OF DETONATIO FOR PRECISE DEFINITION, SEE SUBROUTINE TMPT.
#INCPEMENT OF TIME VALUES IN SECONDS FOR WHICH SUCCESSIVE WAVEFORM POINTS ARE TABULATED.
#MAGNITUDE OF HORIZONTAL DISTANCE IN KM BETWEEN SOURCE
                                                                                                                                      MAIN 297
          TEND
                                                                                                                                      MAIN 298
                                                                                                                                      MAIN
                                                                                                                                              299
                                                                                                                                      MAIN 300
                                                                                                                                      MATH 301
          DFLTT
                                                                                                                                      MAIN
                                                                                                                                              302
          RORS
                                                                                                                                      MAIN
                                                                                                                                              303
                                  AND OBSERVER.
                                                                                                                                      MAIN
                                                                                                                                              304
          TOPT
                                 -INTEGER CONTROLLING WHICH MODES ARE INCLUDED IN THE
                                                                                                                                      MAIN
                                                                                                                                              305
                                  COMPUTED WAVEFORM. FOR PRECISE DEFINITION. SEE SUBROUTINE TMPT.
                                                                                                                                      MAIN 306
                                                                                                                                      MAIN 307
                                                                                                                                      MAIN 308
                                                                                                                                      MAIN 309
                                  ---- PROGRAM FOLLOWS BELOWS ----
                                                                                                                                      MAIN 310
                                                                                                                                      MAIN
                                                                                                                                              311
                                                                                                                                      MAIN
                                                                                                                                      MAIN
          DIMENSION CI(100).VXI(100).VYI(100).HI(100).AMP(1000).AMPLTD(1000)
DIMENSION T(100).VKNTX(100).VKNTY(100).ZI(100).PHASQ(1000)
DIMENSION WANGLE(100).HINDY(100)
DIMENSION OM(100).VP(100).INMODE(10000)
                                                                                                                                      MATH 314
                                                                                                                                      MAIN
                                                                                                                                      MAIN
                                                                                                                                      MAIN 317
           DIMENSION KST(10).KFIN(10).OMMOD:1000).VPMOD(1000)
                                                                                                                                      MAIN 318
                                                                                                                                      MAIN
                                                                                                                                              319
C ALOCATION OF VARIABLES TO COMMON STORAGE
           COMMON IMAX.CI.VXI.VYI.HI
                                                                                                                                      MAIN 321
                                                                                                                                      MATH 322
                                                                                                                                              323
C NAMELIST STATEMENTS
                                                                                                                                      MAIN
          NAMELIST /NAMI/ NSTART.NPRRT,NPNCH
NAMELIST /NAMI/ NSTART.NPRRT,NPNCH
NAMELIST /NAMI/ LANGLE.IMAX.T.VKNTX.VKNTY.MINDY.WANGLE.ZI
NAMELIST /NAMI/ IMAX.CI.VXI.VYI.HI
NAMELIST /NAMI/ THETKD.VI.VZ.OMI.OMZ.NCMI.NVPI.MAXMOD
NAMELIST /NAMI/ IMAX.CI.VXI.VYI.HI.THETKD.MDFND.KST.KFIN.OMMOD.
                                                                                                                                      MAIN
                                                                                                                                      MAIN 325
                                                                                                                                     MAIN
                                                                                                                                              326
                                                                                                                                      MAIN
                                                                                                                                      MAIN
         1 VPMOD
                                                                                                                                     MAIN 329
           NAMFLIST /NAM6/ ZSCRCE.ZGBS
NAMELIST /NAM7/ OMMOD.VPMOD.MDFND.KST.KFIN.AMP.ALAM.FACT
                                                                                                                                      MAIN 330
           NAMELIST /NAME/ YIELD
NAMELIST /NAME/ HOFNO-KST-KFIN-OMMOD. VPMOD. AMPLTD. PHASQ
                                                                                                                                      MAIN
                                                                                                                                              332
                                                                                                                                      MATN
                                                                                                                                              333
           NAMELIST /NAMIO/ TFIRST.TEND.DELTT.ROBS.IOPT
                                                                                                                                      MAIN
                                                                                                                                      MAIN 336
   BEFORE ANY DATA IS READ IN. ALL NAMELIST VALUES ARE PRESET TO ZERO. THIS IS DONE SIMPLY TO MAKE NAMELIST PRINTOUT EASIER TO READ.
                                                                                                                                     MAIN
                                                                                                                                              337
                                                                                                                                      MAIN
           NSTART=0
                                                                                                                                      MAIN 339
           MORNTEO
                                                                                                                                     MATN
                                                                                                                                              340
           NPNCH=0
                                                                                                                                      MAIN 341
                                                                                                                                      MAIN 342
           LANGLE=0
           IMAX=0
                                                                                                                                     MAIN 343
                                                                                                                                     MAIN 344
           THETKD=0.0
           V1=0.0
           V?=0.0
                                                                                                                                     MAIN 346
                                                                                                                                                       PROGRAM
           OM1=0.0
                                                                                                                                     MAIN 347
                                                                                                                                                           MAIN
                                                                                                                                     MAIN 348
           0M2c0.0
                                                                                                                                     MAIN
           NOMI=0
                                                                                                                                                             PAGE
           NVPI=0
                                                                                                                                     MAIN 350
```

- -----

```
MAXMOD=0
MOFND=0
ZSCRCF=0.0
                                                                                                           MAIN 351
                                                                                                           MAIN 352
HAIN 353
         2085=0.0
                                                                                                           MAIN 354
        ALAM=0.0
FACT=0.0
                                                                                                           MAIN 355
                                                                                                           HAIN 356
         VIFLD=0.0
                                                                                                           MAIN 357
MAIN 358
         TEIRST=0.0
                                                                                                           MAIN 359
         DFLTT=0.0
                                                                                                           MAIN 360
         RG95=0.0
                                                                                                           MAIN 361
MAIN 362
         IDPT=0
         00 21 tpm=1.100
CT(TPR)=0.0
                                                                                                           MAIN 363
         VXIIIPRI=0.0
                                                                                                           MAIN 365
                                                                                                          MAIN 366
MAIN 367
         VY1( IPP)=0.0
         HT(TPR)=0.0
         Tf[PR]=0.0
        VKNTX ( IPR )=0.0
                                                                                                           MAIN 369
         VKNTY ( IPR)=0.0
                                                                                                           MAIN 370
         Z1([PR)=0.0
                                                                                                           MAIN
                                                                                                                 371
         WANGLE ( IPF )=0.0
                                                                                                           MAIN 372
         WINDY(IPP)=0.0
                                                                                                           HAIN 373
        OM(IPR)=0.0
                                                                                                          MAIN 374
MAIN 375
    PI VPIIPRI=0.0
        no 31 [PP=1.10
KST([PR)=0
                                                                                                           MAIN 377
    31 KFIN(IPR)=0
                                                                                                          MAIN 378
         DO 41 100-1.1000
                                                                                                          MAIN 379
         AMPLIPRI-0.0
                                                                                                          HAIN 380
         AMPLTD(IPR)=0.0
PHASQ(IPR)=0.0
OMMOD(IPR)=0.0
                                                                                                           MAIN 381
                                                                                                           MAIN 382
                                                                                                          MATH 383
    41 VPMOD(IPP)=0.0
                                                                                                          MAIN 334
C
                                                                                                           MAIN 385
                                                                                                           MAIN 386
   STAFF OF EXECUTABLE PORTION OF PROGRAM
                                                                                                          HAIN 367
                                                                                                          MAIN 388
C NEWPLT IS A CALCOMP SUBROUTINE WHICH INITIATES THE CALCOMP PLOTTER
C TAPE FILE. 4640 IS THE M.I.Y. COMPUTATION CENTER PROBLEM NO. 5923 IS
C THE PROGRAMMER NO. GRAPH PAPER WITH BLACK INK IS REQUESTED.
CALL NEWPLT(*M5640*,*5923*,*WHITE *,*BLACK *)
                                                                                                          MAIN 389
                                                                                                          MAIN 390
                                                                                                          MAIN 391
                                                                                                          MAIN 392
                                                                                                          MAIN 393
MAIN 394
     1 READ (5. NAM1)
                                                                                                          MAIN 395
C IT IS CONSIDERED GOOD PRACTICE TO HAVE INPUT DATA PRINTED ON OUTPUT
                                                                                                          HAIN 396
        WRITE (6.37)
FORMAT(IH //// 27HINAM1 HAS JUST REEN READ IN)
                                                                                                          MAIN 397
                                                                                                          MAIN 398
                                                                                                           MAIN 399
                                                                                                          HAIN 400
HAIN 401
C CURPENT VALUE OF NSTART CONTROLS THE STAGE AT WHICH COMPUTATION BEGINS C SINCE COMPUTED GO TO STATEMENTS SOMETIMES OD NOT COMPILE CORRECTLY IF C INDEX IS NOT EXPLICITLY DEFINED. WE PLAY IT SAFE WITH REDUNDANT
                                                                                                          MAIN 402
MAIN 403
  STATEMENT.
                                                                                                          MAIN 404
         NSTART=NSTART
                                                                                                          MAIN 405
                                                                                                          MAIN 406
C
         GD TO (200+300+400+500+600+999)+NSTART
                                                                                                          HAIN 407
                                                                                                          MAIN 408
MAIN 409
C WE ARRIVE HERE IF NSTAPT=1
   200 READ (5.NAM2)
                                                                                                          MAIN 410
                                                                                                          MAIN 411
  WRITE (6,737)
737 FORMAT(1H //// 27H NAM2 HAS JUST BEEN READ IN)
                                                                                                          MAIN 412
                                                                                                          MAIN 413
                                                                                                          MAIN 414
MAIN 415
MAIN 416
MAIN 427
         WPITE (4.NAMZ)
C CONVERT ATMOSPHERIC DATA TO STANDARD FORM
                                                                                                                        PROGRAM
         CALL ATMOSIT. VKNTX. VKNTY. ZI. WANGLE. WINDY . LANGLE?
                                                                                                                           MATN
                                                                                                          MAIH 418
MAIN 419
MAIN 420
         IF( NPRNT .LE. 0) GO TO 270
                                                                                                                             PAGE
  PPINT ATMOSPHERIC PROFILE IF MPRNT .GT. O
```

```
MAIN 421
       CALL PRATHO
                                                                                                       MAIN 422
  270 IF( NPNCH .LE. 0) GO TO 305
                                                                                                       MAIN 423
                                                                                                       MAIN 424
MAIN 425
C PUNCH NAME DATA IF NPNCH .GT. O
  PUNCH NAME GRIM IF NAME = 01 · U

WRITE (7.271)

271 FOPMAT ( 7H ENAME)

IUHS = TMAX + 1

WRITE (7.272) IMAX.(CI(T).I=1.IUHS)

272 FORMAT ( 10H IMAX = .I3.1H. / 8H C

1 ( 6X.G15.8.1H...G15.8.1H...G15.8.1H...G15.8.1H...)
                                                                                                       MAIN 426
                                                                                                       MAIN 427
                                                                                                       MAIN 478
                                                                                                       MAIN 429
                                                                  # 8H CT = /
                                                                                                       MAIN 430
                                                                                                       MAIN 431
  MAIN 432
                                                                                                       MAIN 433
                                                                                                       MAIN 434
MAIN 435
                                                                                                       MAIN 436
                                                                                                       MAIN 437
                                                                                                       HAIN 438
                                                                                                       MAIN 439
MAIN 440
        WRITE (7,279)
                                                                                                       MAIN 441
  279 FORMAT ( 6H &END )
WRITE (6.583)
WRITE (6.271)
WRITE (6.272) IMAX.(CI(!).[=1.IUHS)
                                                                                                       MAIN 442
MAIN 443
                                                                                                       MAIN 444
                                                                                                       MAIN 445
        WRITE(6.274) (VXI(1).1=1.1UHS)
WRITE(6.276) (VYI(1).1=1.1UHS)
WRITE(6.278) ( HI(1).1=1.1UHS)
                                                                                                       MAIN 446
                                                                                                       MAIN 447
                                                                                                       MAIN 448
  WRITE (5-279)
280 GO TO 305
                                                                                                       MAIN 449
                                                                                                       MATH 450
                                                                                                       MAIN 451
C WE APRIVE HERE IF NSTART=2
                                                                                                       MAIN 452
   300 READ (5.NAM3)
   WPITE (6,302)
302 FORMAT(14 //// 27H NAM3 HAS JUST REFN READ IN)
                                                                                                       MAIN 454
                                                                                                       MAIN 455
WRITE (6.NAM3)
IF( NPRYT .LE. 0) GO TO 305
C PRINT ATMOSPHERIC PPCFILE IF NPRNT .GT. 0
                                                                                                       MAIN 456
                                                                                                       MAIN 457
                                                                                                       MAIN 458
                                                                                                       MAIN 459
        CALL PRATMO
                                                                                                       MAIN 460
C CONTINUING FROM 270. 280. 302. OR 303
   305 READ (5.NAM4)
WRITE (6.307)
                                                                                                       MAIN 462
MAIN 463
   307 FORMAT(1H //// 27H NAM4 HAS JUST BEEN READ IN)
                                                                                                       MAIN 464
        WRITE (6. NAM4)
                                                                                                       MAIN 465
C CONVERT THETKO FROM DEGREES TO RADIANS
THETK = (3-14159) = THETKD / 180-0
                                                                                                       MAIN 466
                                                                                                       MAIN 467
                                                                                                       MAIN 468
        IMON = MON
IQVN = QV
                                                                                                       MAIN 469
                                                                                                       MATN 470
                                                                                                       MAIN 471
MAIN 472
C CONSTRUCT TABLE OF INMODE VALUES
        CALL TARLETON: . DM2.V1.V2.NOM.NVP.THETK.OM.VP.INMODE.NPRNT)
                                                                                                       MAIN 473
                                                                                                       MAIN 474
C COMPUTE DISPERSION CURVES OF GUIDED MODES
                                                                                                       MAIN 475
        CALL ALLMODINVP.NOM. MAXMOD. MDFND. OM. VP. KST. KFIN. OMMOD. VPMOD.
                                                                                                       MAIN 476
       1 INMODE. THETK.KHOP)
                                                                                                       MAIN 477
MAIN 478
C CHECK TO SEE IF ANY MODES WERE FOUND IF( KNOP .GF. 0) GO TO 320
                                                                                                       MAIN 480
                                                                                                       MAIN 481
C FXIT IF KWOP .LT. O
WRITE (6.311) KWCP
311 FORMAT(1H . 5HKWOP=. I3)
                                                                                                       MAIN 482
                                                                                                       MAIN 483
                                                                                                       MAIN 484
MAIN 485
        CALL FXIT
                                                                                                       MAIN 486
                                                                                                                    PROGRAM
C CONTINUING WITH KWOP .GE. O FROM 308
320 IF( NPRNT .LF. 0) GO TO 350
                                                                                                      MAIN 487
MAIN 488
                                                                                                                       MAIN
                                                                                                       MAIN 489
                                                                                                                         PAGE
C PRINT MORMAL MODE DISPERSION CURVES
                                                                                                       MAIN 490
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三方 学生经历研究 人名霍

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بالمحمولات أأرابه أحلو

1

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CALL NODEST(HOFNO, OMMOD, VPMOD, KST. KFIN)
                                                                                                                        MAIN 491
                                                                                                                       MAIN 492
MAIN 493
C CONTINUING FROM 320 OF 321
   350 IFE NPNCH .LE. O) GO TO 360
                                                                                                                        MAIN 494
C PUNCH NAME DATA IF NENCH .GT. O
                                                                                                                        MAIN 496
   WRITE (7.351)
351 FORMAT ( 7H CNAM5 )
1UHS = IMAX + 1
WRITE (7.272) IMAX.(CI(I).I=1.IUHS)
                                                                                                                       MAIN 497
MAIN 498
                                                                                                                        MAIN 499
   MRITE (7.272) IMAX.(CI(I).I=1.I(IMS)

WRITE(7.274) (VX[[I].I=1.IUMS)

WRITE(7.276) (VYI(I).I=1.IUMS)

WRITE(7.278) ( HI(I).I=1.IUMS)

MRITE (7.278) ( HI(I).I=1.IUMS)

MRITE (7.278) ( HI(I).I=1.IUMS)

MRITE (7.278) ( HI(I).I=1.IUMS)

1 (6X.G15.8.IM..G15.8.IM..G15.8.IM..G15.8.IM..G15.8.IM.)

WRITE(7.355) (KFIN(I).I=1.MDFND)

355 FORMAT (10M KFIN = /
                                                                                                                        MAIN 501
                                                                                                                       MAIN 502
MAIN 503
                                                                                                                        MAIN 504
                                                                                                                       MAIN 505
                                                                                                                        MAIN 506
                                                                                                                        MAIN 507
                                                                                                                        MAIN 508
   MAIN 509
                                                                                                                        MAIN 510
                                                                                                                        MAIN 511
                                                                                                                        MAIN 512
                                                                                                                        MAIN 514
                                                                                                                       MAIN 515
            f 6x.G15.8.1H..G15.8.1H..G15.8.1H..G15.8.1H. ) }
                                                                                                                        MAIN 516
          WRITE (7,279)
WRITE (6,583)
                                                                                                                        MAIN 517
                                                                                                                        MAIN 518
          WRITE (6.537)
WRITE (4.272) IMAX.(CI(I).I=1.IUHS)
WRITE (4.272) IMAX.(CI(I).I=1.IUHS)
WRITE(6.274) (VXI(I).I=1.IUHS)
WRITE(6.276) (VYI(I).I=1.IUHS)
WRITE(6.278) (HI(I).I=1.IUHS)
WRITE (6.352) THETKD.MDFND.(KST(I).I=1.MDFND)
WRITE (6.357) (KFIN(I).I=1.MDFND)
WRITE (6.357) (OMMOD(I).I=1.KLAST)
WRITE (6.279)
                                                                                                                        MAIN 519
                                                                                                                        MAIN 520
                                                                                                                        MAIN 521
                                                                                                                        MAIN 522
                                                                                                                       MAIN 523
MAIN 524
                                                                                                                        MAIN 525
                                                                                                                        MAIN 526
                                                                                                                        MAIN 527
                                                                                                                        MAIN 528
          WRITE (6.279)
                                                                                                                        MAIN 529
   CONTINUING FROM 350 CR 351
                                                                                                                        MAIN 530
    360 GO TO 415
                                                                                                                        MAIN 531
                                                                                                                        MAIN 532
                                                                                                                        MAIN 533
   WF ARRIVE HFRE IF NSTART=3
                                                                                                                        MAIN 534
    400 READ (5.NAM5)
WRITE (6.403)
403 FORMAT(1H //// 27H NAM5 HAS JUST BEEN READ IN)
                                                                                                                        MAIN 535
                                                                                                                        MAIN 536
                                                                                                                        MAIN
          WRITE (6. NAMS)
                                                                                                                        MAIN 538
                                                                                                                        MAIN 539
                                                                                                                        MAIN 540
 C CONVERT THETKO FROM DEGREES TO RADIANS
          THETK = (3.14159) + THETKD / 180.0
                                                                                                                        HAIN 541
                                                                                                                       MAIN 542
MAIN 1543
 C CONTINUING FROM 360 OR 402
                                                                                                                       MAIN 544
MAIN 545
    415 READ (5.NAM6)
WRITE (6.417)
    417 FORMAT(1H //// 27H NAM6 HAS JUST BEEN READ IN)
                                                                                                                        MATH SAA
                                                                                                                       MAIN 547
          WRITE (6.NAM6)
                                                                                                                        MAIN 548
   COMPUTE VIELD INDEPENDENT AMPLITUDE FACTORS FOR GUIDED MODES CALL PAMPDE(ZSCRCE.ZOBS.MDFND.KST.KFIN.OMMOD.VPMOD.AMP.ALAM.FACT.
                                                                                                                        HAIN 549
                                                                                                                       MAIN 550
                                                                                                                        MAIN 551
         1 THETK. NPRNT)
                                                                                                                        MAIN 552
 C
    450 IF( NPNCH .LF. 0) GO TO 460
                                                                                                                        MAIN 553
                                                                                                                       MAIN 554
C PHINCH NAME DATA IF MANCH .GT. 0
                                                                                                                        MAIN 555
    KLAST = KFIN(MDFND)

WRITE (7-451)(AMP(I), I=1.KLAST)

451 FORMAT ( 7H ENAMY / 9H AMP = /
1 ( 6x-G15.8-1H-.G15.8-1H-.G15.8-1H-) )

WRITE (7-452) ALAM-FACT
                                                                                                                        MAIN 556
                                                                                                                                       PROGRAM
                                                                                                                       MAIN 557
                                                                                                                                          MAIN
                                                                                                                        MAIN 558
                                                                                                                                            PAGE
                                                                                                                        MAIN 560
```

ngang nagang dan sa sa

```
452 FORMAT ( 10H
                              ALAM = ,G16.8,1H. / 10H FACT = ,G16.8,1H. )
                                                                                                              MAIN 561
   MRITE (7.455) HDFND. (KST(I).I=1.MDFND)
455 FDRMAT (
                                                                                                              MAIN 562
MAIN 563
                                                                  MDFND =+13+1H+/8H KST =/
        HAIN 564
                                                                                                              HAIN 565
                                                                                                              MAIN 566
                                                                                                              HAIN 567
                                                                                                              MAIN 568
                                                                                                              MAIN 569
MAIN 570
                                                                                                              MAIN 571
MAIN 572
         WRITE(6.355) (KFIN(1).1=1.MDFND)
WRITE(6.357) (OMMOD(1).1=1.KLAST)
                                                                                                              MAIN 573
         WRITE (6.357) (OMMOD(I).I=1.KLAS
WRITE(6.359) (VPMOD(I).I=1.KLAST)
                                                                                                              MAIN 574
                                                                                                              MAIN 575
   459 WRITE (6.279)
                                                                                                              MAIN 576
                                                                                                              MAIN 577
C CONTINUING FROM 450 CR 459
460 GO TO 515
                                                                                                              MAIN 578
MAIN 579
                                                                                                              MAIN 580
C
                                                                                                              MAIN 581
C WE ARRIVE HERE IF NSTART=4
                                                                                                              MAIN 582
   500 READ (5.NAM7)
WRITE (6.501)
                                                                                                              MAIN 583
                                                                                                              MAIN 584
   501 FORMAT(1H //// 27H NAM7 HAS JUST BEEN READ IN) 502 WRITE (6.NAM7)
                                                                                                             MAIN 585
MAIN 586
                                                                                                              MAIN 587
C CONTINUING FROM 460 CR 502
                                                                                                              MAIN 588
   515 READ (5.NAMB)
WRITE (6.516)
                                                                                                              MAIN 589
                                                                                                              MAIN 590
   516 FORMAT! IH //// 27H NAMB HAS JUST BEEN READ IN)
                                                                                                              MAIN 591
   517 WRITE (G.NAMS)
                                                                                                              MAIN 592
                                                                                                              MAIN 593
C COMPUTE VIELD DEPENDENT AMPLITUDES AND PHASE TERMS OF GUIDED MODES
                                                                                                              MAIN 594
         CALL PPAMPITIELD, MDFND, KST, KFIN, OMMOD, VPMOD, AMP, ALAM, FACT, AMPLTD.
                                                                                                              MAIN 595
       1 PHASO)
                                                                                                              MAIN 596
518 IF ( NPRNT .LE. 0 ) GO TO 580
C THE RESULTS OF CALLING PPAMP ARE PRINTED OUT BY CALLING TABPRT
                                                                                                              MAIN 597
   520 CALL TABPRT(YIELD, MOFND, KST, KFIN, OMMOD, VPML, AMPLTD, PHASQ)
                                                                                                             MAIN 599
                                                                                                             MAIN 600
   CONTINUING FROM 518 OR 520
                                                                                                             MAIN 601
   580 IF( NPNCH .LE. 0) GO TO 590
                                                                                                             MAIN 603
  PUNCH NAM9 DATA IF NPNCH .GT. 0

KLAST = KFINIMDEND)

WRITE (7.581) (AMPLTD[]),I=1,KLAST)

581 FORMAT ( 7H ENAM9 / 12H AMPLTD = /

1 ( 6X.G15.8.1H.,G15.8.1H.,G15.8.1H.,G15.8.1H.) )

WRITE (7.582) (PHASO(I),I=1.KLAST)

582 FORMAT ( 11H PHASO = /

1 ( 6X.G15.8.1H.,G15.8.1H.,G15.6.1H.,G15.8.1H.) )

WRITE (7.455) MDFND,(KST(I),I=1,MDFND)

WRITE (7.355) (KFIN(I),I=1,MDFND)

WRITE (7.357) (OMMOD(I),I=1.KLAST)

WRITE (7.359) (VPMOD(I),I=1.KLAST)

WRITE (7.279)
C PUNCH NAMS DATA IF NPNCH .GT. 0
                                                                                                             MAIN 604
                                                                                                              MAIN 605
                                                                                                             MAIN 606
                                                                                                             MAIN 607
                                                                                                             MAIN 608
                                                                                                             MAIN 609
                                                                                                             MAIN 610
                                                                                                             MAIN 611
                                                                                                             MAIN 613
                                                                                                             MAIN 614
MAIN 615
         WRITE (7,279)
WRITE (6,583)
                                                                                                             MAIN 616
                                                                                                             MAIN 617
                                                                                                             MAIN 618
         FORMATI 1H //// 41H THE FOLLOWING DATA HAS JUST BEEN PUNCHED)
         VRITE (6.581) (AMPLTD(I).I=1.KLAST)
WRITE (6.582) (PHASQ(I).I=1.KLAST)
WRITE (6.455) MDFND.(KST(I).I=1.MDFND)
                                                                                                             MAIN 619
                                                                                                             MAIN 620
                                                                                                             MAIN 621
         WRITE(6.355) (KFIN(!)+1=1.MDFND)
WRITE (6.357) (CMMOD(!)+1=1.KLAST)
WRITE(6.359) (VPMOD(!)+1=1.KLAST)
                                                                                                             MAIN 623
                                                                                                             MAIN 624
                                                                                                             MAIN 625
   584 WRITE (6,279)
                                                                                                             MAIN 626
                                                                                                                            PROGRAM
  CONTINUING FROM 560 CR 584
                                                                                                             MAIN 627
C
                                                                                                                               MAIN
   590 GO TO 615
                                                                                                             MAIN 628
                                                                                                             MAIN 629
                                                                                                                                PAGE
                                                                                                             DEA NIAM
```

PROGRAM MAIN

```
AAAA (SUBROUTINE)
                                                      7/25/68
                                                                                                  AAAA
                         ----ARSTRACT----
                                                                                                  AAAA
                                                                                                  AAAA
                                                                                                  AAAA
  TITLE - AAAA
           THIS SUBROUTINE COMPUTES THE 2-BY-2 MATRIX A OF COEFFICIENTS
                                                                                                  AAAA
C.
           IN THE RESIDUAL FOUATIONS
                                                                                                  AAAA
                 D(PHI1)/DZ = (A11)*PHI1 + (A12)*PHI2
                                                                                                  AAAA
                 D(PHI2)/DZ = (A21)*PHI1 + (A22)*PHI2
                                                                                                  11
                                                                                                  AAAA
C
           DFRIVED BY A. PIERCE. J. COMP. PHYS.. VOL. 1. NO. 3. 343, -366. 1967. (SEE EQN. (10) OF THE PAPER.) THE EXPLICIT EXPRESSIONS FOR THE A(1.J) ARE
                                                                                                  AAAA
                                                                                                  AAAA
                                                                                                         14
C
                                                                                                  ....
                                                                                                  AAAA
                 A(1+1) = G*(K/R(M)**2 - GAMMA*G/(2*C**2)
                                                                                                  AAAA
                A(1.2) = 1 - (C+K/80M)=+2
A(2.1) =((G*K)/(80M+C))++2 - (80M/C)++2
                                                                                                  AAAA
C
                                                                                                  AAAA
                 A(2.2) = -A(1.1)
                                                                                                  AAAA
                                                                                                         20
                                                                                                  AAAA
           WHERE GAMMA=1.4 IS THE SPECIFIC HEAT RATIO, G=.0098 KM/SEC##2 IS THE ACCELERATION OF GRAVITY, C IS THE SOUND SPFED. K IS THE HORIZONTAL WAVE NUMBER AND BOM IS THE DOPPLER SHIFTED ANGULAR
                                                                                                  AAAA
C.
                                                                                                  AAAA
                                                                                                         23
                                                                                                 AAAA
                                                                                                 AAAA
           FREQUENCY
                                                                                                  26
                - FORTRAN IV (360. REFERENCE MANUAL C28-6515-4)
- A.D.PIERCE. M.I.T., JULY, 1968
C LANGUAGE
                                                                                                 C AUTHOR
                                                                                                 AAAA
                                                                                                         28
                                                                                                 AAAA
                        ---- CALLING SEQUENCE----
                                                                                                 AAAA
                                                                                                 SEE SUBROUTINES ELINT. MMMM. NAMPDE. NMDFN
                                                                                                 AAAA
                                                                                                 AAAA
       DIMENSION A(2.2)
       CALL AAAA(OMEGA.AKX.AKY.C.VX.VY.A)
                                                                                                 AAAA
                                                                                                 35
  NO EXTERNAL SUBROUTINES ARE REQUIRED
                                                                                                 AAAA
                                                                                                         36
                                                                                                  AAAA
                        ----ARGUMENT LIST----
                                                                                                 38
                                                                                                 AAAA
       OMEGA
                                                                                                 AAAA
       AKX
                     R#4
                               ND
                                       INP
                                                                                                 AAAA
                    R#4
        AKY
                               ND
                                       TNP
                                                                                                 AAAA
                     R#4
                               ND
                                       INP
                               NO
        ٧x
                     R#4
                                       INP
       VY
                     R#4
                               NO
                                       IND
                                                                                                 R#4
                              2-8Y-2 OUT
                                                                                                 AAAA
  NO COMMON STORAGE IS USED
                                                                                                 AAAA
                                                                                                 AAAA
                        ----INPUTS----
                                                                                                 AAAA
                                                                                                         90
                                                                                                 AAAA
                       #ANGULAR FREQUENCY IN RAD/SEC

#X COMPONENT OF HORIZONTAL WAVE NUMBER VECTOR IN 1/KM

#Y COMPONENT OF HORIZONTAL WAVE NUMBER VECTOR IN 1/KM
       OMEGA
                                                                                                 AGAA
        AKX
                                                                                                 AAAA
       AKY
                                                                                                 AAAA
                       =SOUND SPEED IN KM/SEC
=X COMPONENT OF WIND VELOCITY IN KM/SEC
=Y COMPONENT OF WIND VELOCITY IN KM/SEC
       ٧x
                                                                                                 AAAA
C
                                                                                                 ----OUTPUTS----
                                                                                                 AAAA
                                                                                                 AAAA
                                                                                                        60
                       *(I.J)-TH ELEMENT OF HATRIX A OF COEFFICIESTS IN THE
       A(T.J)
                                                                                                 AAAA
                        PESIDUAL EQUATIONS AS DEFINED IN THE ABSTRACT.
                                                                                                 AAAA
                        ----PROGRAM FOLLOWS BELOW
                                                                                                 AAAA
C
                                                                                                 ***
        SUBROUTINE AAAA(OMEGA,AKX,AKY,C,VX,VY,A)
                                                                                                 ....
                                                                                                              PR(IGNAH
r
                                                                                                 4444
4444
                                                                                                        67
                                                                                                                 ....
       DIMENSION A(2+2)
                                                                                                        4.6
       BONSO= (OMEGA-AKX+VX-AKY+VY)++2
                                                                                                                  PAGE
       CSQ=C*C
                                                                                                 AAAA
```

T=(AKX=*7+AKY==7)*ROMSG AAAA 71
Af1-11=.009R*T-.00686/CSQ AAAA 72
C CAMMA*G2 IS .00686
Af1-21=1.0-CSQ*T AAAA 73
Af1-21=1.0-CSQ*T AAAA 75
C G**2 IS 96.04E-6)*T-ROMSO)/CSQ AAAA 75
RETURN AAAA 76
FND AAAA 79

PROGRAM AAAA

AND THE RESIDENCE OF THE PROPERTY OF THE PROPE

The state of the s

```
AKI (SURROUTINE)
                                                    8/15/68
                                                                                               AKI
                                                                                               AK T
                         ----ABSTRACT-- -
                                                                                               AKI
                                                                                               AKI
  TITLE - AKI
           EVALUATION OF INTEGRAL OF A OMEGA) + COS(PHILOMEGA)) FROM ONL TO
                                                                                               AKI
           240
                                                                                               ARI
AKI
C
                  A(CMEGA) AND PHI(OMEGA) ARE ASSUMED TO BE LINEAR BETWEEN OM1 AND OM2, FOLLOWING THE METHOD OF AKI ( J. GEOPHYS. RES., VOL. 65 (1960), Pp. 729-740 ). THE INTEGRAL IS READILY EVALUATED AS
C
                                                                                               AKI
                                                                                               AKI
                                                                                               AKI
C
                                                                                               AKI
                                                                                               AKI
                     (PHI*)**(-1) * (AI + A**(OM2-DM1)) * SIN(PHI!*X)
                                                                                               AKĪ
                                                                                                     15
                                                                                               AK I
                                                                                                     16
17
                         + PHI***(-2) * A* * COS(PHII + X)
                                                                                               AKI
                         - PHI^***(-1) * (AI - A* * (OM2 - OM1)) * SIN(PHII-X)
                                                                                               AKI
                                                                                                     19
                                                                                                     20
21
c
                                                                                               AKI
                         - PHI***(-2) * A* * COS(PHI - X)
                                                                                               AKI
                                                                                               AKI
                   WHERE
                                                                                               AKI
AKI
                                                                                                     23
                                                                                               AKI
                         AT = AVERAGE VALUE OF A IN INTERVAL
                         AT = AVERAGE VALUE OF AT IN INTERVAL

A' = O(A) / D(OMEGA)

PHI' = D(PHI) / D(OMEGA)

X = PHI' + (OM2 - O41) / 2
                                                                                               AKI
                                                                                               AKI
                                                                                               AKI
                                                                                                     28
                                                                                               AKI
                                                                                               AKI
                   A SOMEWHAT MORE CONVENIENT FORMULA OBTAINABLE BY TRIGONO-METRIC IDENTITIES IS
                                                                                               AKI
                                                                                                     31
                                                                                               AKI
                                                                                                     32
33
                                                                                               ALI
                                                                                                     34
35
36
                     AKIINT = 2 + PHI***(-1) + AI + SIN(X) + COS(PHII)
                                                                                               AKI
                                                                                               AKI
                                 + 2 * PHI***(-2) * A* * (X * COS(X) - SIN(X))
                                                                                               AKI
                                                                                               AK I
                                   * SIN(PHII)
                                                                                               AKT
                                                                                                     39
40
                                                                                               AKI
                   WHENEVER X IS SMALL. SIN(X)/X AND COS(X) ARE EVALUATED BY
                                                                                               AKI
                   USING THEIR POWER SERIES REPRESENTATIONS.
                                                                                               AKI
                                                                                              AK I
                                                                                                     42
43
  LANGUAGE
                - FORTRAN IV (360, REFERENCE MANUAL C28-6515-4)
                                                                                               AKI
                - A.D.PIERCE AND J.POSFY, M.I.T., AUGUST,1968
  AUTHORS
                                                                                               AK I
                                                                                                     46
                                                                                              AKI
                                                                                               AKT
                                                                                                     48
                         ----USAGF----
                                                                                               AKİ
                                                                                              AK I
       NO SUBROUTINES APP CALLED
                                                                                                     50
                                                                                                     51
52
                                                                                               AKI
  FORTRAN USAGE
                                                                                              AKI
AKI
                                                                                                     53
54
55
       CALL AKI (OM1.0M2.41.A2.CTRIGI.STRIGI.CTRIG2.STRIG2.
                                                                                               AKI
         DELPH.AKTINT)
                                                                                               AK I
                                                                                               AKE
                                                                                                     56
57
58
  INPUTS
                                                                                               AKI
                                                                                              AK I
                   LOWER LIMIT OF INTEGRATION OVER ANGULAR FREQUENCY
C
      CHI
                                                                                              AK I
                                                                                                     59
ć
         R#4
                   (RADIANS)
                                                                                                     60
                                                                                              AK I
                   UPPER LIMIT OF INTEGRATION (RADIANS)
                                                                                              AKI
C
      OM2
                                                                                                     62
                                                                                                     63
64
                                                                                              AKI
                   VALUE OF A AT OMEGA = OM1
                                                                                              AKI
                                                                                              AK I
                                                                                                     66
                                                                                                          PROGRAM
                                                                                              AKT
                                                                                                     67
      A?
R#4
                                                                                                             AKI
                   VALUE OF A AT OMEGA * OM2
                                                                                              AKI
                                                                                                     68
69
Ç
                                                                                              AKI
                                                                                                             PAGE
                                                                                                     70
                                                                                                                13
```

mer in from it with metalogical and the second of the seco

-217-

```
CTRIGI
                       COS(PHI) WHERE ONEGA = ONI
                                                                                                                       AKI
0000
                                                                                                                              71
72
73
74
75
76
77
78
79
          R#4
                                                                                                                       AKT
                                                                                                                       AKI
        STRIGE
                        SIN(PRI) WHERE OMFGA = OM1
                                                                                                                       AKI
2000
                                                                                                                       AKI
       DELPH
R*4
                        CHANGE IN PHI OVER THE INTERVAL ( PHICOM2) - PHICOM1) )
                                                                                                                       AKI
AKI
AKI
                        (RADIANS)
C OUTPUTS
                                                                                                                       AKI
                                                                                                                              81
82
93
                                                                                                                       AKI
        CTRIGZ
                       COS(PHI) WHERE OMEGA = 042
10011001000
          R#4
                                                                                                                       AKI
                                                                                                                              84
85
                                                                                                                       AKI
        STRIG?
                       SINIPHI | WHERE ONEGA = OM2
                                                                                                                       AKI
                                                                                                                              86
87
          R#4
                                                                                                                       AKI
                                                                                                                       AK I
        AKIINE
                        VALUE OF INTEGRAL DEFINED IN ABSTRACT IN UNITS OF A*OMEGA
                                                                                                                              88
                                                                                                                       AKI
                                                                                                                       AKI
                                                                                                                       AKI
                                                                                                                              91
92
                               ----PROGRAM FOLLOWS BELOW----
C
                                                                                                                       AKI
                                                                                                                      AKI
        SUBROUTINE AKI(OM1.OM2.A1.A2.CTRIG1.STRIG1.CTRIG2.1 STEEG.DELPH.AKIINT)
                                                                                                                              95
96
                                                                                                                       AKI
         DELOM=ON2-OM1
                                                                                                                       AKI
                                                                                                                              97
         DELAA=A2-A1
                                                                                                                      AKI
AKI
                                                                                                                              98
r
         AI=(A2>41)/7.0
X=D&LPH/2.0
                                                                                                                       AKT 100
                                                                                                                      AKI 101
AKI 102
AKI 103
         CTRX=COS(X)
          STRX=SIN(X)
         CTRIGI=CTRIGI=CTRX-STRIGI=STRX
STRIGI=STRIG1=CTRX+CTRIGI=STRX
                                                                                                                      AKI 104
AKI 105
AKI 106
         CTR102=CTR161+CTRX-STR161+STRX
STR162=STR161+CTRX+CTR161+STRX
IF(ABS(X)-1-UF-2) 20-20-10
                                                                                                                      AKI 106
AKI 107
AKI 108
AKI 109
AKI 110
AKI 111
AKI 112
AKI 113
AKI 114
AKI 115
AKI 116
     10 S1=STRX/X
         S2=(S1-CTRX)/X++2
GO TO 30
     2C S1=1.0-(1.0/6.0)*x**2+(1.0/120.0)*x**4

S2=(1.0/3.0)-(1.0/30.0)*x**2+(1.0/840.0)*x**4

3O AKIINT=(AI*S1*CTRIGI-DELAA*DELPH*0.25*S2*STRIGI)*DELOM
         RETURN
          END
```

. . .

PROGRAM AKI PAGE

and a supplication of the section of

```
ALLMOD (SUBROUTINE)
                                                                                 6/25/63
                                                                                                                                                      ALLM
                                                                                                                                                      ALLM
                                                                                                                                                      ALL#
TITLE - ALLHOD
                                                                                                                                                      ALLM
               PPOGRAM TO TAMILATE DISPERSION CURVES OF UP TO MAXMOD GUIDED
                                                                                                                                                      ALLM
              PPOGRAM TO TARJEATE DISPERSION CURVES OF UP TO MAXMOD GUIDED MODES. ONLY PORTIONS OF CURVES WITH OMEGA BETWEEN ON(1) AND OM(NCOL) AND WITH PHASE VELOCITY BETWEEN VP(NCOL) AND VP(1) ARE TABULATED. THE ANGULAR DEVIATION OF GROUP VELOCITY DIRECTION FROM PHASE VELOCITY DIRECTION THETK IS NEGLECTED. SUCCESSIVE MODES NUMBERED FROM 1 TO MORND ARE EACH TABULATED BY CALLING SUBROUTINE MODETR. STARTING POINTS FOR EACH MODE ARE FOIND BY CALLING SUBROUTINE NXMODE. THE NORMAL MODE DISPERSION FUNCTION (MNDF) SHOULD BE NEARLY ZERO FOR EVERY TABULATED POINT ON EACH DISPERSION CHROSS.
                                                                                                                                                      ALLM
                                                                                                                                                      ALLM
                                                                                                                                                      ALLM
                                                                                                                                                      ALLH
                                                                                                                                                      ALLM
                                                                                                                                                     ALL M
                                                                                                                                                     ALLH
              ON EACH CISPERSION CUPVE. THE COMPUTATIONAL METHOD IS BASEC ON THE PREVIOUSLY COMPUTED VALUES OF THE NMOF SIGN INMODE((J-1)*NROW+1) AT POINTS (I.J) IN A RECTANGULAR ARRAY OF
                                                                                                                                                      ALLM
                                                                                                                                                                 14
                                                                                                                                                     ALLM
                                                                                                                                                                 16
17
               HROW ROWS AND NCOL COLUMNS.
                                                                         DIFFERENT COLUMNS (J) CORRESPOND
                                                                                                                                                     ALLM
              TO DIFFERENT ANGULAR FREQUENCIES OM(J) WHILE DIFFERENT ROWS (I) CORRESPOND TO DIFFERENT PHASE VELOCITIES VP(I). IT IS ASSUMED THAT VP(I). GT. VP(2). GT. VP(2). ETC. DISPERSION CURVES OF VARIOUS MODES APPEAR ON THIS ARRAY AS LINES OF DEMARCATION RETWEEN ADJACENT REGIONS WITH OPPOSITE INMODES. IT IS ASSUMED
                                                                                                                                                     ALLM
                                                                                                                                                                  19
                                                                                                                                                     ALLM
                                                                                                                                                                 20
                                                                                                                                                     ALLM
               THAT DISPERSION CURVES SLOPE DOWNMARDS.
STARTING FROM LOWER LEFT OF INMODE ARRAY.
                                                                                                  MODES ARE NUMBERED
                                                                                                                                                     ALLM
                                                                                                                                                                 23
                                                                                                                                                     ALLM
                                                                                                                                                                 24
                                                                                                                                                     ALLH
PROGRAM NOTES
                                                                                                                                                                 26
                                                                                                                                                     ALLM
                                                                                                                                                                 27
                           THE ARRAYS OMMOD AND VPMOD ARE USED TO STORE DISPERSION
                                                                                                                                                     ALLM
                          CURVES FOR ALL THE MODES TO CONSERVE STORAGE. FOR THE NMODE-TH MODE, VPMOD(KST(NMODE)+K-1) IS THE PHASE VELOCIT CORRESPONDING TO ANGULAR FREQUENCY OF OMMOD(KST(NMODE)+K-1). THE PAIR OF VALUES CORRESPONDS TO THE K-TH TABULAT
                                                                                                                                                     ALLM
                                                                                                                                                                 30
                                                                                                                                                     ALLM
                                                                                                                                                                 31
                          POINT FOR THE MODE. THE LAST TABULATED POINT FOR THE MMODE-TH MODE IS LABELED BY THE PAIR VPMOD(KFIN(MMODE)), OMMOD(KFIN(NMODE)). THUS OMMOD(K), VPMOD(K) FOR K.GE. KST(NMODE) AND K.LT. KFIN(NMODE) DESCRIBE THE NMODE-TH MODE-S DISPERSION CURVE.
                                                                                                                                                     ALLM
                                                                                                                                                     ALLM
                                                                                                                                                     ALLM
                                                                                                                                                     ALLM
                                                                                                                                                                 37
                                                                                                                                                     ALLM
                                                                                                                                                                 38
                           THE FLAG KWOP IS NORMALLY RETURNED AS 1. HOWEVER, IF NO DISPERSION CURVES ARE TABULATED, KWOP IS RETURNED AS
                                                                                                                                                     ALLM
                                                                                                                                                                 40
                                                                                                                                                     ALLM
                      - FORTRAN IV (360, REFERENCE MANUAL C28-6515-4)
- A.D.PIFRCE, M. I.T., JUNE, 1968
LANGUAGE
                                                                                                                                                     ALLM
AUTHOR
                                                                                                                                                     AL I M
                                                                                                                                                     ALLH
                                   ----CALLING SEQUENCE----
                                                                                                                                                                 46
                                                                                                                                                     ALLM
SFF MAIN PROGRAM
                                                                                                                                                     ALLM
        DIMENSION OM(100).VP(100).KST(10).KFIN(10).DMMOD(1000).VPMOD(1000)
DIMENSION INMODE( 000)
DIMENSION CI(100).VXI(100).VYI(100).HI(100)
                                                                                                                                                     ALLM
                                                                                                                                                                 50
                                                                                                                                                     At t M
THE SUBROUTINE USES VARIABLE DIMENSIONING. THE ASSIGNMENTS ABOVE ARE THOSE GIVEN BY MAIN PROGRAM
                                                                                                                                                     ALLM
COMMON THAX.CI.VXI.VYI.HI
ATMOSPHERIC VARIABLES MUST BE IN COMMON BEFORE ALLMOD IS CALLED.
CALL ALLMODINPOW.NCOL.MAXHOD.MDFND.OM.VP.KST.KFIN.OMMOD.VP.COD.
                                                                                                                                                     ALL M
                                                                                                                                                     ALLM
                                                                                                                                                     ALLM
          INMODE. THETK . KUCP
         IFIKWOP .NE. 11 GO SOMEWHERF
                                                                                                                                                     ALLM
                                                                                                                                                     ALLM
                                   ---- EXTERNAL SURROUTINES REQUIRED----
                                                                                                                                                     ALLM
                                                                                                                                                                 60
                                                                                                                                                     ALLM
                                                                                                                                                                 61
         NXMODE.MODETR.NXTPNT.RTMI.FNMODI.FNMOD2.NMDFN.AAAA.RRRR.MMMM.CAI.S
                                                                                                                                                     ALLM
                 NXMODE AND NODETE ARE EXPLICITLY CALLED. THE REST ARE
                                                                                                                                                     ALLH
                 IMPLITITLY CALLED BY CALLING MODETR. FOR FURTHER INFORMATIO ON 18-1 SCIENTIFIC SUBPOUTINE PACKAGE POUTINE KTMI. SEE DOCU-
                                                                                               FOR FURTHER INFORMATION
                                                                                                                                                     ALLM
                                                                                                                                                                 66
                                                                                                                                                                         PROGRAM
                  MENTATION OF MODETR.
                                                                                                                                                     ALLM
                                                                                                                                                                67
                                                                                                                                                                             ALLMOD
                           ---- ARGUMENT LIST----
                                                                                                                                                                               PAGE
                                                                                                                                                     ALLM
                                                                                                                                                                 69
```

ALLM

15

```
NROW
                                                            INP
                                                HD
                                                                                                                                                   ALLM
            MCGE
MAXMOD
                                  194
                                                             INP
                                                ND
                                                            INP
                                                                                                                                                   ALLM
                                                                                                                                                              73
            MOFNO
                                  1+4
                                                            OUT
                                                                                                                                                   ALLM
                                                                                                                                                              74
75
                                                ND
            nn
                                  R#4
C
                                                                                                                                                              7f
77
                                  2 *4
            VP
                                                VAR
                                                            INP
                                                                                                                                                   ALLM
                                                           OUT
            KST
                                  1#4
                                                VAR
                                                                                                                                                   ALL"
                                                                                                                                                   ALL4
            KFIN
                                   1*4
                                                            OUT
            THINGS
                                  ...
                                                VAR
                                                            OUT
                                                                                                                                                   ALLM
                                                                                                                                                              70
                                                VAR
            VPMOD
                                  R*4
                                                                                                                                                   ALLM
ALLM
                                                            OUT
                                                                                                                                                              80
             ENMODE
                                  1#4
                                                YAR
                                                            INP
                                                            INP
            THETK
                                  R#4
                                                ND
                                                                                                                                                              92
                                  1 *4
            KWOP
                                                           OUT
                                                NI
                                                                                                                                                   ALL*
                                                                                                                                                              83
                                                                                                                                                   ALLM
                                                                                                                                                              84
   COMMON STORAGE USED
                                                                                                                                                              85
            COMMON IMAX.CI.VXI.VYI.HI.OMEGAC.VPHSEC.THETKP
                                                                                                                                                   ALL M
                                                                                                                                                              86
                                                                                                                                                   ALLM
                                                                                                                                                              97
                                  1*4
                                                            INP
            IMAX
                                                NO
            CI
                                  P#4
                                                100
                                                            INP
                                                                                                                                                   ALLM
                                                                                                                                                              89
            VXI
                                  R #4
                                                100
                                                            INP
                                                                                                                                                   ALLM
                                                                                                                                                              90
            VYI
                                  ...
                                                100
                                                            INP
            41
                                  R#4
                                                                                                                                                              92
93
                                                100
                                                            INP
                                                                                                                                                   ALLM
            DMEGAC
                                  RAL
                                                            OUT (USED INTERNALLY)
                                                ND
                                                                                                                                                  ALLM
            VPHSFC
                                  9 44
                                                ND
                                                            BUT (USED INTERNALLY)
                                                                                                                                                              94
            THETKP
                                  R#4
                                                NO
                                                            OUT (USED INTERNALLY)
                                                                                                                                                  ALLM
                                                                                                                                                              95
                                                                                                                                                   ALLM
                                                                                                                                                              96
                                      ----INPUTS----
                                                                                                                                                              97
                                                                                                                                                              98
99
                                                                                                                                                  ALLM
            NRTH
                                    *NUMBER OF ROWS IN INMODE ARRAY. MAXIMUM INDEX OF
                                                                                                                                                   ALLM
                                                                                                                                                           100
                                    =NUMBER OF COLUMNS IN INMODE ARRAY. MAXIMUM INDEX OF
            NCOL
                                                                                                                                                  ALLM
                                                                                                                                                           101
                                                                                                                                                  ALLM 102
                                      DM(N).
                                    MAXIMUM NUMBER OF MODES TO BE TABULATED

**ANGULAR FREQUENCY OF N-TH COLUMN IN INMODE ARRAY

**PHASE VELOCITY OF N-TH ROW IN INMODE ARRAY

**1.-1. OR 5 DEPENDING ON WHETHER SIGN OF NORMAL MODE

DISPESSION FUNCTION IS + OR -, 5 IF NMDF DOESNT EXIST

THE (J-1)**NROW-I-TH ELEMENT CORRESPONDS TO NMDF WHEN
            MAXMOD
            OMENS
                                                                                                                                                  ALL#
                                                                                                                                                           104
             VP(N)
                                                                                                                                                  ALLM 105
             INMODE
                                                                                                                                                  ALLM 107
                                                                                                                                                  ALLM
                                                                                                                                                           108
                                   THE (J-1)*NROW+I-TH ELEMENT CORRESPONDS TO NMOF WHEN CHEGA=OM(J). PHASE VELOCITY=VP(I).

=PHASE VELOCITY DIRECTION IN RADIANS RECKONED COUNTERCLOCKWISE WITH RESPECT TO X AXIS.

=NUMBER OF ATMOSPHERIC LAYERS OF FINITE THICKNESS

=SOUND SPFED IN I-TH LAYER

=X COMPONENT OF WIND VELOCITY IN I-TH LAYER

=Y COMPONENT OF WIND VELOCITY IN I-TH LAYER

=THICKNESS OF I-TH LAYER
                                                                                                                                                   ALLH 109
            THETK
                                                                                                                                                  ALLM
                                                                                                                                                           110
                                                                                                                                                  ALLH
            THAY
                                                                                                                                                  ALLM 112
C
            CILLI
                                                                                                                                                  ALLM
             AXIIII
                                                                                                                                                  ALLM
                                                                                                                                                  ALLM 115
ALLM 116
            VYIII
            HILLI
                                                                                                                                                   ALLM
                                      ---- OUT PUT S----
¢
                                                                                                                                                  ALLM 118
                                                                                                                                                  ALLM
                                   "NUMBER OF MODES FOUND

INDEX OF FIRST TABULATED POINT IN N-TH MODE

INDEX OF LAST TABULATED POINT IN N-TH MODE.

GENERAL, KFIN(N)=KST(N+1)-1.

**ARRAY STORING ANGULAR FREQUENCY ORDINATE OF POINTS
ON DISPERSION CURVES. THE NMODE MODE IS STORED FOR
N BETWEEN KST(NMODE) AND KFIN(NMODE).

**ARRAY STOPING PHASE VELOCITY ORDINATE OF POINTS ON
DISPERSION CURVES. THE NMODE-TH MODE IS STORED FOR
N BETWEEN KST(NMODE) AND KFIN(NMODE).

**-1 IF NO MODES ARE TABULATED. OTHERWISE IT IS 1.

**INTERNALLY USED FREQUENCY TRANSMITTED AMONG SUBROUTIN
THROUGH COMMON
            MDFND
            KSTINI
                                                                                                                                                  ALLM 121
                                                                                                                                                  ALLM
                                                                                                                                                           122
            KF IN(N)
            OMMODENE
                                                                                                                                                  ALLM 124
                                                                                                                                                  ALLM
            VPMOD(N)
                                                                                                                                                           127
                                                                                                                                                 ALLM 129
ALLM 130
            KWOP
            OMEGAC
                                      THROUGH CCHMON
                                                                                                                                                  ALLM 132
                                    INTERNALLY USED PHASE VELOCITY TRANSMITTED AMONG SUBBRUTINES THROUGH COMMON
                                                                                                                                                  ALLH
            VPHSEC
                                                                                                                                                  ALLH
                                                                                                                                                           134
                                                                                                                                                  ALLH
            THETEP
                                    -SAME AS THETK
                                                                                                                                                 ALLM 136
ALLM 137
                                                                                                                                                                     PROGRAM
                                     ----EXAMPLE----
                                                                                                                                                                         ALLHOD
                                                                                                                                                  ALLH 138
             SUPPOSE THE TABLE OF INHODE VALUES IS AS SHOWN BELOW WITH
                                                                                                                                                                           PAGE
                                                                                                                                                  ALLM 140
                                                                                                                                                                               16
```

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marketing of the second and an analysis of the second

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+++--+
                                 NROW=6. NCGL=10
                                                                                                       ALLM 141
c
            +++---++--
                                                                                                      ALLH 142
ALLH 143
             ****---*
                                IF MAXMOD=10. YOU SHOULD FIND MDFND=6.
                                                                                                      ALLH 144
             544-44444
                                                                     OMMOD(1-36)
                                                                                       SHOULD BE
                                                                                                      ALLH 145
                                                KFIN(2)=10
KFIN(3)=21
                                 KST(7)=5
KST(3)=11
                                                                                                      ALLM 146
ALLM 147
c
c
            5++-++++
                                                                     VPMOD(1-36)
                                                                                       TABULATED
                                                KFIN(4)=29
                                                                                                      ALLH 148
                                 KST(51=30
                                                KFIN(5)=34
                                                                                                      ALLH 149
C.
                                                                                                      ALLM
                                                                                                             150
                                 XST(6)=35
                                                KFIN(6)=36
                                                                                                      ALLH 151
                                                                                                      ALLM 152
                          ---- PROGRAM FOLLOWS BELOW----
C
                                                                                                      ALLH 153
                                                                                                      ALLH 154
                                                                                                             155
C
        SUBROUTINE ALL MODINROW. NCOL. MAXMOD. MOFND. OM. VP. KST. KFIN. OMMOD.
                                                                                                      ALLM 156
         VPMOD. INMODE. THETK. KWCP)
                                                                                                      ALL4 157
                                                                                                      ALLM 158
ALLM 159
C
        DIMENSION C1(100).VX1(100).VY1(100).H1(100)
        DIMENSION OM(1).VP(1).KST(1).KFIN(1).OMMCD(1).VP OD(1).INMODE(1)
COMMON IMAX.CI.VXI.VVI.HI.OMEGAC.VPHSEC.THETKP
                                                                                                      ALLM 160
                                                                                                      ALLM 161
                                                                                                      ALLM 162
C STORE THETK IN COMMON
                                                                                                      ALLM 163
        THETKP=THETK
                                                                                                      ALLM 164
                                                                                                      ALLM
C AT THIS POINT. WE HAVEN-T FOUND ANY MODES
                                                                                                      ALLM 166
                                                                                                      ALLM 167
C TWE START SHARCH FOR FIRST MODE IN LOWER LEFT CORNER OF INMODE ARRAY. C WE SEEK A POINT WITH INMODE .NE. 5 WHERE THE NMDE EXISTS.
                                                                                                      ALLM 168
                                                                                                      ALLM 169
                                                                                                      ALLM 170
ALLM 171
        KST(NMODE)=1
                                                                                                      ALLM 172
        TST=NROW
                                                                                                      ALLM 173
ALLM 174
C THE SEARCH GOES TO THE RIGHT. IF WE DON-T FIND A POINT IN THE BOTTOM C POW. WE TRY THE (NROW-1)-TH ROW. ETC. AT STATEMENT 2 WE ARE STARTING C AT THE LEFT OF A GIVEN ROW.
                                                                                                      ALLM 175
                                                                                                      ALLM 176
ALLM 177
       JST=1
     3 IO=INMODE((JST-1)*NROW+IST)
IF(10 .NE. 5) GO TO 10
                                                                                                      ALLM 179
                                                                                                      ALLH 180
C IF JST IS NOT NCOL WE GO TO THE RIGHT.
IF(JST .FQ. NCOL) GO TO 5
                                                                                                      ALLM 182
ALLM 183
        JST=JST+1
                                                                                                      ALLM 185
ALLM 186
C AT THIS POINT WE HAVE EXHAUSTED AN ENTIPE ROW. WE GO TO THE NEXT C HIGHER ROW PROVIDED IST .NE. 1. IF IST IS 1. THE ENTIRE SET OF
                                                                                                      ALLM 187
                                                                                                      ALLM 188
ALLM 189
  INMODES ARE >.
      5 TF(IST .EQ. 1) GO TO 7
                                                                                                      ALLM 190
                                                                                                      ALLM 191
ALLM 192
ALLM 193
        GO TO 2
C
      7 WRITE (6.8)
                                                                                                      ALLM 194
ALLM 195
      8 FORMATILHO+51HTHE NORMAL MODE DISPERSION FUNCTION DOES NOT EXIST .
      1 26HFOR ANY POINT IN THE ARRAY / IH , 22HALLMOD RETURNS KWOP=-1) 9 KWOP=-1
                                                                                                      ALLM 196
                                                                                                      ALLM 197
ALLM 198
        RETURN
                                                                                                            198
                                                                                                      ALLM 199
C STATEMENT 10 IS START OF LOOP. EACH PASSAGE THROUGH LOOP CORRESPONDS
                                                                                                      ALLM 200
                                                                                                      ALLM 201
    10 CALL NXMODE(IST.JST.NCOL.NROW-INMODE.IFND.JFND.KEX)
                                                                                                      ALLH 202
ALLH 203
  IF YOU CANNOT FIND THE FIRST MODE YOU ARE IN TROUBLE IF (NMODE .NE. 1) GO TO 15 IF (KEX .FO. 1) GO TO 15
                                                                                                      ALLM 204
                                                                                                      ALLM 205
                                                                                                      ALLM 206
ALLM 207
                                                                                                                   PROGRAM
    WRITE (6.11)
11 FORMAT(1HO. 36HNXMODE COULD NOT FIND THE FIRST MODE/ 1H .
127HALLMOD RETURNS KWOP=-1)
                                                                                                                      ALLMOD
                                                                                                     ALLM 208
ALLM 209
                                                                                                                       PAGE
                                                                                                      ALL4
        60 TO 9
```

THE REPORT OF THE PERSON NAMED IN COLUMN 1

Segan 'ren 'adoler 'alleda

TO THE POST OF THE PROPERTY OF THE PARTY OF

```
ALLM 211
C IF THE MODE SOUGHT IS NOT THE FIRST AND YOU CANNOT FIND IT. THEN THE
                                                                                                                          ALLM 212
C RETURN IS CONSIDERED SATISFACTORY.
15 IF (KEX .EQ. -1) GO TO 50
                                                                                                                          ALLM 213
ALLM 214
                                                                                                                          ALL# 215
C WE NOW TABULATE THE NMODE-TH MODE
CALL MCDETR(IFND.JFND.NMODE.KST.KFIN.OMMCD.VPMOD.NROW.NCOL.INMODE.
1 OM.VP.KRUD)
                                                                                                                          ALLM 216
                                                                                                                          ALLM 217
                                                                                                                          ALLM 218
C IT IS DOUBFUL THAT KRUD COULD RE -1. HOWEVER. IF IT DID HAPPEN. WE CHOULD LIKE TO KNOW THAT IT DID.

IF(KRUD .FQ. 1) GO TO 30

WRITF (6.21) NHODE. IFMD. JFND

21 FORMAT(IHO. 23HMODETR RETURNS KRUD=-1...2X.25HCURRENT VALUE OF NHODE
                                                                                                                          ALLM 220
                                                                                                                          ALLM 221
                                                                                                                          ALL# 222
                                                                                                                          ALL# 223
                                                                                                                          ALLM 224
        1 IS+ I4+ 3H+ + 5HIFND=+ I4+3H+ + 5HJFND=+ I4/ 1H +27HSEE DOCUME
2NTATION OF ALLMOD)
                                                                                                                          ALLH 225
                                                                                                                          ALLM 226
ALLM 227
ALLM 228
C WE KEEP NMODE THE SAME AND TRANSFER CONTROL TO STATEMENT 35
     GO TO 35
30 MOFNO=MOFNO+1
                                                                                                                          ALLH 230
                                                                                                                          ALL4 231
C THIS IS THE CURRENT NUMBER OF MODES FOUND.

C WE NOW CHECK IF THIS IS MAXMOD. IF IT IS. THE RETURN IS WITH KWOP=1.

IF(MDFND .EQ. MAXMOD) GO TO 50

NMODE=NMODE+1
                                                                                                                          ALLH 232
                                                                                                                          ALLM 233
                                                                                                                           ALLM 234
                                                                                                                          ALLM 235
          KST(NMODF)=KFIN(NMODE-1)+1
                                                                                                                          ALLM 236
                                                                                                                          ALLH 237
C WE SEEK NEW IST AND JST BFFORE CALLING NXMODE.
35 IO=INMODF((JFND-1)=NROW+IFND)
IF(IFND .EQ. 1) GO TO 40
                                                                                                                          ALLM 238
                                                                                                                          ALL# 239
                                                                                                                          ALLM 240
                                                                                                                          ALLM 241
ALLM 242
C WE CHECK INMODE OF POINT ABOVE
           IUP=INMODE((JFN9-1)*NROW+IFND-1)
                                                                                                                          ALLH 243
                                                                                                                          ALLM 244
ALLM 245
C IF THIS IS -10. THE POINT ABOVE IS THE ONE DESIRED IF(IUP .NE. -10) GD TO 40
                                                                                                                          ALLM 246
           IST=IFND-1
JST=JFND
                                                                                                                          ALLH 247
ALLH 248
                                                                                                                          ALLM 249
ALLM-250
           GO TO 10
   WF CHECK INMODE OF POINT TO RIGHT. THERE IS NO PLACE TO GO INCOL. THIS IS INTERPRETED AS SUCCESS PROVIDING MOFND .NE. 0. 40 IF(JFND .NE. NCOL) GO TO 43 GO TO 50
                                                             THERE IS NO PLACE TO GO IF JFND=
                                                                                                                          ALLM 251
ALLM 252
ALLM 253
                                                                                                                          ALLM 255
ALLM 256
C IRT IS INNODE OF POINT TO RIGHT
43 IRT=INMODE((JEND)+NROH+IEND)
IF(IRT .NE. +10) GO TO 50
'ST=IEND
                                                                                                                          ALLH 257
                                                                                                                          ALLM 258
ALLM 259
           JST=JFND+1
                                                                                                                          ALLH 260
                                                                                                                          ALLM 261
ALLM 262
           GO TO 10 .
 THE SEARCH HAS TERMINATED. IF MOFND=0, WE HAVE BEEN UNSUCCESSFUL. 50 IF(MOFND .EQ. 0) GO TO 9
                                                                                                                          ALLH 263
                                                                                                                          ALLM 264
ALLM 265
           KWOP=1
                                                                                                                          ALLM 266
ALLM 267
           FND
```

PROGRAM ALLHOD

```
AMENT (SURROUTINE)
                                                                 7/27/68
                                                                                                                        AMBN
                                                                                                                        AMRN
                                                                                                                        AMBN
                            ----ARSTRACT----
                                                                                                                        AMBN
TITLE - AMENT
            THIS SUBROUTINE COMPUTES THE AMBIENT PRESSURE IN DYNES/CH**2 AT A GIVEN ALTITUDE 7 KM BY USE OF THE EQUATION
                                                                                                                        AMRN
                                                                                                                        AMBN
               PRESUR = (1.E6)*EXP(-INTEGRAL FROM 0 TO 7 OF GAMMA*G/C**2)
                                                                                                                        AMRN
                                                                                                                        AMRN
                                                                                                                                 10
            WHERE 1.66 DYNES/CM**2 IS THE AMBIENT PRESSURE AT THE GROUND. GAMMA=1.4 IS THE SPECIFIC HEAT RATIO FOR AIR, G=.0099 \lambdaM/SEC**2 IS THE ACCELEPATION OF GRAVITY. AND G IS THE ALTITUDE DEPENDENT SOUND SPEED IN KM/SEC. THE ABOVE EQUATION FOLLOWS FROM THE HYDROSTATIC EQUATION DIPOJ/DZ = -G*RHOO AND THE IDEAL GAS LAW
                                                                                                                        AMBN
                                                                                                                        AMBN
                                                                                                                        AMRM
                                                                                                                                 13
                                                                                                                        AMBN
                                                                                                                                 14
15
                                                                                                                        AMBN
            C##2 = GAMMA + PO/RHOO.
                                                                                                                        AMBN
                                                                                                                                 16
                                                                                                                        AMBN
                                                                                                                                 17
            THE SOUND SPEED PROFILE IS THAT OF A MULTILAYER ATMOSPHERE AND IS PRESUMED TO BE STORED IN COMMON BEFORE EXECUTION. THE PROGRAM ALSO RETURNS THE INDEX I OF THE LAYER IN WHICH 7 LIES.
                                                                                                                        AHBN
                                                                                                                        AMRN
                                                                                                                                 19
                                                                                                                        AMBN
                                                                                                                                 20
                                                                                                                        AMBN
                                                                                                                                 21
                                                                                                                        AMBN
PROGRAM NOTES
                                                                                                                        AMBN
                                                                                                                                 23
                      IN THE EVENT THAT THE INPUT VALUE OF 7 SHOULD BE NEGATIVE THE FIRST LAYER IS ASSUMED TO HOLD FOR 7 .LT. O WITH THE AMBIENT PRESSURE STILL EQUAL TO 1.F5 AT Z=0. THE PROGRAM
                                                                                                                       AMBN
                                                                                                                        AMBN
                                                                                                                                 26
27
                                                                                                                       AMBN
                                                                                                                        AMBN
                      RFTURNS PRESUR .GT. 1.E6 AND I=1.
                                                                                                                        AMBN
LANGUAGE
                  - FORTRAN IV (360, REFERENCE MANUAL C28-6515-4)
                                                                                                                        AMBN
                                                                                                                                 29
                                                                                                                        AMBN
AUTHOR
                  - A.D.PIERCE, M.I.T., JULY,1968
                                                                                                                                 30
                             ----CALLING SEQUENCE----
                                                                                                                        AMRN
                                                                                                                        AMBN
SEE SUBROUTINE PAMPHE
                                                                                                                        AMBN
       DIMENSION CI(100). VXI(100). VYI(100). HI(100)
                                                                                                                        AMBN
                                                                                                                                 35
       COMMON IMAX.CI.VXI.VYI.HI
CALL AMBNT(7.PRESUR.I)
                                                     (THESE MUST BE STORED IN COMMON)
                                                                                                                        AMBN
                                                                                                                                 36
                                                                                                                        AMBN
                                                                                                                        AMBN
                            ----EXTERNAL SUBROUTINES REQUIRED----
                                                                                                                        AMBN
                                                                                                                                 39
                                                                                                                        AMBN
                                                                                                                                 40
       NO EXTERNAL SURROUTINES ARE REQUIRED.
                                                                                                                        AMRN
                                                                                                                        AMBN
                                                                                                                                 42
                             ----ARGUMENT LIST----
                                                                                                                        AMBN
                                                                                                                       AMBN
AMBN
                                                                                                                                 44
                         R *4
                                     ND
                                               INP
                                                                                                                        AMBN
       PRESUR
                                               OUT
                                     ND
                                                                                                                       AMRN
AMRN
                         1+4
                                                                                                                        AMBN
COMMON STORAGE USED
        COMMON IMAX.CI.VXI.VYI.HI
                                                                                                                        AMBN
                                                                                                                        AMBN
        TMAX
                                     ND
                                                                                                                        AMRN
                                               INP
        CT
                         R#4
                                     100
                                               INP
                                                                                                                        AMBN
                                                        (NOT USEC BY THIS SUBROUTINE) (NOT USED BY THIS SUBROUTINE)
                         R#4
                                                                                                                       AMBN
                                              INP
        VXI
                                     100
        VYI
                                               INP
                                     100
                         ...
                                     100
                                                                                                                       AMBN
                                                                                                                        AMBN
                                                                                                                                 57
                             ----INPUTS----
                                                                                                                        AMBN
                                                                                                                       AMRN
                           #HEIGHT IN KM
*NUMBER OF ATMOSPHERIC LAYERS WITH FINITE THICKNESS
#SOUND SPEED (KM/SEC) IN I-TH LAYER
#X COMPONENT OF WIND VELOCITY (KM/SEC) IN I-TH LAYER
#Y COMPONENT OF WIND VELOCITY (KM/SEC) IN I-TH LAYER
#THICKNESS IN KM OF I-TH LAYER
                                                                                                                       AMBN
                                                                                                                                 60
        IMAX
                                                                                                                       AMBN
       VXI(1)
                                                                                                                       AMBN
                                                                                                                       AMBN
                                                                                                                                 63
                                                                                                                       AMBN
                                                                                                                       AMRN
        HILLI
                                                                                                                                 65
                                                                                                                       AMBN
                                                                                                                                       PROGRAM
                                                                                                                                66
67
                             ----OUT PUTS----
                                                                                                                       AMBN
                                                                                                                                           AMBNT
                                                                                                                       AMBN
                                                                                                                                 68
                           *AMBIENT PRESSURE IN DYNES/CH##2 AT ALTITUDE Z
                                                                                                                       AMBN
                                                                                                                                            PAGE
        PRESIIR
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Section of the second section of the section of the second section of the section of the second section of the section o

AMBN

INDEX OF LAYER IN WHICH Z LIES

AKRN AMRN ---- PROGRAM FOLLOWS RELOW----Ċ AMBN 74 75 SUBROUTINE AMENT (2. PRESUR. I) APBN AMEN C DIMENSION AND COMMON STATEMENTS
DIMENSION CI(100).VXI(100).VVI(100).HI(100) AMBN COMMON IMAX.CI.VXI.VYI.HI AMBN AMBN AMBN C THE FINAL VALUE OF ENDOW WILL BE THE INTEGRAL FROM 0 TO 7 OF C -GAMMA #G/C##2. THE RUNNING VALUE WILL RE THE SUBTOVAL. 80 AMBN AMBN AMBN AMBN ENPON-0.0 THE RUNNING VALUE OF I WILL BE THE LAYER BEING CONSIDERED I=1 7 LIES IN LAYER 1 IF IMAX=0. ZT=0.0 AMBN AMBN AMBN AMBN IF(IMAX .EQ. 0) GO TO 30 AMBN AMBN AMBN C TOP OF FIRST LAVER 90 AMBN C THE START OF A LOOP. THE CURRENT ZT DENOTES THE TOP OF THE I-TH LAYER 10 1F(Z .GT. ZT) GO TO 20 93 AMBN AMBN C 7. LIES IN 1-TH LAYER
C 7T-HI(I) IS HEIGHT OF BOTTOM OF I-TH LAYER
C 7-7T-HI(I) IS DISTANCE OF 7 ABOVE BOTTOM OF I-TH LAYER
ENPON=ENPON=1.4*(.0094/CI(I)**2)*(Z-ZT+HI(I)) AMBN 96 AMBN AMBN AMBN 99 AMBN 100 12 GO TO 40 C 7 LIES ABOVE TOP OF I-TH LAYER
20 FNPON=FNPON-1.4+(.0099/CI(!)+*2)*HI(!)
C THE CURRENT ENPON IS THE INTEGRAL OF -1.4+G/C**2 UP TO THE TOP AMBN AMBN 102 AMBN 103 AMBN **AMBN 105** 1=1+1 AMBN 106 IF(I ofto IMAX) GO TO 30 ZT=7T+HI(I) C 7Y IS THE TOP OF THE NEW I-TH LAYER GO TO 10 AMBN **AMBN 108** AMBN 109 AMBN 110 AMBN 111 C END OF LOOP AMBN 112 C 7 LTES IN UPPER HALFSPACE 30 ENPON=ENPON-1.4*(.0098/CI(I)**2)*(Z-ZT) AMBN 113 AMBN 114 AMBN 115 C CONTINUING FROM 12 OR 30 40 PRESUR=1.E6*EXP(ENPON) AMBN 116 AMBN 117 AMBN 118 RETURN END **AMBN 119**

> PROGRAM AMBNT

```
ATMOS (SUBROUTINE)
                                                                                                      ATMO
                                                        6/19/68
                                                                                                      OMTA
C
                                                                                                      ATMO
                           ----ABSTRACT----
                                                                                                      ONTA
                                                                                                      ATHO
                                                                                                      CHTA
  TITLE - ATHRE
                                                                                                     ATMO
            TABULATION OF WIND VELOCITY COMPONENTS AND SPEED OF SOUND FOR
                                                                                                     OMTA
            ALL LAYERS OF MODEL ATMOSPHERES
                                                                                                     CHTA
                                                                                                     OHTA
                    THE MODEL ATMOSPHERE CONSISTS OF UP TO 100 ISOTHERMAL LAYERS (THE TOP LAYER BEING INFINITE). EACH LAYER MAY HAVE A UNIQUE TEMPERATURE. THICKNESS AND WIND VELOCITY. SURROUTINE ATMOS CONVERTS AN INPUT DESCRIPTION OF THE ATMOSPHERE'S PROPERTIES INTO ONE MORE APPROPRIATE FOR THE CALCULATIONS TO FOLLOW (SUCH AS EVALUATION OF THE NORMAL MODE DISPERSION FUNCTION IN NMDEN. DESCRIBED ELSEWHERE IN THIS SERIES).
                                                                                                     ATMO
                                                                                                     OKTA
                                                                                                     ATHO
                                                                                                     ATHO
                                                                                                     ATMO
                                                                                                             15
                                                                                                     ATMO
                                                                                                     OHTA
                                                                                                     ATHO
                                                                                                     ATMO
                                                                                                             19
                                                                                                     ATHO
  LANGUAGE
                 - FORTRAN IV (360+ REFERENCE MANUAL C28-6515-4)
                                                                                                             20
                                                                                                     ATMO
                                                                                                     OHTA
  AUTHORS
                 - A.D.PIERCE AND J.POSEY, M.I.T.. JUNE-1968
                                                                                                             22
                                                                                                             23
                                                                                                     ATMO
                           ----US AGE----
                                                                                                     OMTA
                                                                                                     ATMO
        IMAX MUST BE STORED AS THE FIRST VARIABLE IN UNLABELED COMMON WHEN
                                                                                                     DMTA.
                                                                                                     ATMO
                                                                                                     ATMO
        NO FORTRAN SUBROUTINES ARE CALLED.
                                                                                                     ATMO
                                                                                                             30
                                                                                                     OMTA
                                                                                                             31
  FORTRAN USAGE
                                                                                                     ATHO
                                                                                                     ATMO
        CALL ATMOS(T.VKNTX.VKNTY.ZI.WANGLE.WINDY.LANGLE)
                                                                                                     ATMO
                                                                                                     OMTA
  THPUTS
                                                                                                     OMTA
OMTA
                    NUMBER OF LAYERS OF FINITE THICKNESS IN THE MODEL ATMOS-
       TMAX
                                                                                                     OMTA
                                                                                                     ATMO
                     PHERF. ( 1.LF. IMAX.LE.99 )
                                                                                                             40
                     T(1) IS TEMPERATURE OF LAYER 1 IN MODEL ATMOSPHERE.
                                                                                                     AFMO
         R#4(D)
                    (DEGREES KELVIN)
                                                                                                     ATMO
                                                                                                     OMTA
                     VKNTX(I) IS WIND VELOCITY COMPONENT IN X-DIRECTION (WEST
      VKNTX
                    TO EAST) FOR LAYER I. (KNOTS)
                                                                                                             45
         R#4(D)
                                                                                                     ATMO
                                                                                                     DMTA
                    VKNTY(1) IS WIND VFLOCITY COMPONENT IN Y-DIRECTION (SOUTH TO NORTH) FOR LAYER I. (KNOTS)
       VKNTY
                                                                                                     ATMO
         Q#4(D)
                                                                                                     OPTA
                                                                                                             48
                                                                                                     OHTA
                                                                                                     ATMO
OMTA
                    71(1) IS THE HEIGHT ABOVE THE GROUND OF THE TOP OF LAYER
                                                                                                             50
         R=4(D) J. (KM)
                                                                                                             51
                    WANGLE(I) IS WIND VELOCITY DIRECTION FOR LAYER I. RECKONE COUNTER CLOCKWISE FROM THE X-AXIS. (DEGREES)
       WANG! F
                                                                                                     ATMO
         R#4(N)
                                                                                                     ATMO
                                                                                                     ATHO
       WINDY
                     WINDY(I) IS MAGNITUDE OF WIND VELOCITY IN LAYER I.
                                                                                                     ATHO
         R#4(D)
                    (KNOTS)
                                                                                                     ATMO
                                                                                                     ATHD
                                                                                                             58
                    SPECIFIES WHICH SORT OF WIND DATA IS INPUT-
IF LANGLE-LE-O , VKNTX AND VKNTY ARE INPUT-
IF LANGLE-GT-O , WANGLE AND WINDY ARE INPUT-
      LANGLE
                                                                                                     GMTA
         1 = 4
                                                                                                     DMTA
                                                                                                             60
                                                                                                     OHTA
                                                                                                     OMTA
                                                                                                     OMTA
  OUTPUTS
                                                                                                            63
             THE OUTPUTS ARE STORED IN UNLABFLED COMMON IN THE FOLLOWING
                                                                                                            64
              ORDER. REGINNG IN POSITION 2
                                                                                                     ATMO
             C1(100) + VXI(100) + VYI(100) + HI(100)
                                                                                                     OMTA
                                                                                                            66
                                                                                                                  PROGRAM
                                                                                                     OMTA
                                                                                                            57
                                                                                                                     ATMOS
                    CI(I) IS THE SPEED OF SOUND IN LAYER I OF THE MODEL ATMOS
                                                                                                    ATMO
                                                                                                            68
         R#4(D) PHEPF. ( KM/SFC )
                                                                                                     OMTA
                                                                                                                      PAGE
                                                                                                     ATMO
                                                                                                            70
```

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the season of th

-225-

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VXIII) IS WIND VELOCITY COMPONENT IN X-DIRECTION (WEST TO ATMO 71
        R#4(D) FEST) FOR LAYER 1. ( KM/SEC )
                                                                                              ATMO
        VYI(I) IS WIND VELOCITY COMPONENT IN Y-DIRECTION (SOUTH R#4(D) TO NORTH) FOR LAYER I. ( KM/SEC )
                                                                                              ATHO
      VYI
                                                                                              OMTA
                                                                                              ATHO
                                                                                                     76
77
                                                                                             OMTA
OMTA
      HI
                  HI(I) IS THE THICKNESS OF LAVER I. ( KM )
        8*4(0)
                                                                                                     78
                                                                                              ATHO
                                                                                             ATMO
                         ----PROGRAM FOLLOWS BELOW----
                                                                                                     81
                                                                                              ATMO
                                                                                              ATHO
       SUPPOUTINE ATMOSIT. VKNTX. VKNTY. ZI. WANGLE. WINDY. LANGLE)
                                                                                              ATNO
                                                                                             ATHO
r
                                                                                                     85
       DIMENSION C1(100). VXI(100). VYI(100). HI(100)
                                                                                              ATMO
       DIMENSION T(100).VKNTX(100).VKNTY(100).ZI(100)
DIMENSION WANGLE(100).WINDY(100)
                                                                                             ATMO
                                                                                              ATMO
                                                                                                     88
       CHANDA IMAX.CI.VXI.VYI.HI
                                                                                              ATMO
                                                                                              ATMO
                                                                                              ATMO
C JET IS TOTAL NUMBER OF LAYERS.
                                                                                                     91
                                                                                              ATMO
       JET = [MAX + 1
[MAX = JET - 1
                                                                                              ATMO
IF (LANGLE .LE. C) 69 TO 20
D3 = 3.1415927 / 180.0
C D3 IS THE NUMBER OF RADIANS IN A DEGREE
                                                                                             OMTA
OMTA
                                                                                                     04
                                                                                                     95
                                                                                              ATMO
                                                                                             ATMO
ATMO
C IF VKNTX AND VKNTY WERE NOT INPUT. THEY ARE NOW DETERMINED FROM WINCY
                                                                                                     98
C AND WANGLE.

ON 5 [=1,JFT

VKNTX([) = WINDY([) = COS(D3*WANGLE([]))

5 VKNTY([] = WINDY([]) = SIN(D3*WANGLE([]))

20 91 = 1.4 * 8.3144 * 0.001 / 29.0
                                                                                             ATHO
                                                                                              ATMO 100
                                                                                             ATMO 101
                                                                                             ATMO 102
                                                                                              ATMO 103
C 02 IS THE NUMBER OF KM/SEC PER KNOT.
02 = 0.0005148
                                                                                             ATMO 104
ATMO 105
C
                                                                                              ATMO 106
        DO 30 I = 1.JET
                                                                                             ATHO 107
                                                                                             ATMO 108
C THE SPEED OF SOUND = { GAMMA + P / RHO } FOR PERFECT GAS. AND { P/RHO
                                                                                              ATHO 109
C = ( R + T )
C R IS THE (UNIVERSAL GAS CONSTANT)/(MOLECULAR MEIGHT)
                                                                                             ATMO 110
                                                                                             ATMO 111
       CI(1) = SORT(D1*T(1))
                                                                                             ATMO 112
                                                                                             ATMO 113
ATMO 114
                          * V(KM/SEC)
                                                                                             ATHO 115
                                                                                             ATMO 116
ATMO 117
                                                                                              ATMO 118
                                                                                             ATHO 119
ATMO 120
                                                                                              ATHO 121
        RETURN
                                                                                             ATHO 122
                                                                                             ATMO 123
        FND
```

.

PROGRAM ATHOS

```
7/25/68
                                                                                           8868
C.
       ARRE (SURROUTINE)
                                                                                           8888
                       ----ABSTRACT----
                                                                                           BRRR
                                                                                           8888
  TITLE - BRAR
           THIS SURROUTINE COMPUTES THREE FUNCTIONS RI-R2+R3 OF A VARIABLE
                                                                                           BARR
                                                                                           8888
               THESE ARE DEFINED FOR X .GE. O BY THE FORMULAS
                                                                                           5888
C
              R1= 1.0 +SINH(2Y)/(2Y)
                                                                                           8888
                                                                                           RRRR
                                                                                                  10
                                                                                           BRRR
              R2= (SINH(2Y)/2Y - 1.0)/Y**2
                                                                                                  11
                                                                                           5866
                                                                                           5555
              R3= (COSH(2Y)-1.0)/Y**2
                                                                                           8888
           WHERE Y= SQPT(X). FORMULAS FOR NEGATIVE X MAY BE OBTAINED BY ANALYTIC CONTINUATION. FOR SMALL VALUES OF X. THE FUNCTIONS ARE COMPUTABLE BY THE POWER SERIES
                                                                                           8888
                                                                                           8888
                                                                                           BBAR
                                                                                                  17
                                                                                           8888
C.
                                                                                                  18
              R1= 2 + 4x/(3FACT) +(4X)++2/(5FACT) + (4X)++3/(7FACT) +...
                                                                                           8888
                                                                                                  20
              R2= 4/(3FACT) + 4*(4X)/(5FACT) + 4*(4X,**2/(7FACT) +...
                                                                                           BRRR
                                                                                                  21
                                                                                           888R
              R3= 4/(2FACT) + 4*(4x)/(4FACT) + 4*(4x)**2/(6FACT) +...
                                                                                           6888
                                                                                           BBBB
           THE MANNER IN WHICH THESE PARTICULAR FUNCTIONS ARISE IN THE
                                                                                           8888
           THEORY COMES FROM INTEGRATIONS OVER VARIOUS PRODUCTS OF CALLX)
                                                                                           8888
           AND SAI(X). IN PARTICULAR, FOR X POSITIVE.
                                                                                           RRRR
                                                                                                  27
                                                                                           8888
              RI= (2/Y)(INTEGRAL ON Y FROM O TO Y OF (COSH(Y))**2)
                                                                                           8888
C.
                                                                                           8888
                                                                                                  30
              R2= (2/Y**3)(INTEGRAL ON Y FROM O TO Y OF (SINH(Y))**2)
                                                                                           BBBB
                                                                                                  31
                                                                                           8888
C
C,
               P3= (4/Y++2)(INTEGRAL ON Y FROM O TO Y OF SINH(Y)+COSH(Y))
                                                                                           8888
                                                                                           -
                               THE CORRESPONDING FORMULAS FOR X NEGATIVE CAN
           WITH Y=SQRT(x). THE CORRESPONDING FORMULAS FOR X NEGATIVE CAN BE OBTAINED BY REPLACING SINH AND COSH BY SIN AND COS. RESPECTIVELY. AND BY REINTERPRETING Y AS SQRT(-x).
                                                                                           8888
                                                                                           8588
                                                                                           BBBB
                                                                                                  37
                                                                                           8888
                                                                                                  38
                 FORTRAN IV (360, REFERENCE MANUAL C28-6515-4)
                                                                                           8888
  LANGUAGE
                - A.D.PIFRCE. M.I.T., JULY.1968
                                                                                           8888
                                                                                                  40
                                                                                           8888
                       ----CALLING SFOUENCE----
                                                                                           8888
                                                                                           8888
  SEE SUBROUTINE FLINT
                                                                                           8886
                                                                                           8888
       CALL BRBS(X.R1.R2.R3)
                                                                                           8888
                                                                                           8888
                          ----EXTERNAL SUBROUTINES REQUIRED----
                                                                                           8888
  C
                                                                                           8888
8888
C
       CAT. SAT
                                                                                                  50
                                                                                           8368
                       ---- ARGUMENT LIST----
                                                                                           8888
                                                                                           8888
                                                                                                  53
                             NO
                                     INP
                                                                                           8888
                   ...
                             NI)
                                     OUT
                                                                                           8888
C
                                                                                           BRRR
       02
                   ReL
                             NO
                                     CUIT
                                                                                                  56
                                                                                           8888
                   R * 4
                                     DUT
       83
                                                                                                  58
                                                                                           8888
   NO COMMON STORAGE IS USED
                                                                                           8888
                                                                                                  59
                                                                                           8888
                       ---- PROGRAM FOLLOWS BELOW----
                                                                                           ARAR
                                                                                           8888
        SUBROUTINE BARB(X.R1.R2.R3)
                                                                                           8888
                                                                                                  64
65
                                                                                           RRAR
                                                                                           8888
        [F(ARS(X) .GT. 1.E-2) GO TO 3
                                                                                           8888
                                                                                                       PROGRAM
                                                                                                  66
  COMPUTATION FOR SMALL X
                                                                                           BBBB
                                                                                                  47
                                                                                                         8888
       701#11W FIN STREE A
R2=2.0/3.0+(2.0/15.0) #X+(4.0/315.0) #X**2+(2.0/9.0) #X**3/315.0
R3=2.0+2.0+X/3.0>4.0#X**7/45.0+2.0#X**3/315.0
                                                                                           8888
                                                                                           8888
```

8888

70

23

•	8888	71
L AND THE PART OF	8888	72
C COMPUTATION FOR X NOT NEAR ZEPO	8888	73
3 RZ=(S-1.0)/X R3=(CAT(4.0+X)-1.0)/X	8888	74
# 3# (C#) 1460-X/-1607/X	8888	75
C COMPUTATION OF RI FOR ARBITPARY X	9888	76
	8888	77
4 #1=1.0+S	9888	78
RETURN	6886	79
END		

PROGRAM BBRR

```
CAI
                                                            7/25/69
        CAL (FUNCTION)
                                                                                                               CAI
CAI
CAI
                           ----ARSTRACT----
  TITLE - CAT
            - rat

program to evaluate function cal(x) for given variable x.

if x is negative, cal(x)= cos(sort(-x)). If x is positive.

cal(x)= cosm(sort(+x)). The function is also representable
                                                                                                               CAI
CAI
CAI
             AY THE POWER SERSES
                                                                                                               CAI(X)= 1 + X/(2FACT) + X=+2/(4FACT) + X++3/(6FACT) + ...
                  - FORTRAN IV (360. REFERENCE MANUAL C28-6515-4)
  LANGUAGE
                   - A.D.PIERCF. M.I.T., JULY,1968
----CALLING SEQUENCE----
  AUTHOR
C
        CATTANY R*4 ARGUMENT) MAY BE USED IN ARITHMETIC EXPRESSIONS
                                                                                                                      20
21
                            ----FXTERNAL SUBROUTINES REQUIRED----
        NO EXTERNAL SURPOUTINES ARE REQUIRED
                                                                                                                      23
24
25
                            ----ARGUMENT LIST----
                                            INP
                                    NΩ
         X
CAT
                                            OUT
                                                                                                                      28
29
30
C NO COMMON STORAGE IS USED
                            ---- PROGRAM FOLLOWS RELOW----
r
                                                                                                                      33
34
35
         FUNCTION CATEX)
r
         1F(x .GF. 0.0) GO TO 11
                                                                                                                      36
37
                                                                                                               CAI
CAI
CAI
CAI
CAI
CAI
CAI
   X IS LESS THAN 0
10 CAT=COS(SORT(-X1)
RETURN
C X IS GREATER OR EQUAL TO 0
11 E=FXP(SQRT(X))
C THE HYPERBOLIC COSINE IS COMPUTED CAI=0.5*(E+1./E)
                                                                                                                       44
45
46
         FFTURN
          END
```

A - 1 - - NOW MAN AND POLY

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c

The state of the s

PROGRAM CAT PAGE 25

The second secon

```
ELINT (SURROUTINE)
                                                        7/25/68
                                                                                                       FLIN
                                                                                                       EL IN
                          ----ARSTRACT----
                                                                                                       FLIN
                                                                                                       EL IN
C TITLE - FLINT
                                                                                                       FLIN
            THIS SUBROUTINE COMPUTES THE INTEGRAL
                                                                                                       ELIN
                                                                                                       EL IN
EL IN
              AINT = INTEGRAL OVER Z FROM O TO H OF
                                                                                                       ELIN
                        [A1*F1(7) + A2*F2(2))**2
                                                                                                       FLIN
                                                                                                               10
                                                                                                       FLIN
           THE FUNCTIONS F1(7) AND F2(2) ARE THE SOLUTIONS OF THE COUPLED
           ORDINARY CIFFERENTIAL EQUATIONS
                                                                                                      ELIN
               DF1/NZ = A11#F1 + A12#F2
DF2/DZ = A21#F1 + A22#F2
                                                                                                124
                                                                                                       ELIN
                                                                                                               17
            WHERE THE FLEMENTS OF THE MATRIX A ARE INDEPENDENT OF 7.
                                                                                                       EL IN
                                                                                                               18
           FOR GIVEN SOUND SPEED C. WIND VELOCITY COMPONENTS VX AND VV.
ANGULAR FREQUENCY OMEGA. AND WAVE NUMBER COMPONENTS AKX AND AKY
THE A(1.J) ARE COMPUTED BY CALLING ASAA. THE SOLUTION TO THE
DIFFERENTIAL EQUATIONS IS FIXED BY SPECIFICATION OF F1 AND F2
                                                                                                      ELIN
                                                                                                               20
                                                                                                       ELIN
                                                                                                               21
                                                                                                       ELIN
            AT Z=H.
                                                                                                       EL IN
                                                                                                      FI IN
  PROGRAM NOTES
                                                                                                       ELTN
                                                                                                              26
                    THE GENERAL SOLUTION OF EONS. (2) IS
                                                                                                      ELIN
                                                                                                       ELIN
                        F1(2) = CAI(X)*F1(H)-(H-Z)*SAI(X)*(A11*F1(H)*A12*F2(H)
F2(Z) = CAI(X)*F2(H)-(H-Z)*SAI(X)*(A21*F1(H)*A22*F2(H)
                                                                                                      ELIN
                                                                                                               30
                                                                                                      ELIN
                                                                                                               31
                    WITH X=(A11++2+A12+A21)+(H-2)++2 SINCE A22=-A11. WE LET
                                                                                                      EL IN
                                                                                                              33
                        R1 = (INTEGRAL OF (CAT(X))**2)*(2/H)
R2 = (INTEGRAL OF ((H-Z)*SAT(X))**2)*(2/H**3)
R3 = (INTEGRAL OF ((H-Z)*SAT(X)*CAT(X)))*(4/H**2)
                                                                                                      ELIN
                                                                                                              36
37
                                                                                                      ELIN
                                                                                                      ELIN
                    WHERE IN EACH CASE THE INTEGRATION IS OVER Z FROM 0 TC H. THE QUANTITIES R1.R2.R3 ARE COMPUTED BY CALLING BBBB.
                                                                                                      EL IN
                                                                                                      ELIN
                                                                                                              39
                    THEN
                                                                                                      ELIN
                                                                                                              40
                        AINT=(H/2)*(FP1)**2*R1+(H0*3/2)*(FP2)**2*R2
-(H**2/2)*(FP1)*(FP2)*R3
                                                                                                      ELIN
                                                                                                      ELIN
                                                                                                      ELIN
                                                                                                              45
46
                    WITH
                                                                                                      ELIN
                        FP1= A1+F1(H)+A2+F2(H)
                                                                                                      ELIN
                         FP7= A1*(A11*F1(H)+A12*F2(H))+A2*(A21*F1(H)+A22*F2(H))
                                                                                                      ELIN
                                                                                                              48
                    HF LATTER TWO QUANTITIES REPRESENT THE COEFFICIENTS OF CAI(x) AND (H-Z)*SAI(x) IN A1*F1+42*F2.
                                                                                                      ELIN
                                                                                                      ELIN
C LANGUAGE - FORTRAN IV (360, REFERENCE MANUAL C28-6515-4)
                                                                                                      ELIN
CAUTHOR
                 - A.D.PIERCE. M.I.T.. JULY.1968
                                                                                                      EL IN
                                                                                                      EL IN
                          ----CALLING SFQUENCE----
                                                                                                      ELIN
ELIN
ELIN
                                                                                                              57
58
C SEF SUBROUTINE TOTINT
  NO DIMENSION STATEMENTS REQUIRED
                                                                                                              54
        CALL ELINTI MEGA. AKX. AKY. C. VX. VY. H. FIH. FZH. A1. A2. AINTI
                                                                                                      EL IN
                                                                                                              60
                                                                                                      ELIN
                                                                                                      ELIN
                          --- EXTERNAL SURROUTINES REQUIRED ----
                                                                                                              63
        AAAA, BBBB
                                                                                                      ELIN
                                                                                                              65
                          ---- ARGUMENT LIST----
                                                                                                                    PROGRAM
                                                                                                              66
                                                                                                                      EL INT
                                                                                                      ELIN
        OMEGA
                       844
                                 MO
                                         THE
                                                                                                              68
                                         INP
                                                                                                                        PAGE
                                 ND
        AKX
        AKY
                       ...
                                 ND
                                          INP
```

```
FLIN
                                       ND
                                                 INP
                                                                                                                         EL!N
EL!N
                                                 INP
                                       ND
                            R*4
                                       ND
                                                 INP
                            ---
                                                 INP
INP
                                       NO
                                       ND
                                                                                                                         ELIN
         FIH
         F2H
                           R#4
                                                 INP
с
С
         A1
                            R#4
                                       NO
                                                 INP
                                                                                                                         ELIN
                            ...
                                                 INP
                                                                                                                         FLIN
                                                                                                                                   78
          A2
                                       ND
          AINT
                                                 OUT
                                                                                                                                  80
                                                                                                                         ELIN
   NO COMMON STORAGE USED
                                                                                                                         ELTN
                                                                                                                         ELIN
                               ----INPUTS----
                                                                                                                         FLIN
         OMFG4
                             =ANGULAR FREQUENCY IN RADIANS/SEC
                                                                                                                         ELIN
                             =ANGULAR FREQUENCY IN RADIANS/SEC

=X COMPONENT OF WAVE NUMBER VECTOR IN KM=*(-1)

=Y COMPONENT OF HAVE NUMBER VECTOR IN KM=*(-1)

=SOUND SPEED IN KM/SEC

=X COMPONENT OF WIND VELOCITY IN KM/SEC

=Y COMPONENT OF WIND VELOCITY IN KM/SEC

=INTEGRATION INTERVAL (LAYER THICKNESS) IN KM

=YALUE OF F1(Z) AT UPPEP LIMIT OF INTEGRAL

=VALUE OF F2(7) AT UPPEP LIMIT OF INTEGRAL

=COEFFICIENT OF F2(Z) IN INTEGRAND

=COEFFICIENT OF F2(Z) IN INTEGRAND
          AKX
          AKY
                                                                                                                         ELIN
                                                                                                                         ELIN
                                                                                                                         EL IN
          ٧v
                                                                                                                                   90
          н
                                                                                                                         ELIN
          AI
                                                                                                                         EL IN
                                                                                                                         FLIN
                               ---- 01171175----
                                                                                                                         EL IN
                                                                                                                                  97
          ATNT
                              FINTEGRAL OVER HEIGHT WITH RANGE H OF THE QUANTITY
                                                                                                                         ELIN
                                                                                                                        ELIN 100
ELIN 101
                               (A1#F1(Z)+A2#F2(Z))##Z WHERE F1(Z) AND F2(Z) ARE EQUAL TO F1H AND F2H, RESPECTIVELY, AT THE UPPER
                               LIMIT AND SATISFY THE RESIDUAL DIFFERENTIAL EQUATIONS
                                                                                                                         FL IN
EL IN
                                                                                                                                 103
                               ----PROGRAM FOLLOWS BELOW----
                                                                                                                                104
                                                                                                                         ELIN 106
ELIN 107
          SURROUTINE ELINT (OMEGA. AKX. AKY. C. VX. VY. H. FIH. F2H. A1. A2. AINT)
          DIMENSION A(2.2)
          CALL AAAA(CHEGA.AKX.AKY.C.VX.VY.A)
                                                                                                                         ELIN
                                                                                                                         ELIN 109
C COMPUTATION OF FP1 AND FP2
                                                                                                                         EL IN
                                                                                                                                 110
          TP1=A1*F1H+A2*F2H
FP1=A1*F1H+A2*F2H
FP2=A1*(A(1,1)*F1H+A(1,2)*F2H)+A2*(A(2,1)*F1H+A(2,2)*F2H)
                                                                                                                         ELIN 111
                                                                                                                         ELIN 112
C COMPUTATION OF COEFFICIENTS OF R1.R2.R3
                                                                                                                         ELIN 113
                                                                                                                         ELIN 114
          $1=0.5*H&FP1**2
$2=0.5*(H**3)*FP2**2
                                                                                                                         ELIN 115
                                                                                                                         ELIN 116
ELIN 117
                                                                                                                         ELIN
           $3=-0.5*(H**2)*FP1*FP2
                                                                                                                         ELIN 118
     C COMPUTATION OF R1.R2.R3
X=(A(1.1)p+2+A(1.2)+A(2.1))+H++2
                                                                                                                         ELIN 119
                                                                                                                         ELIN 120
          GALL BBBB(x.R1.R2.R3)
                                                                                                                         ELIN 121
                                                                                                                         ELIN 122
ELIN 123
C COMPUTATION OF AINT
          AINT=S1*P1+S2*P2+S3*P3
RETURN
                                                                                                                         ELIN 124
ELIN 125
                                                                                                                         ELIN 126
           FND
```

PROGRAM EL INT PAGE

La Marie La Contra Marie and . Sandala . The contra the contra to the

THE RESIDENCE OF THE PARTY OF T

```
6/19/68
                                                                                                         FNM1
       ENMODE (FUNCTION)
                                                                                                         FNMI
                           ----ARSTRACT----
                                                                                                         FNM1
                                                                                                         FNMI
                                                                                                        FNM1
 TITLE - FNMCOL
           EVALUATATION OF NORMAL MODE DISPERSION FUNCTION AS FUNCTION OF
                                                                                                        FNMI
                                                                                                         FNM1
           PHASE VELOCITY V
                   THE NORMAL MODE DISPERSION FUNCTION DEPENDS ON THREE VARIABLES. ANGULAR FREQUENCY OMEGA. PHASE VELOCITY V. AND DIRECTION OF PROPAGATION THETK. FNMODI OBTAINS V THROUGH ITS ARGUMENT. OMEGA AND THETK FROM COMMON. SURPOUTINE NMDFN IS THEN CALLED TO EVALUATE THE FUNCTION. (SEE PIERCE. J.COMP.PHYSICS. FEB..1967. P.343-366 FOR DEFINITION OF NORMAL MODE DISPERSION FUNCTION.)
                                                                                                        FNM1
                                                                                                        FNM1
                                                                                                        FNM1
                                                                                                         FNM1
                                                                                                                 14
                                                                                                        FNM1
                                                                                                         FNM1
                                                                                                         FNM)
                                                                                                         FNM1
 LANGUAGE
                 - FORTRAN IV (360. REFERENCE MANUAL C28-6515-4)
                                                                                                        FNM1
                                                                                                        FNM1
                 - A.D.PIERCE AND J.POSEY. M.I.T., JUNE.1968
                                                                                                         FNM1
 AUTHORS
                                                                                                        FNM1
                                                                                                         FNM1
                           ----USAGE----
                                                                                                                 24
25
                                                                                                         FNM1
       THEGA HUST BE STORED IN WORD POSITION 402 OF UNLABELED COMMON. AND
                                                                                                        FNH1
                                                                                                         FNM1
        THETK MUST BE IN POSITION 404.
                                                                                                         FNM1
       FNMOD1 CALLS SURROUTINE NMDFN WHICH CALLS AAAA AND RRRR. RRRR CALLS AAAA AND MMMM. ALL THESE SUBROUTINES ARE DESCRIBED FLSE-WHERE IN THIS SERIES.
                                                                                                        FNM1
                                                                                                                 28
                                                                                                         FNM1
                                                                                                         FNM1
                                                                                                        FNM1
                                                                                                                 31
                                                                                                        FNM1
  CALLING SEQUENCE
                                                                                                                 32
                                                                                                         FNM1
                                                                                                                 34
35
        COMMON CM1(401). OMEGA. CM2, THETK
                                                                                                         FNM1
        OMEGA = XXX
THETK = XXX
                                                                                                         FNM1
                                                                                                         FNM1
                                                                                                         FNM1
                                                                                                                 37
        FUNCTH = FHMODICVI
                                                                                                         FNF1
                                                                                                                 38
                                                                                                         FNH1
  INPUTS
                                                                                                         FNH1
                                                                                                                 40
                                                                                                         FNM1
                                                                                                         FNM1
                     PHASE VELOCITY (KM/SEC).
C
                                                                                                         FNM1
                                                                                                        FNM1
                                                                                                         FNM1
                     ANGULAR FREQUENCY (RADIANS/SEC).
      OMEGA
                                                                                                         FNM1
         R+4
                                                                                                        FNM1
                                                                                                                 47
                     PHASE VELOCITY DIRECTION MEASURED COUNTER-CLOCKWISE FROM
                                                                                                         FNM1
       THETK
                                                                                                         FNM1
                     X-AYIS.
         R=4
                                                                                                                 50
51
                                                                                                        FNM)
                                                                                                         FNMI
  OUTPUTS
                                                                                                                 52
53
                                                                                                         FNM1
       THE ONLY OUTPUT IS THE VALUE OF THE NORMAL MODE DISPERSION FUNCTION FOR THE VALUES OF V. OMEGA. AND THETK WHICH HAVE BEEN INPUT.
                                                                                                        FNM1
                                                                                                         FNM1
                                                                                                         FNM1
                                                                                                         FNM1
                                                                                                         FNH1
                            ----PROGRAM FOLLOWS BELOW----
                                                                                                                 58
59
                                                                                                         FNM1
                                                                                                         ENM1
                                                                                                         FNM1
        FUNCTION FNMOD1(V)
                                                                                                         FNM1
r
                                                                                                         FNM1
         DIMENSION C1(100).VX1(100).VY1(100).HI(100)
                                                                                                                 62
                                                                                                         FNMI
         COMMON IMAX.CI.VXI.VYI.HI.CMEGAC.VPHSEC.THETK
                                                                                                         FNM1
                                                                                                                 65
   OMEGA AND THETK OBTAINED FROM COMMON
                                                                                                         FNM1
                                                                                                                       PROGRAM
                                                                                                         FNH1
                                                                                                                 66
        OMEGA=OMEGAC
         CALL NMMENIOMEGA.V. THETK.L. FPP.KI
                                                                                                         FNM1
                                                                                                                 67
                                                                                                                        FNMOD1
         FN40D1 = FPP
                                                                                                         FNMI
                                                                                                                 58
                                                                                                         FN#1
                                                                                                                           PAGE
         RETURN
                                                                                                         FNMI
                                                                                                                              28
         FND
```

-232-

```
FNMOD2 (FUNCTION)
                                                       6/19/68
                                                                                                   FMM2
                                                                                                   FN42
                          ----ABSTRACT----
                                                                                                   FN42
                                                                                                   FNM2
  TITLE - FNMODS
           EVALUATATION OF NORMAL MODE DISPERSION FUNCTION AS FUNCTION OF
                                                                                                   FNM2
            ANGULAR FREQUENCY DMEGA
                                                                                                   FNM2
                                                                                                   FNMZ
                    THE NORMAL MODE DISPERSION FUNCTION DEPENDS ON THREE VARIABLES. ANGULAR FREQUENCY OMEGA. PHASE VELOCITY V. AND DIRECTION OF PROPAGATION THETK. FAMODE ORTAINS OMEGA
                                                                                                   FNM2
                                                                                                   FNM2
                                                                                                   FN42
                   THROUGH ITS ARGUMENT. AND THETK FROM COMMON. SURROUTINE NMOFN IS THEN CALLED TO EVALUATE THE FUNCTION. (SEE PIERCE. J. COMP. PHYSICS. FER. 1967. P.343-366 FOR DEFINITION OF NORMAL MORE DISPERSION FUNCTION.)
                                                                                                   FNM2
C
                                                                                                   FNM2
                                                                                                   FNM2
                                                                                                   FNMZ
                                                                                                   FNM2
  LANGUAGE
               - FORTRAN IV 1360. REFERENCE MANUAL C28-6515-41
                                                                                                   FNM2
                                                                                                           10
                                                                                                   FNM?
  AUTHORS
                 - A.D.PIERCE AND J.POSEY. M.I.T., JUNE-1968
                                                                                                   FNH2
                                                                                                           20
                                                                                                   FNM2
                                                                                                           21
                                                                                                   FNHZ
                                                                                                          23
                          ----IISAGE----
                                                                                                   FNH2
                                                                                                   FNM2
       V MUST BE STORED IN WORD POSITION 403 OF UNLABELED COMMON. AND
                                                                                                   FNMZ
        THETK MUST BE IN POSITION 404.
                                                                                                          26
27
                                                                                                   FNH2
                                                                                                   FNM2
        FNMOD2 CALLS SUBROUTINE NMDFH WHICH CALLS AAAA AND RRRR.
                                                                                     RRRR
                                                                                                   FNM2
       CALLS AAAA AND MMMM. ALL THESE SUBROUTINES ARE DESCRIBED ELSE-
WHERE IN THIS SERIES.
                                                                                                   FNH2
                                                                                                          29
                                                                                                  FNH2
                                                                                                           30
                                                                                                  FNM2
  CALLING SEQUENCE
                                                                                                  FNM2
                                                                                                  FNM2
                                                                                                          33
                                                                                                  FNM2
FNM2
       COMMON CM114021.V.THETK
                                                                                                          34
        DWFGA = XXX
                                                                                                  FNM2
                                                                                                          36
                                                                                                  FNM2
FNM2
c
        THETK . XXX
        FUNCTH = FNMCD2(OMEGA)
                                                                                                          38
                                                                                                  FNH2
  INPUTS
                                                                                                  FNM2
                                                                                                          40
                                                                                                  FNM2
                                                                                                          41
                    PHASE VELOCITY (KM/SEC).
                                                                                                  FNH2
                                                                                                          43
                                                                                                  FNH2
                                                                                                          44
45
       04EGA
                    ANGULAR FREQUENCY (RADIANS/SEC).
                                                                                                  FNM2
         R#4
                                                                                                  FNM2
                                                                                                  FNM2
       THETK
                    PHASE VFLOC'YY DIRECTION MEASURED COUNTER-CLOCKWISE FROM
                                                                                                  FNH2
         R=4
                    X-AXIS.
                                                                                                  FNM2
                                                                                                          49
                                                                                                  FNM2
                                                                                                          50
  OUTPUTS
                                                                                                  ENH?
                                                                                                          51
                                                                                                  FNM2
                                                                                                          52
      THE ONLY OUTPUT IS THE VALUE OF THE NGRMAL MODE DISPERSION FUNCTION FOR THE VALUES OF \nu_{\star} omega. And theth which have seen input.
                                                                                                          54
55
                                                                                                  FNH2
                                                                                                  FN#2
                          ----PROGRAM FOLLOWS BELOW----
000
                                                                                                  FMM2
                                                                                                          57
                                                                                                  FNHZ
                                                                                                          58
                                                                                                  FNM2
       FUNCTION ENHADZEDMEGAT
                                                                                                  FNM2
                                                                                                          60
C
                                                                                                  FNM2
        DIMENSION CI(100).VX1(100).VYI(100).HI(100)
COMMON IMAX.CI.VXI.VYI.HI.OMEGAC.VPHSEC.THETK
                                                                                                  FNM2
                                                                                                          62
                                                                                                  FNM2
                                                                                                          63
                                                                                                  FNH2
C V AND THETK OBTAINED FROM COMMON
                                                                                                  FNM2
                                                                                                          65
        V = VPHSEC
                                                                                                  FNM2
                                                                                                               PROGRAM
                                                                                                          66
        CALL NADENIOMEGA. V . THETK. L. FPP. KI
                                                                                                  FNM2
                                                                                                          67
                                                                                                                 FN#CD2
        FNMOD2 = FPP
                                                                                                  FNM2
                                                                                                          68
69
        RETURN
                                                                                                                   PAGE
        FND
                                                                                                  FNM2
                                                                                                          70
```

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LNGT
         LNGTHN (SUBROUTINE)
                                                               7/19/68
                                                                                                                 LNGT
C.
                                                                                                                  LNGT
                               ----ABSTRACT----
                                                                                                                 INGT
                                                                                                                 LNGT
                                                                                                                  LNGT
   TITLE - INGTHN
             LENGTHEN THE MATRIX INMODE BY ADDING KL ROWS BETWEEN THE NI AND
                                                                                                                 INGT
                                                                                                                 I NGT
                                                                                                                 LNGT
                       LINGTHM ADDS KL ELEMENTS TO THE VECTOR OF PHASE VELOCITIES
                       V. DIVIDING THE INTERVAL BETHEEN V(NI) AND V(NI+1) INTO KL+1 EQUAL PARTS. FOR EACH NEW PHASE VELOCITY. A NEW ROW IS ADDED TO THE INMODE MATRIX (DEFINED IN SUBROUTINE MPOUT). INMODE IS STORED COLUMN BY COLUMN IN VECTOR FORM
                                                                                                                 LNGT
                                                                                                                 LNGT
                                                                                                                 LNGT
                                                                                                                 LNGT
                                                                                                                          15
                   - FORTRAN IV (360, REFERENCE MANUAL C28-6515-4)
- J.W.POSEY, M.I.T., JUNE-1968
                                                                                                                 LNGT
                                                                                                                          16
   LANGUAGE
                                                                                                                  LNGT
   AUTHOR
                                                                                                                 LNGT
                                                                                                                          18
                                                                                                                 LNGT
                                                                                                                 LNGT
                               ----IISAGE----
                                                                                                                 LNGT
          OM. V. INMODE MUST BE DIMENSIONED IN THE CALLING PROGRAM
                                                                                                                          22
                                                                                                                 LNGT
                                                                                                                          23
          NMOFN IS ONLY SUBROUTINE CALLED
                                                                                                                 LNGT
                                                                                                                          25
   FORTRAN USAGE
          CALL LAGTHA (OM. V. INMODE, NOM, NVP. NVPP. N1. KL. THETK)
                                                                                                                 LNGT
                                                                                                                  LNGT
                                                                                                                  LNGT
                                                                                                                          28
   INPUTS
                                                                                                                 LNGT
                                                                                                                          29
                       VECTOR WHOSE ELEMENTS ARE THE VALUES OF ANGULAR FREQUENCY CORRESPONDING TO THE COLUMNS OF THE INMODE MATRIX.
                                                                                                                 LNGT
                                                                                                                          30
        ON
                                                                                                                  LNGT
           R#4(0)
                                                                                                                  LNGT
                                                                                                                          32
                       VECTOR WHOSE ELFMENTS ARE THE VALUES OF PHASE VELOCITY CORRESPONDING TO THE ROWS OF THE INMODE MATRIX.
                                                                                                                  LNGT
                                                                                                                          33
           8*4(0)
                                                                                                                 LNGT
                                                                                                                          35
                       EACH ELEMENT OF THIS MATRIX CORRESPONDS TO A POINT IN THE FREQUENCY (OM) - PHASE VELOCITY (V) PLANE. IF THE NORMAL MODE DISPERSION FUNCTION (FPP) IS POSITIVE AT THAT POINT. THE ELEMENT IS +1. IF FPP IS NEGATIVE, THE ELEMENT IS -1, IF FPP DOES NOT EXIST. THE ELEMENT IS 5. INMODE HAS NVP ROWS (INCREASED TO NVPP) AND NOM COLUMNS. MATRIX IS STORED IN VECTOR FORM COLUMN AFTER COLUMN. THE NUMBER OF ELEMENTS IN OM.
                                                                                                                 LNGT
         INMODE
                                                                                                                          36
           144(0)
                                                                                                                 LNGT
                                                                                                                          38
                                                                                                                 LNGT
                                                                                                                          39
                                                                                                                 LNGT
                                                                                                                           40
                                                                                                                  LNGT
 C.
                                                                                                                 LNGT
                                                                                                                          42
 Č
                                                                                                                 LNGT
         NOM
            144
                                                                                                                  LNGT
                                                                                                                          44
         NVP
                        THE NUMBER OF ELEMENTS IN V (WHEN LNGTHN IS CALLED).
                                                                                                                 LNGT
                                                                                                                  LNGT
 C,
           1+4
                        NUMBER OF INMODE ROW IMMEDIATELY ABOVE SPACE IN WHICH NEW
                                                                                                                 LNGT
         N1
 Ç
            1 *4
                        ROWS ARE TO BE ADDED
                                                                                                                 LNGT
                                                                                                                          48
                                                                                                                  LNGT
                      NUMBER OF ROWS TO BE ADDED
                                                                                                                  LNGT
         KL
            1 84
                                                                                                                 LNGT
                                                                                                                          51
                                                                                                                 LNGT
LNGT
                        PHASE VELOCITY DIRECTION (RADIANS)
         THETK
            R#4
                                                                                                                 LNGT
LNGT
                                                                                                                          54
                                                                                                                           55
    OUTPUTS
                                                                                                                  LNGT
         THE OUTPUTS ARE NVPP (= NVP + KL) AND REVISED VERSIONS OF V AND
                                                                                                                 LNGT
LNGT
                                                                                                                           57
         INMODE.
                                                                                                                  LNGT
                                                                                                                  LNGT
                                                                                                                          60
                                                                                                                  LNGT
                                ----EXAMPLE----
                                                                                                                  LNGT
                                                                                                                           62
                                                                                                                  LNGT
         VALUES OF INMODE NOT VALID -- FOR ILLUSTRATION PURPOSES ONLY
                                                                                                                           63
                                                                                                                  LNGT
                                                                                                                  LNGT
                                                                                                                           65
                        V=1.0.2.0
                                                                                                                                 PROGRAM
                        OM=1.0.2.0
                                                                                                                          66
                                                                                                                           67
                        INMODE=1.-1.-1.1
CALL LNGTHN(OM.Y.INMODE.2.2.NVPP.1.3.THETK)
                                                                                                                                  LNGTHN
                                                                                                                  LNGT
                                                                                                                  INGT
                                                                                                                                     PAGE
                 UPON RETURN TO CALLING PROGRAM THE VALUES OF V AND NVPP ARE
                                                                                                                  LNGT
                                                                                                                                         30
```

```
V=1.0.1.25.1.5.1.75.2.0
                                                                                                           LNGT
              NVPP=5
INMODE WILL BE OF THE FORM
                                                                                                            LNGT
c
                                                                                                           LNGT
                                                                                                                    73
                     IMMODE=1.7.7.7.7.-1.-1.7.7.7.1
THE Y'S ARE NEW ELEMENTS, FACH OF WHICH MAY BE -1. 1.
                                                                                                           LNGT
                                                                                                            LNGT
                                                                                                                    76
77
               OR 5
                                                                                                            LNGT
                                                                                                           LNGT
                                                                                                           LNGT
               ORIGINAL MATRIX
                                                          EXPANDED MATRIX
                                                                                                            LNGT
                                                                                                           LNGT
LNGT
                                                                                                                    80
Ċ
                                                                    YY
                                                                                                           LNGT
LNGT
                                                                    77
Ċ.
                                                                                                           LNGT
                                                                                                           LNGT
                                                                                                                    86
                             ----PROGRAM FOLLOWS BELOW----
                                                                                                           LNGT
                                                                                                                    87
                                                                                                           LNGT
                                                                                                           LNGT
                                                                                                           LNGT
LNGT
         SUBROUTINE LINGTHNIOM.V. INMODE. NOM. NVP. NVPP.N1.KL. THETK)
                                                                                                                    90
C VARIABLE DIMENSIONING
                                                                                                           LNGT
DIMFNSION OM(1).v(1).inmode(1)

COMMON IMAX.CI(100).vXI(100).vYI(100).HI(100)

DELVP = (V(NI+1)-V(NI)) / (KL+1)

C DELPP IS THE INTERVAL OF PHAS VELOCITIES FOR THE ADDED ROWS.

NVPP = NVP > KL
                                                                                                           LNGT
                                                                                                           LNGT
                                                                                                           LNGT
                                                                                                           LNGT
                                                                                                           LNGT
                                                                                                           LNGT
C NVPP IS THE NEW NUMBER OF ROWS IN THE TOTAL MATRIX.
C C N2 IS NEW NUMBER OF CLD RCW NO. (N1+1)
                                                                                                           LNGT
                                                                                                                    90
                                                                                                           LNGT 100
                                                                                                           LNGT 101
C
                                                                                                           LNGT 102
C SHIFT OLD VALUES OF V(I) IN LOWER ROWS TO I+KL SPOT9 ONE HAS TO C SHIFT THE NVP ELEMENT FIRST. NOTE THAT I RANGES FROM NVPP TO N2 ODWNWARD WHILE I-KL RANGES FROM NVP TO N1+1.

On 71 IP =N2,NVPP
I = NVPP - (IP-N2)
                                                                                                           LNGT 103
                                                                                                           LNGT 104
                                                                                                           LNGT 105
                                                                                                           LNGT 106
                                                                                                           LNGT 107
     71 V(1) = V(1-KL)
                                                                                                           LNGT 108
                                                                                                           LNGT 109
C NEW VALUES OF VP ARE INSERTED INTO V
                                                                                                           LNGT 110
     DO 72 IP=1-KL
I = N1 + IP
72 V(I) = V(N1) + IP+DELVP
                                                                                                           LNGT 111
                                                                                                           LNGT 112
                                                                                                           LNGT 113
                                                                                                           LNGT 114
C BEGINNING AT THE RIGHT INMODE IS LENGTHENED COLUMN BY COLUMN
                                                                                                           LNGT 115
         DO 90 JP=1.NOM
J = NOM - (JP-1)
DO 90 [P=1.NVPP
                                                                                                           LNGT 116
                                                                                                           LNGT 117
                                                                                                           LNGT 118
         I = NVPP- ([P-1]
                                                                                                           LNGT 119
                                                                                                           LNGT 120
\tilde{c} THE 1J ELEMENT IN THE INMODE VECTOR IS THE J ELEMENT IN THE I ROW OF C THE NEW INMODE MATRIX
                                                                                                           LNGT 121
                                                                                                           LNGT 122
         IJ = (J-1)*NVPP + I
                                                                                                           LNGT 123
                                                                                                           LNGT 124
C IF I CORRESPONDS TO A NEW ROW INMODELLY) MUST BE DETERMINED FROM NMDFN IF (I-GT-N1-AND-I-LT-N2) GO TO 9
                                                                                                           LNGT 126
                                                                                                           LNGT 127
C IJOLD IS NO. OF ELEMENT IN OLD INMODE VECTOR WHICH IS TO BE MOVED INTO C IJ POSITION OF NEW VECTOR IJOLD = (J-1)*NVP + I
                                                                                                          LNGT 128
                                                                                                           LNGT 129
C NOTE THAT IOLD IS ALWAYS I IF I .LT. NI BUT IOLD IS I-KL IF I .GE. N2.
C IJOLD IS COMPUTED ON THE MASIS OF NVP RATHER THAN NVPP ROWS.

IF (I.GE.N2) IJOLD = IJOLD - KL
INMODE(IJ) = INMODE(IJOLD)
                                                                                                          LNGT 131
                                                                                                          LNGT 132
                                                                                                           LNGT 133
                                                                                                          LNGT 134
LNGT 135
         GO TO 80
                                                                                                                         PROGRAM
                                                                                                          LNGT 137
LNGT 138
      9 CALL NMDFN(OM(J) .V(I) .THETK.L.FPP.K)
                                                                                                                          LNGTHN
PAGE
```

A CONTRACTOR OF THE PROPERTY O

LNGT 140

> PROGRAM LNGTHN

```
HMMM
                                                    7/25/68
C
       MMMM (SURROUTINE)
                                                                                              -
                        ----ARSTPACT----
                                                                                             -
                                                                                              MMMM
                                                                                             MMMM
  TITLE - 4MM4
           THIS SUBROUTINE COMPUTES THE 2-BY-2 TRANSFER MATRIX EF WHICH
                                                                                             MMMM
           CONNECTS THE SOLUTIONS OF THE RESIDUAL EQUATIONS AT THE TOP OF A LAYER TO THOSE AT THE BOTTOM OF THE LAYER BY THE RELATIONS
                                                                                             MMMM
                                                                                             HMMM
                PHII(78)= FM(1.1)*PHII(Z8+H)+ EM(1.2)*PHI2(Z8+H)
                                                                                             ---
                                                                                             HMMM
                                                                                                     11
                                                                                              -
                PHI2(ZB)= EM(2.1)*PHI1(ZR+H)+ EM(2.2)*PHI2(ZB+H)
                                                                                              MMMM
           WHERE IR DENOTES THE HEIGHT OF THE BOTTOM OF AN ISOTHERMAL
                                                                                             MMMM
                                                                                                     14
           LAYER (THICKNESS H) WITH CONSTANT WINDS. THE QUANT PHIL(7) AND PHIL(2) SATISFY THE RESIDUAL EQUATIONS.
                                                                                             MMMM
                                                                THE QUANTITIES
                                                                                              ммми
                                                                                             MMMM
                                                                                              O(PHI1)/O7 = A(1-1)*PHI1(7) + A(1-2)*PHI2(7)
                                                                                             -
                                                                                              MMMM
                                                                                                     20
               D(PHI2)/DZ = A(2.1)*OHI1(Z) + A(2.2)*PHI2(Z)
                                                                                              MMMP
           WHERE THE A(I.J) ARE CONSTANT OVER THE LAYER AND WHERE A(2.2)=-A(1.1). ON THIS BASIS. ONE CAN SHOW THAT
                                                                                             MMMM
                                                                                             -
                                                                                             MMMM
                                                                                              -
               FM(1.J) =CAI(X)*KDELTA(1.J)-H*SAT(X)*A(1.J)
                                                                                              MMMM
                                                                                             -
           WHERF
                                                                                             MMMM
                       X = (&{1,1)**?+&(1,2)*A(2,1))*H**?
                                                                                              -
           AND WHERE KOFLTA(I.J) IS THE KRONECKER DELTA (1 IF INDICES
                                                                                             ---
                                                                                                     30
           FOUAL. O OTHERWISE). THE FUNCTIONS CAL AND SAT ARE DEFINED THE DESCRIPTIONS OF THE CORRESPONDING FUNCTION SURPROGRAMS.
                                       THE FUNCTIONS CAL AND SAL ARE DEFINED IN
                                                                                             MMMM
                                                                                             MMMM
                                                                                              MMMM
           THE MATRIX A IS COMPUTED FOR GIVEN FREQUENCY, WAVE NUMBER. SOUN SPEED. AND WIND VELOCITY BY CALLING SUBROUTINE AAAA.
                                                                                             MMMM
                                                                                             MMMM
                                                                                              мммм
                - FORTRAN IV (360. PFFFRENCE MANUAL C28-6515-4)
                                                                                             MMMM
  LANGUAGE
                                                                                             MMMM
                                                                                                     38
                                                                                              -
  AUTHOR
                 - A.D.PIFRCE. M.I.T., JULY-1968.
                                                                                             MMMM
                                                                                                     40
                                                                                             MMMM
                        ----CALLING SEQUENCE----
                                                                                              -
       SUBROUTINES NAMPDE. PRRR
                                                                                             MMMW
                                                                                             MMMM
        DIMENSION EM(2.2)
                                                                                             MMMM
        CALL MMMM (OMEGA. AKX. AKY. C. VX. VY. H.EM)
                                                                                              MMMM
                        ----EXTERNAL SUBROUTINES REQUIRED----
                                                                                             MMMM
                                                                                              MMMM
                                                                                             MMMM
        AAAA, CAI. SAI
                                                                                             MMMM
                                                                                                     50
                        ---- ARGUMENT LIST----
                                                                                              MMMM
                                                                                              MMMM
                                                                                             MMMM
        OMEGA
                      R * 4
                               NO
                                      INP
                                                                                              MMMM
                      R#4
                                      INP
        AKY
                               ND
                                       INP
                                                                                             мммм
        AKY
                                                                                                     56
57
                      R +4
                               NO
                                      INP
                                                                                              MMMM
                                                                                              MMMM
                      R 44
                                       INP
        ٧x
                               ND
                      R#4
                                       INP
                                                                                             MMMM
                               ND
                                                                                              MMMM
                                                                                                     59
                      2 *4
                               ND
                                       INP
                                                                                              MMMM
                      R *4
                             2-8Y-2
                                      OUT
                                                                                              -
                                                                                              MMMM
   NO COMMON STORAGE IS USED
                                                                                                     62
                                                                                              MMMK
                        ----INPUTS----
                                                                                              MMMM
                                                                                              ММММ
                       FANGULAR FREQUENCY IN RADISEC
                                                                                              MMMM
                                                                                                          PROGRAM
        OMEGA
                       EX COMPONENT OF HORIZONTAL WAVE NUMBER VECTOR IN 1/KM EY COMPONENT OF HORIZONTAL WAVE NUMBER VECTOR IN 1/KM ESOUND SPEED IN KM/SFC
                                                                                              -
                                                                                                     47
                                                                                                            MMMM
                                                                                              мммм
        AKY
                                                                                                     68
                                                                                              -
                                                                                                              PAGE
                        EX COMPONENT OF WIND VELOCITY IN KM/SEC
                                                                                              MMMM
                                                                                                     70
                                                                                                                33
```

-116" -- -

-237-

```
YY
H
                           *Y COMPONENT OF WIND VELOCITY IN KM/SEC *THICKNESS IN KM OF LAYER
                                                                                                              MMMM
                                                                                                              MMMM
                                                                                                                      72
73
74
                                                                                                              -
                            ----NUTPUTS----
                                                                                                              ММММ
                                                                                                                      75
76
77
                                                                                                              MMMM
                           =2-BY-2 TRANSFER MATRIX WHICH RELATES THE SOLUTIONS OF THE PESIDUAL EQUATIONS AT THE TOP OF A LAYER TO THOSE AT THE BOTTOM OF THE LAYER
         FH
                                                                                                             MMMM
                                                                                                                      78
79
                                                                                                             MMMM
                                                                                                             MMMM
                            ----PROGRAM FOLLOWS BELOW----
                                                                                                             MMMM
                                                                                                                      80
ŗ
                                                                                                             мини
         SUBROUTINE MMMM(OMEGA.AKX.AKY.C.VX.VY.H.EM)
                                                                                                             MMMM
                                                                                                                      82
                                                                                                             MMMM
                                                                                                                      83
84
         DIMENSION A(2.2) . EM(2.2)
                                                                                                             -
C COMPUTE A(1+J)+ CAI(X)+ AND SAI(X)
CALL AAAA(OMEGA+AKX+AKY+C+VX+VY+A)
                                                                                                             MMMM
                                                                                                             MMMM
                                                                                                                      86
                                                                                                             MMMM
                                                                                                                      87
         X={At1,1}**2+A(1,2)*A(2,1)}*H**2
CA=CAT(X)
                                                                                                             MMMM
                                                                                                             MMMM
                                                                                                                      99
90
         SA=SAI(X)
                                                                                                             MMM
C COMPUTE THE TERMS -H*SAT(X)*A(I,J)
                                                                                                             MMMM
                                                                                                                      92
                                                                                                             MMMM
    TA=H*SA

DO 90 !*1.2

DO 90 J=1.2

90 FM([,J]=-TA*A([,J])
                                                                                                             MMMM
                                                                                                                      94
95
                                                                                                             MMMM
                                                                                                             MMMM
                                                                                                                      96
97
C ADD IN CAI(x)=KDELTA(I.J) TERMS BY ADDING CA TO DIAGONAL ELEMENTS
DO 190 I=1.2
190 EM(I.I)=EM(I.I)+CA
                                                                                                             MMMM
                                                                                                             MMMM
                                                                                                                      98
                                                                                                                      99
                                                                                                             MMMM 100
                                                                                                             MKMM 101
MMMM 102
MMMM 103
         RETURN
         FND
```

PROGRAM MMMM

```
MOTR
                 MODETR (SUBROUTINE)
                                                                                                                     6/75/68
                                                                                                                                                                                                                    MOTE
                                                                                                                                                                                                                    MOTP
                                                      ----ABSTRACT----
                                                                                                                                                                                                                    MOTR
                        PROGRAM TO TABULATE A TABLE OF PHASE VELOCITY VERSUS FREQUENCY FOR A GIVEN GUIDED MODE. THE NORMAL MODE DISPERSION FUNCTION IS 7ERO FOR EACH LISTING OF THE TABLE. THE COMPUTATIONAL METHOD IS BASED ON THE PREVIOUSLY COMPUTED VALUES OF THE NMDF SIGN INMODE(J-1)**PROW+1) AT POINTS (1, J) IN A RECTANGULAR ARRAY OF NROW ROWS AND NCOL COLUMNS. DIFFERENT COLUMNS (J) CORRESPOND TO DIFFERENT FREQUENCIES WHILE DIFFERENT ROWS (I) CORRESPOND TO DIFFERENT PHASE VELOCITIES. DISPERSION CURVES OF VARIOUS MODES APPEAR ON THIS ARRAY AS LINES OF OFMARCATION BETWEEN ADJACENT REGIONS WITH DIFFERENT INMODES. TWO ADJACENT POINTS WITH INMODES OF OPPOSITE SIGN BRACKET A POINT ON THE ACTUAL DISPERSION CURVE. IF THE POINTS CORRESPOND TO THE SAME FREQUENCY. THEN THE PHASE VELOCITY CORRESPOND TO THAT OMEGA ON THE DISPERSION CURVE IS FOUND BY CALLING RTWI, A 360 PACKAGE ROUTINE FOR SOLVING NONLINEAR EQUATIONS, AND CONSIDERING THE NMOF AS A FUNCTION OF VPHSE WITH OMEGA FIXED. SIMILARLY, IF THE POINTS CORRESPOND TO THE SAME PHASE VELOCITY, THE APPROPRIA OMEGA CORPESPONDING TO THIS PHASE VELOCITY IS FOUND BY CALLING RTWI WITH THE NMOF CONSIDERED AS A FUNCTION OF OMEGA WITH VPHSE FIXED.
     TITLE - MODETR
                                                                                                                                                                                                                    MOTR
                                                                                                                                                                                                                    HOTE
                                                                                                                                                                                                                    HOTR
                                                                                                                                                                                                                    MDTR
                                                                                                                                                                                                                    MOTR
                                                                                                                                                                                                                                    10
                                                                                                                                                                                                                    MOTR
                                                                                                                                                                                                                    MOTE
                                                                                                                                                                                                                    MOTE
                                                                                                                                                                                                                                     13
                                                                                                                                                                                                                    HOTR
C
                                                                                                                                                                                                                   MOTR
                                                                                                                                                                                                                                    15
                                                                                                                                                                                                                   MOTR
Ċ
                                                                                                                                                                                                                   HOTR
                                                                                                                                                                                                                   HOTE
                                                                                                                                                                                                                   MOTP
                                                                                                                                                                                                                                    19
C.
                                                                                                                                                                                                                   MOTR
                                                                                                                                                                                                                                    20
                                                                                                                                                                                                                    MOTR
                                                                                                                                                                                                                   MOTE
                                                                                                                                                                                                                  MOTE
                                                                                                                                                                                                                                    23
                                                                                                                                                                                                                   MOTR
C
                                                                                                                                                                                                                   MOTR
                          VPHSE FIXED.
                                                                                                                                                                                                                   HOTR
                                                                                                                                                                                                                                   26
27
                                                                                                                                                                                                                   MOTR
                         THE PROGRAM SUCCESSIVELY CONSIDERS EACH PAIR OF ADJACENT POINTS WITH OPPOSITE INMODES BRACKETING A LINE OF DEMARCATION AND PROCEEDS IN THE DIRECTION OF INCREASING FREQUENCY UNDER THE
                                                                                                                                                                                                                                   28
29
                                                                                                                                                                                                                  MOTR
                                                                                                                                                                                                                   MOTR
                                                                                                                                                                                                                   MDTR
                                                                                                                                                                                                                                   30
                         ASSUMPTION THAT THE PHASE VELOCITY CURVE SLOPES DOWNWARDS.
                                                                                                                                                                                                                   MOTE
                                                                                                                                                                                                                                  32
33
                                                                                                                                                                                                                   MOTR
      PROGRAM NOTES
                                                                                                                                                                                                                   MOTR
                                                                                                                                                                                                                   MOTR
                                           THE MODES APE NUMBERED. THE INPUT INTEGER MMODE DESIGNAT
                                                                                                                                                                                                                  MDTR
                                                                                                                                                                                                                                   35
                                          WHICH MODE IS REING TABULATED. THE PAIRS OF FREQUENCY AND PHASE VELOCITY VALUES ARE STORED AS (MMODE(KST(NMODE)))
OMMOD(KST(NMODE)+1).OMMOD(KST(NMODE)+2)......
                                                                                                                                                                                                                                   36
                                                                                                                                                                                                                  MATO
                                                                                                                                                                                                                   MDTR
                                                                                                                                                                                                                                   38
                                          MMMOD(KFIN(NMODE)).VPMOD(KST(NMODE)).VPMOD(KST(NMODE)+1).
....VPMOD(KFIN(NMODE)). THE ARRAYS OMMOD AND VPMOD
                                                                                                                                                                                                                   MOTR
                                                                                                                                                                                                                                   40
                                            ARE USED TO STORF DISPERSION CURVES FOR ALL MODES.
                                                                                                                                                                                                                   MOTR
                                                                                                                                                                                                                                   41
                                          KST(NMODE) IS INPUT WHILE KFIN(NMODE) IS DETERMINED DURIN THE COMPUTATION. THE TOTAL NUMBER OF POINTS EXTRACTABLE FROM THE ARRAY OF INMODE VALUES DETERMINES KFIN-KST+1. IF A SINGLE POINT CANNOT BE CALCULATED, THE PROGRAM RETURNS KRUD=1. OTHERWISE IT RETURNS KRUD=1.
                                                                                                                                                                                                                  MOTR
                                                                                                                                                                                                                                   43
                                                                                                                                                                                                                  MOTR
                                                                                                                                                                                                                   MOTR
                                                                                                                                                                                                                                  46
47
                                                                                                                                                                                                                  MOTE
                                                                                                                                                                                                                  MOTR
                                                                                                                                                                                                                  MOTR
                                          SUBROUTINE RTHT FOR SOLVING A NONLINEAR EQUATION IS ALLOWED A MAXIMUM OF TEN ITERATIONS TO FIND THE PHASE VELOCITY TO ACCURACY OF 1.E-5 KM/SEC OR THE FREQUENCY TO FOUR SIGNIFICANT FIGURES. IF THE SEARCH IS UNSUCCESSFUL A MESSAGE IS PRINTED AND THE POINT IS
                                                                                                                                                                                                                  MDTR
                                                                                                                                                                                                                   MOTR
                                                                                                                                                                                                                                   50
                                                                                                                                                                                                                  MDTR
                                                                                                                                                                                                                  MOTR
                                                                                                                                                                                                                                   52
                                                                                                                                                                                                                  MDTR
                                           SKIPPED OVER.
                                                                                                                                                                                                                  MOTR
                                                                                                                                                                                                                  MOTR
                                                                                                                                                                                                                                  55
                                          THE INPUT PARAMETERS IST, JST ARE COURDINATES OF A POINT I THE INMODE ARRAY. THIS POINT SHOULD BE THAT POINT FURTHE TO THE UPPER LEFY OF THOSE POINTS LYING BELOW THE LINE OF DEMARCATION FOR THE MODE CONSIDERED, PROVIDING THAT POINT
                                                                                                                                                                                                                  MULE
                                                                                                                                                                                                                  MDTR
                                                                                                                                                                                                                                  58
                                                                                                                                                                                                                  HOTR
                                           DOES NOT HAVE INMODE = 5.
                                                                                                                                                                                                                  MDTR
                                                                                                                                                                                                                                  60
                                                                                                                                                                                                                  MOTR
                                                                                                                                                                                                                                  61
                                     - FORTRAN IV 1360, REFERENCE MANUAL C28-6515-41 - A.D.PIERCE, M.I.T., JUNE.1968
      LANGUAGE
                                                                                                                                                                                                                  MC TR
C
      AUTHOR
                                                                                                                                                                                                                  MITR
                                                                                                                                                                                                                                  63
                                                                                                                                                                                                                  MÈTR
                                                      ----CALLING SEQUENCE----
                                                                                                                                                                                                                  40 IR
                                                                                                                                                                                                                                             PROGRAM
                                                                                                                                                                                                                  MOTR
      SEE SURPOUTINE ALLMOD
                                                                                                                                                                                                                                 67
                                                                                                                                                                                                                  MOTR
                                                                                                                                                                                                                                                 MCDETR
                 OTMENSION KST(1), KFIN(1), OMMOD(1), VPMOD(1), INMODE(1), OM(1), VP(1)

(SUBROUTINE USES VARIABLE DIMENSIONING)

CALL MODETRIIST, JST, NMODE, KST, KEIN, CMMCD, VPMOD, NROW, NCOL, INMODE,
                                                                                                                                                                                                                  MOTR
                                                                                                                                                                                                                  MOTR
                                                                                                                                                                                                                                                      PAGE
```

MOTR

```
1 34.46.46001
                                                                                                      MDTR
     TEL KRIID . FO. 1 ) GO SOMEWHERE
                                                                                                      MDTR
                                                                                                              73
74
                                                                                                      MATA
                        ---- FXTERNAL SURROUTINGS REQUIRED ---
                                                                                                      MOTR
                                                                                                      MOTR
     NXTPNT, PTMI, FNMODI, FNMODI, NADER, AAAA, PPRP, MMMM, CAI, SAI (FNMODI AND FNMODE CALL NADER), MHICH IN TURN CALLS AAAA AND RRRR GRAR CALLS AAAA AND MMMM. DESCRIPTIONS OF THESE PROGRAMS APE
                                                                                                      MOTP
                                                                                                      MOTR
                                                                                                              77
                                                                                                      MOTR
         GIVEN FL SEWHERE IN THIS SERIES. 1
                                                                                                      MOTR
                                                                                                      MOTR
                                                                                                              8C
     RIMI IS A SUBPOUTINE CODED BY IRM TO DETERMINE A ROOT OF A GENERAL
                                                                                                      MDTR
                                                                                                              81
     NONLINEAR EQUATION F(X)=> BY MEANS OF MUELLER-S TERRATION SCHEME OF SUCCESSIVE BISECTION AND INVERSE PARABOLIC INTERPOLATION. A COMPLETE DESCRIPTION AND DECK LISTING IS GIVEN ON PAGES 198-199 OF
                                                                                                      MOTE
                                                                                                      MOTE
                                                                                                              83
                                                                                                      MOTR
                                                                                                              84
     DOCUMENT HOUDONS-2. SYSTEM/360 SCIENTIFIC SUBROUTINE PACKAGE (360A-CM-03X) VERSION 11. PROGRAMMER-5 MANUAL. IRM. TECHNICAL PUBLICATIONS DEPARTMENT, 112 FAST POST ROAD. WHITE PLAINS, N.Y.
                                                                                                      MOTR
                                                                                                     MDTR
                                                                                                      MOTR
                                                                                                              R7
     10601. PURITSHED 1966. 1967.
                                                                                                      MDTR
                                                                                                              88
                                                                                                      HOTR
                  ---- ARGUMENT LIST----
                                                                                                     MOTR
                                                                                                              90
                                                                                                     MOTP
                                                                                                              91
     151
                     1 *4
                                       INP
                                                                                                      MDTR
     151
                     1+4
                               NN
                                       TND
                                                                                                     MDTR
     NAUDE
                               งก
                                       INP
                                                                                                     MOTR
                                                                                                              94
     KST
                     1+4
                               VAR
                                        INP (ONLY KST(NMODE) NEEDED)
                                                                                                      MOTR
     KFIN
                     1 84
                                       OUT (ONLY KFINIMPONE) COMPUTED)
OUT (COMPUTED FOR N .GF. KST(NMODE))
OUT (COMPUTED FOR N .GF. KST(NMODE))
                               VAR
                                                                                                      MOTR
     OWMODINE
                               VAR
                                                                                                     MOTR
                                                                                                             97
     VPHCD (N)
                     R = 4
                               VAR
                                                                                                      MOTR
                                                                                                              98
                     I #4
     MESH
                               ND
                                       INP
                                                                                                     MOTR
     MERL
                               NO
                                       INP
                                                                                                     MDTR 100
     INMODE
                     1 *4
                                                                                                     MOTR
                                                                                                            101
     04
                     ...
                               VAP
                                       INP
                                                                                                     MDTR
     ٧P
                     9 .4
                               VAR
                                       INP
                                                                                                     MOTR
                                                                                                            103
     KRUD
                                       OUT
                                                                                                     MOTE
                                                                                                            104
                                                                                                     MOTR
COMMON STORAGE USED
                                                                                                     MOTR 106
     CHAMON IMAX.CI.VXI.VYI.HI.OMEGAC.VPHSEC.THETK
                                                                                                     MOTR
                                                                                                            107
                                                                                                     MOTP 108
     1 44 X
                                       INP
                                                                                                     MDTR 109
                     r =4
     r t
                               100
                                       INP
                                                                                                     MDTR 110
     VXI
VYI
                     0 44
                               100
                                       INP
                                                                                                     HOTE
                     R 44
                               100
                                       INP
                                                                                                     MOTR 112
                     0 #4
                               100
                                       INP
                                                                                                     MOTR 113
                                       OUT (USED INTERNALLY)
OUT (USED INTERNALLY)
     THEGAC
                    9 44
                               NΩ
                                                                                                     MOTR
                     Q +4
     VPHSEC
                               ND
                                                                                                     MOTR 115
                               ND
                                                                                                     MDTR 116
                                                                                                     HDTR
                        ----INPUTS----
                                                                                                     MOTR 118
                                                                                                     MOTR 119
                      **ROW INDEX OF START POINT, WHICH MUST LIE BELOW LINE OF DEMARCATION
     IST
                                                                                                     MOTR
                                                                                                     MDTR 121
                       SCOLUMN INDEX OF START POINT
                                                                                                     MDTR 122
                      *NUMBER LARELLING MODE TO BE TABULATED

*INDEX OF OMMOD AND VPMOD CORRESPONDING TO FIRST
POINT TABULATED.
     NMOOF
                                                                                                     MOTR
     KSTENMODES
                                                                                                     MOTR 124
                                                                                                     MDTR 125
                      #NUMPER OF ROWS IN INMODE ARRAY
#NUMBER OF COLUMNS IN INMODE ARRAY
#ARRAY WHOSE (J-1)#NROW+I-TH ELEMENT IS THE SIGN OF
     MONU
     NCO:
                                                                                                     MOTR
     INMODE
                                                                                                     MOTR
                                                                                                            128
                        THE NORMAL MODE DISPERSION FUNCTION WHEN OMEGA=OM(J).
                                                                                                     HOTR
                        VPHSF=VP([).
                                                                                                     MDTR 130
                      *VECTOR OF PHASE VELOCITIES AT WHICH INMODE IS TABULATED.
     ΩM
                                                                                                     MOTE
                                                                                                            131
     VP
                                                                                                     MOTR
                      TARM ATED. **NUMBER OF ATHOSPHERIC LAYERS OF FINITE THICKNESS.
                                                                                                     MDTR 133
     IMAX
                                                                                                     HDTR 134
                      CILLI
                                                                                                     MDTR
     VXIII
                                                                                                    MDTR 136
                                                                                                                  PROGRAM
     VY[{[]}
                                                                                                    MOTR 137
                                                                                                                    HODETR
                      "THICKNESS IN KM OF I-TH LAYER
     RICIE
                                                                                                     HDTR 138
                      *PHASE VELOCITY DIRECTION IN RADIANS W.R.T. X AXIS
                                                                                                    MOTR
                                                                                                           139
                                                                                                                       PAGE
                                                                                                     MOTE
                                                                                                                         36
```

```
MDTR 141
                      ---- CHITPHTS----
                                                                                        MOTP
                                                                                             142
                                                                                        WOTR 143
      KEIN(NMODE) = IMDEX OF OHMOD AND VPMOD CORRESPONDING TO LAST
                                                                                        HOTP
                       PRINT TARULATED.
                                                                                              145
                      =ANGINAR FREQUENCY OF POINTS ON DISPERSION CUPYE.
                                                                                        MOTP
      OMMODINE
                       N=KST(NMODE) UP TO KEIN(NMODE) CORRESPONDS TO NMODE-
                                                                                       MDTR 146
                                                                                             147
                                                                                        MATR
                      MODE. =PHASE VELOCITY OF POINTS ON DISPERSION CURVE.
                                                                                        MOTP
      VPMODENT
                       N=KST(NMODE) UP TO KEIN(NMODE) CORRESPONDS TO NMODE-
                                                                                       MOTO 149
                                                                                       MDFR 150
                      #FIAG INDICATING IF ANY POINTS OF DISPERION CURVE HAVE BEEN FOUND. 1 IF YES. -1 IF NO. #INTERNALLY USED FREQUENCY TRANSMITTED AMONG SUB-
                                                                                        ₽DTR
      KRUD
                                                                                        MOTR
      OMEGAC
                                                                                       MOTE
                                                                                             153
                                                                                        MOTP
                      ROUTINES THROUGH COMMON ** INTERNALLY USED PHASE VELOCITY TRANSMITTED AMONG
      VPHSEC
                       SUBROUTINES THROUGH COMMEN.
                                                                                       MOTP
                                                                                             156
                                                                                       MDTR 157
                                                                                       ATON
                      ----EXAMPL F----
                                                                                             159
                                                                                        MOTO
                                                                                       HOTR 160
      SUPPOSE THE TABLE OF INMODE VALUES IS AS SHOWN BELOW WITH
                                                                                        MN TR
                                                                                             161
                                                                                       4019
                              NROW=7. NCOL=14
          ******
                                                                                        MDTR 163
                              NM=.1..2..3..4..5..6..7..8..9.1.0.1.1.1.2.1.3.
                                                                                       MDTR
          ---++++++++
                                                                                             164
                                                                                       MOTR 166
                                                                                       MOTR 167
                              VP=.5..45..40..35..30..25..20
                                                                                        MNTR 168
          ***-----
                              NMODE=2. IST=3. JSY=1. KST(L)=7
                                                                                       MDT: 169
                                                                                       MO.R
                                                                                             170
                                                                                        W.TR
                                                                                             171
      THEN OVE MIGHT FIND KRUD=1. KFIN(2)=23. AND
                                                                                       40TR 172
          1.=47}0CMMU
                           VPHOD(7)*.43
                                                OMPOD(16)=.75 VPMPD(16)=.3
                                                                                       MOTP
                                                                                             173
                                                OHMOD(17)=.8 VPMOD(17)=.29
OMMOD(18)=.9 VPMOD(18)=.28
                                                                                             174
                           VPM00(8)=.42
                                                                                       MDTR
          OMMODIA1=.2
                           VPMDD(9)=.41
                                                                 VPMOG(181=.285
                                                                                       MOTR 175
          OH410(10)=.33 VPM0D(10)*.4
                                                OMMOD(19)=1.0 VPMOD(19)=.24
                                                                                       MDTR 176
                                                OMMOD(20)=1.1 VPMOD(20)=.27
CHMCD(21)=1.7 VPMOD(21)=.265
                                                                                       HOTP
                                                                                             177
          GMMGD(11)=+36 VPMGD(11)=+35
                                                                                       POTR 178
          0M4731121=.40
                          VPMOD(12)=.34
                                                OMMOD(22)=1.3 VPMOD(22)=.26
                                                                                       MOTR
          OMMOD(13)=.50 VPMOD(13)=.33
                                                                                             179
                                                OMMOD(23)=1.4 VPMOD(23)=.255
          JMMJJ(14)=.50 VPMJD(14)=.32
                                                                                       MOTR
                                                                                             180
                                                                                       MOTR
          OMMODE151=.70 VPMOD(151=.3
                                                                                       MOTR
                                                                                             192
                                                                                       MOTP
                                                                                             183
                      --- PROGRAM FOLLOWS BELOW----
                                                                                        HDTR
                                                                                       MOTR 185
                                                                                        4DTR 186
       SUBROUTINE MODETRIIST. JST. NMODE, KST. KEIN. OMMOD. VPMOC. NROW. NCOL.
      1 I'M "F.OM. VP. KRUD)
                                                                                       MOTP
                                                                                             188
                                                                                       HDTR 189
C
       DIMENSION CITIOD: VXI(100).VYI(100).HI(100)
DIMENSION KST(1).KEIN(1).OMMOD(1).VPMOD(1).INMODE(1).OM(1).VP(1)
COMMON IMAX.CI.VXI.VYI.HI.CMEGAC.VPHSEC.THE*K
                                                                                        MDTR
                                                                                       4DTR 191
                                                                                        ■DTR 192
                                                                                        HOTE
                                                                                             194
C FUNCTIONS ENMODE AND ENMODE ARE USED AS ARGUMENTS OF RIMI
                                                                                       MOTO
                                                                                             195
       EXTERNAL FNMOD1 . FNMOD2
                                                                                       MOTR
  INDEX OF FIRST POINT ON DISPERSION CURVE IS LARELLED AS K
                                                                                       MOTR
                                                                                             197
       K=KST(NMONE)
                                                                                        HOTR 198
                                                                                             199
       IN=INMODE(: JST-1 )*NROW+IST)
                                                                                       40TR 200
                                                                                        HOTP
  WE CHECK IN SEE IF POINT ABOVE (IST. JST) HAS A DIFFERENT INMODE
                                                                                       MDTR 202
       IF(1ST .40. 1) GO TO A
IUP=TMMODE((UST-1)#MROW+1ST-1)
                                                                                       MOTR 203
                                                                                        MDTR 704
       IFITUP .FO. -101 GO TO 10
                                                                                       MPTR 205
                                                                                       HDTR 206
HDTR 207
                                                                                                   PROGRAM
C IF IT BOESNT, WE CHECK THE POINT ON THE RIGHT. WE CAN ALSO ARRIVE AT
                                                                                                    MCDETR
  5 FROM 2 15 [ST#].
5 [F(JST .FO. NCOL) GO TO B
                                                                                       MOTR 208
                                                                                        MDTP 209
                                                                                                       PAGE
37
       ISID=[NHODE ( (JST )*NROW+ 15T)
                                                                                        MDTR 210
```

```
IF(ISIN .FO. -10) GO TO 15
                                                                                                   MOTR 211
                                                                                                   MDTR 212
C IF WE ARRIVE AT 8. WE CANNOT FIND A POINT EITHER ABOVE OF TO THE PIGHT C OF (157.JST) WHICH HAS A INMODE OF OPPOSITE SIGN.
                                                                                                  MDTP 213
                                                                                                   MDTR 214
                                                                                                         215
     8 KRUD=-1
                                                                                                   MATP
                                                                                                   MDTR 216
                                                                                                   MOTR 217
THE ASSIGN A TYPE INDEX TO THE POINT (IST. JST). SEE DESCRIPTION OF C NYTENT EOP DEFINITION OF TYPE INDEX.
                                                                                                   MOTE 218
MOTE 219
                                                                                                   MOTE
                                                                                                   MOTP 221
C OPPOSITE SIGN ABOVE
                                                                                                   MOTR 222
                                                                                                   4DTR 223
                                                                                                  MOTR 224
MOTR 225
C
    15 1TYP1=2
                                                                                                   MDTP
                                                                                                        226
C OPPOSITE SIGN TO RIGHT
                                                                                                   MOTR 227
C WE NOW CAN IDENTIFY OUR FIRST BRACKETING
                                                                                                   MDTR 228
                                                                                                         229
                                                                                                  MOTE
    20 II+15T
                                                                                                         230
        JI=JST
                                                                                                  MDTR 231
MDTR 232
  STATEMENT 25 IS START OF LOOP TERMINATING AT 19.. FACH PASSAGE THROUG LOOP GENERATES A NEW POINT ON THE DISPERSION CUPVE. 25 IF(ITYPL .EQ. 2) GO TO 50
                                                                                                   MDTR 233
                                                                                                  MOTR
                                                                                                  MDTR 235
C CALCULATION IF ITYPE 1. STORE C CITY WITHIN BRACKETED INTERVAL.
                                                                                                   MDTR 236
                                   STORE FREQUENCY IN COMMON. FIND PHASE VELO-
                                                                                                  MOTR 237
        OMEGAC=OMEJ11
                                                                                                  MOTR 238
        VDOWN=VP([])
VUP=VP([]-1)
                                                                                                  HDTR 239
                                                                                                   MDTR 240
        EPS=1.E-4
                                                                                                  MDTR 241
        CALL RIM! (VA.F.FRMODI. VNOWN. VUP. EPS. 4, TER)
                                                                                                  MDTR 242
        OMMOD(K)=OMEGAC
                                                                                                  MDTR 243
        VPM(1) (K) = V4
                                                                                                  MDTR 244
        GO TO 100
                                                                                                  MDTR 245
                                                                                                  MDTR 246
  CALCULATION IF ITYPE=2. STORE PHASE VELOCITY IN COMMON. FIND FREQUEN
   IN ARACKETED INTERVAL.
50 VPHSEC=VP(11)
                                                                                                  MDTR 248
                                                                                                  MDTR 249
        "HLFF=CH(J1)
        OMRIT=04(J1+1)
                                                                                                  MDTR 251
                                                                                                  MOTR 252
        EPS=[1_E-4]+0MP[T
        CALL RTMI (OMA.F. FNMOD2.OMLFF. DMRIT.EPS.4.IER)
                                                                                                  MDTR 253
         JMMJD (K) = DMA
                                                                                                  MDTR 254
                                                                                                  MOTR 255
        YPHODIK 1 = VPHSEC
                                                                                                   MDTR 256
c
   100 CONTINUE
                                                                                                  MOTR 257
C WE HAVE NOW FOUND THE K-TH POINT. WE DO NOT YET KNOW IF THIS IS THE C FINAL POINT FOR THE NHODE-TH MODE. HOWEVER, WE SET KEIN(NMODE)=K
                                                                                                  MDTR 258
                                                                                                  MDTR 259
  KF1 MMODET=K

KF1 MMODET=K

WHEN THE SURPOUTINE RETURNS. THE CURRENT STORED KFININMODE) WILL BE
                                                                                                  MDTR 260
                                                                                                  MDTR 261
   THE CORRECT ONE.
                                                                                                  MDTR 262
                                                                                                  HDTR
  WE NOW PREPARE THE SEARCH FOR THE NEXT POINT.
                                                                                                  MDTR 264
MDTR 265
   179 CALL NXTPNT(11.J1.ITYP1.12.J2.ITYP2.NROW.NCOL.INMODE.KUDOS)
180 IFF KUDOS .EQ. -1; GO TO 200
                                                                                                  MDTR 266
                                                                                                  MDTR 267
MDTR 268
        11=12
         JI = JZ
                                                                                                  MDTR 269
                                                                                                  MOTR 270
MOTR 271
         ITYP1=ITYP2
   190 GO TO 25
                                                                                                  MOTR
                                                                                                  MDTR 273
MDTR 274
   WE CONTINUE HERE AFTER AN UNSUCCESSFUL ATTEMPT TO FIND THE NEXT POINT.
   PROVIDING WE HAVE FOUND AT LEAST ONE POINT, WE CAN EXIT WITH KRUD=1.

1F( K .LF. KST(NMODF) ) GO TO 8
                                                                                                  MOTR
                                                                                                  MDTR 276
                                                                                                                PROGRAM
                                                                                                  MDTR 277
MDTR 278
                                                                                                                 MODETR
        KRUD#1
        RETURN
                                                                                                  MDTR 279
MDTR 280
                                                                                                                   PAGE
38
٢
```

END

```
MODEST (SUBROUTINE)
                                                         6/19/48
                                                                                                        MOL I
                                                                                                       MOLT.
                                                                                                        MDL T
                            ----ABSTRACT----
                                                                                                        MOLT
                                                                                                       MDL T
                                                                                                        POLT
  TITLE - MODEST
                                                                                                       MOLT
            TABULATION OF SELECTED POINTS ON THE PHASE VELOCITY (VIHSE) VS. ANGULAR EREQUENCY (OMEGA) CURVES OF SELECTED MODES
                                                                                                       MDL T
                                                                                                       MOLT
                                                                                                        MOL T
                    NO COMPUTATION OR CHANGING OF UNITS IS PERFORMED BY SUB-ROUTINE MODEST, IT MERELY PRINTS OUT THE INPUT IN LABELED AND ORGERED FASHION.
                                                                                                       MDL T
                                                                                                       MOL T
                                                                                                       MOLT
  LANGUAGE
                 - FORTRAN IV 1360. REFERENCE MANUAL C24-4515-41
                                                                                                       4DLT
                                                                                                       POLT.
  AUTHERS
                  - A.D.PIERCE AND J.POSEY, M.I.T., JUYE, 1964
                                                                                                       POL T
                                                                                                       YOLT
MOLT
                           ----IJSAGE----
                                                                                                       MDL T
                                                                                                                20
                                                                                                       MDL T
       NO SUBROUTINES ARE CALLED.
                                                                                                       MDL T
                                                                                                       MD L.T
       KEIN, CHMOD, VPMOD, KST WILL ASSUME THE DIMENSIONS SPECIFIED IN THE CALLING PROGRAM. (DIMENSION OF KST AND KEIN MUST HE .CE. NMEN
                                                                                                       4DL T
                                                                                                       POLT
                                                                                                       MOLT
  FORTRAN USACE
                                                                                                       MDLT
                                                                                                       MDL T
       CALL MODEST (MDFND, DMMDD, VPMOD, KST, KFIN)
                                                                                                       MOLT
                                                                                                       PDL T
C INPUTS
                                                                                                       MOLT
                                                                                                       MOLT
       MOFNO
                    NUMBER OF MODES TO BE PRINTED OUT.
                                                                                                       MDL T
         1 *4
                                                                                                       MDL T
                                                                                                       PULT
                                                                                                               35
      CMMUD
                    VECTOR STORING ANGULAR PREQUENCY COORDINATE OF POINTS ON
                                                                                                       MDL T
                    DISPERSION CURVES. MODE " IS STORED FROM ELFMENT KST (M) THROUGH ELEMENT KFIN(M). ( RAD/SEC )
         P * 4(U)
                                                                                                       FDLT
                                                                                                       MOLT
                                                                                                               39
                                                                                                       MDL T
                    VECTOR STORING PHASE VELOCITY COORDINATE OF POINTS ON DISPERSION CURVES. MODE M IS STORED FROM ELEMENT KST(M) THROUGH ELEMENT KFIN(M). ( KM/SEC )
      GUPAA
                                                                                                       MDL T
         R#4(D)
                                                                                                       MDL T
                                                                                                       MDL T
                                                                                                       MDLT
                    SEE OMMOD AND VPMOD ABOVE.
      KST
                                                                                                       MDL T
         1+4(0)
                                                                                                       MOLT
                                                                                                       MDL T
      KFIN
                    SEE OMMOD AND VPMOD ABOVE.
                                                                                                       *DLT
         1*4(D)
                                                                                                      MOLT
                                                                                                       MOL T
    TPUTS
                                                                                                      FOLT
                                                                                                       T JON
      THE OUTPUT IS AN ORDERED AND LABELED PPINT CUT OF THE INPUTS. EXCLUDING KST AND KFIN. ( SEE EXAMPLE RELOW. )
                                                                                                       MOLT
                                                                                                       MOL T
                                                                                                       MDL T
                                                                                                       POLT
                           ---EX AMPLE----
                                                                                                      MOL T
                                                                                                      MOL T
  CALLING PROGRAM
                                                                                                      POLT
                                                                                                      MOLT
        DIMENSION KST(2), KFIN(2), OMMOD(5), VPMOD(5)
                                                                                                      PDL1
                                                                                                              60
        MOFND = 2
KST = 1+3
                                                                                                      MOLT
                                                                                                      MDL T
        KFIN =
                                                                                                      MOLT
                                                                                                              63
        OMMOD = 0.1.0.2.0.1.0.15.7.2
VPMCD = 1.0.2.0.2.0.2.5.3.0
                                                                                                      MDL T
                                                                                                      MOLT.
                                                                                                              65
        CALL MOTEST (MOFNO, OMMOD, VPMOD, KST, KFIN)
                                                                                                                    PROGRAM
                                                                                                      MDL T
                                                                                                      MDL T
                                                                                                                     4 30L ST
  PRINT OUT
                                                                                                      FOLT
                                                                                                              68
                                                                                                      MOL T
                                                                                                                        PAGE
```

-243-

TABULATION OF FIRST

2 40065

POL T

```
POL T
MOLT
                                                                                          MOLT
                                                                                                 74
75
                                          MODE 1
                                                                                          MOLT
                                                                                          MOLT
                                                                                          MDLT
                CMESA (RAD/SEC)
                                              VPHSE (K4/SEC)
                                                                                          MOLT
                                                                                                 77
                                                                                          MIN T
                                                                                                 76
                        0.100000
                                                     1.000000
                                                                                          MOLT
                        2.200000
                                                     2.000000
                                                                                         MDLT
                                                                                                £1
                                                                                         POLT
                                                                                          MDL !
                                                                                         T JCM
                                                                                          MOLT
                                          MODE
                                                                                                 ×4
                                                                                          POLT
                                                                                          WUIT
               CMEGA (RAD/SEC)
                                              VPHSE (KM/SEC)
                                                                                         MDL T
                        0.100000
0.150000
0.200000
                                                     2.000000
                                                                                         MOLT
                                                                                                 ρa
                                                     2.500000
                                                                                                 ar
                                                                                          MDI T
                                                                                          MDLT
                                                                                         MDL T
C END OF EXAMPLE
                                                                                                93
                                                                                          MULT
                                                                                         MDLT
                                                                                         PDL T
                                                                                                96
0000
                        ----PROGRAM FOLLOWS BELOW----
                                                                                         MOLT
                                                                                         MOLT
                                                                                                 98
                                                                                                99
       SUBROUTINE MODIST(MOFNO, OMMOD, VPMOD, KST, KFIN)
                                                                                         MDLT 100
                                                                                         POLT 101
POLT 102
MDLT 103
                                                                                         *DLT 104
MDLT 105
                                                                                         POLT 106
                                                                                         MDLT 107
MDLT 108
                                                                                         MDLT 109
                                                                                         MOLT 110
MOLT 111
                                                                                         MOLT 111
MOLT 112
MOLT 113
MOLT 114
MOLT 115
MOLT 116
MOLT 117
        VPHSE=VPMOD(J)
   31 FORMAT (1H ,12X,F15.6,10X,F14.6)
WRITE (6,31) OMEGA,VPHSE
10C CONTINUE
       RETURN
END
                                                                                         MOLT 118
MOLT 119
```

PROGRAM

```
MPOUT (SURROUTINE)
                                                             7/19/68
                                                                                                               MPOU
                                                                                                               MPOIL
                              ----ARSTRACT----
                                                                                                               MODEL
                                                                                                               MPOU
                                                                                                               ויר אש
  TITLE - MPOUT
             TABLEATION OF NORMAL MODE DISPERSION FUNCTION SIGN AT POINTS
                                                                                                               WD: 11
                                                                                                               MPILL
             IN A RECTANGULAR REGION OF FREQUENCY - PHASE VELUCITY PLANE
                      THE VECTOR V OF PHASE VELOCITIES IS CONSTRUCTED BY 14K1'G VALUES AT INTERVALS OF ((V2-V1)/(NVP-1)) FROM V2 DCWN GV1. SIMILARLY, VECTOR OM OF ANGILAR FREQUENCIES IS CCN-
                                                                                                               MODIL
c
c
                                                                                                               MPIPI
                                                                                                                        11
                                                                                                               ₩P∩U
                      STRUCTED BY TAKING VALUES AT INTERVALS OF (10M2-CM1)/
(NCM-1)) FROM ONL UP TO CM2. NEXT, MATRIX INMCDE IS CON-
STRUCTED WITH NVP ROWS AND NOM COLUMNS. SINCE INMCDE IS
STORED IN VECTOR FORM, CCLUMN AFTER COLUMN, ELEMENT J IN-
ROW I IS REPRESENTED AS INMCDE((J-1)*NVP + I). THE VALUE
OF THIS ELEMENT IS DETERMINED BY CALLING SUPPROVIEW.
                                                                                                               MPAI
                                                                                                               MPRH
                                                                                                               MONU
                                                                                                               #PIN]
                                                                                                               wpny
                      TO EVALUATE THE NORMAL MODE DISPERSION FUNCTION, FPP, FIR FREQUENCY OM(J) AND PHASE VELOCITY V(I). IF FPP DOES NOT EXIST, THE ELEMENT IS SET EQUAL TO 5. OTHERWISE THE ELEMENT
                                                                                                               MOUL
                                                                                                               MPOH
                                                                                                               vpnii
                       MENT WILL BE I TIMES THE SIGN OF FPP.
                                                                                                               MPOU
                                                                                                               MPOU
                   - FORTRAN IV (360, REFERENCE MANUAL C28-6515-4)
- A.D.PIERCE AND J.POSEY, M.I.T., JUNE, 1968
                                                                                                               MPOÜ
C LANGUAGE
   AUTHORS
                                                                                                               MP )U
                                                                                                               MPOU
                                                                                                                        26
                                                                                                               PPOU
                               ----USAGF----
                                                                                                               MEDII
         VARIABLES UM. V. INMIDE MUST BE DIMENSIONED IN CALLING PROGRAM FORTRAN SUBROUTINE NMOFN (DESCRIBED ELSEWHERE IN THIS SERIES) IS
                                                                                                               MPTU
                                                                                                               4P7Ū
         CALLED
                                                                                                               MPOU
                                                                                                                        31
                                                                                                               MPOU
                                                                                                               MPDU
   FORTRAN USAGE
         CALL MPCUT(CM1.0M2.V1.V2.NDM.NVP.INMCDE.CM.V.THETK)
                                                                                                               MPOU
                                                                                                                        34
                                                                                                               MPOU
                                                                                                               MPOU
   INPUTS
                                                                                                               ⊭POU
                                                                                                                        37
                       MINIMUM ANCULAR FREQUENCY TO BE CONSIDERED TRADIANS / SEC
                                                                                                               UC9M
        CM1
                                                                                                               MPOU
                                                                                                                        39
0000000000000000000
                                                                                                               MPOU
                                                                                                                        4 C
                                                                                                               MPOU
        042
                       MAXIMUM ANGULAR FREQUENCY TO BE CONSIDERED TRADIANS / SEC
          R#4
                                                                                                               PPOI
                                                                                                                        42
                                                                                                               MPOU
                                                                                                                        43
                       MINIMUM PHASE VELOCITY TO BE CONSIDERED (KM / SEC)
                                                                                                               MPOU
        ٧l
           R#4
                                                                                                               MPOU
                                                                                                                        45
                                                                                                               MPOU
                                                                                                                        46
                       MAXIMUM PHASE VELOCITY TO BE CONSIDERED (KM / SEC)
                                                                                                               UCAN
                                                                                                                        41
        ٧2
                                                                                                               MPOU
           R*4
                       NUMBER OF FREQUENCIES TO BE CONSIDERED (NO. OF ELEMENTS
                                                                                                               MP7U
        NOM
           1*4
                       IN OM A O NO. OF COLUMNS IN INMODE)
                                                                                                               MPOIL
                                                                                                                        50
                                                                                                               PPOU
                     NUMBER OF PHASE VELUCITIES TO BE CONSIDERED (N). OF ELE-
MENTS IN V AND NO. OF ROWS IN INMODE)
                                                                                                               MPJU
        NVP
           144
                                                                                                               MPOU
                                                                                                                        53
                                                                                                               MPOU
                                                                                                                        54
        THETK
                       DIRECTION OF PHASE VELOCITY MEASURED COUNTER GLLCKWISE
                                                                                                               MPOU
                                                                                                               MPOU
           R#4
                       FROM X-AXIS (RADIANS)
                                                                                                                        56
                                                                                                               MPOU
    CUTPUTS
                                                                                                               MPOU
                                                                                                                        58
                                                                                                               MPOIJ
         INMODE
                       MATRIX OF NORMAL MODE DISPERSION FUNCTION SIGNS (SEE
                                                                                                               MPCH
                                                                                                                        60
                       ABSTRACT ABOVE FOR EXPLANATION OF ELEMENT VALUES)
           1*4(0)
                                                                                                               MECH
                                                                                                                        61
                                                                                                               MPOU
                                                                                                                        62
                       VECTOR OF NOM VALUES OF ANGULAR FREQUENCY AT EQUAL INTER-VALS FROM OM1 TO OM2 INCLUSIVE (RADIANS / SEC)
                                                                                                               MPOH
                                                                                                               MP TU
           R#4(D)
                                                                                                               Mbisi
                       VECTOR OF NVP VALUES OF PHASE VELOCITY AT EMUAL INTERVALS FROM V2. TO V1. INCLUSIVE (KM / SEC).
                                                                                                               ► P TU
                                                                                                                        66
                                                                                                                              PPCGRAM
                                                                                                                        67
                                                                                                                                  4P TUT
                                                                                                               MPOÜ
           P#4(0)
                                                                                                               MPOU
                                                                                                               MPITI
                                                                                                                                   PAGE
                               ---EXAMPLE ----
                                                                                                               MPO I
```

```
MP TU
C CALLING PREGRAY
                                                                                       Meudi
     DIMENSION OMESH, VEST, INMODEST
                                                                                       MPDIE
     041 = 1.0
042 = 3.0
                                                                                       MPOIL
                                                                                              74
                                                                                       MPJIJ
     V1 = 1.0
V2 = 3.0
                                                                                       MPGU
                                                                                       ND 311
                                                                                              7 7
     NCM = 3
NVP = 3
                                                                                       MPOIS
                                                                                              74
                                                                                       чріді
                                                                                       POU
     THETK = 0.0
                                                                                             82
                                                                                        BOU
     CALL MPOUT ICMI "OM2 . VI . V2 . NCM . NVP . INMCDE . OM . V . THETK )
                                                                                              81
                                                                                       MPCHI
                                                                                              82
                                                                                       MPI U
C UPON RETURN FROM MPOUT, OM AND V WILL HAVE THE FOLICHING VALUES
                                                                                       MEGIL
                                                                                              94
MAUI
                                                                                              45
                                                                                       up. nj
                                                                                       زيدوب
                                                                                             97
C BY THE N'IRMAL MODE DISPERSION FUNCTION (SEE ABSTRACT ABOVE)
                                                                                       WP 111
                                                                                              w 4
                                                                                       WF-31
                                                                                              ٩u
                                                                                       PP 1U
                                                                                              90
                       ----PHUGRAM FOLLOWS BELCH----
                                                                                       40' 11
                                                                                             41
                                                                                       YP7I)
                                                                                              42
C.
Č.
                                                                                       wphij
       SUBROUTINE MPOUT ( 1M1, JM2, VI, V2, NOM, NVP, INNODE, JP, V, THETK )
                                                                                       MOOIL
                                                                                       HOOL
c
                                                                                             75
  VARIABLE DIPENSIONING
                                                                                       POU
                                                                                             96
C
       DIMENSION OM(1), V(1), INMODE(1)
                                                                                       PPOU
                                                                                             97
       COMMON IMAX, CICIODI, VXICIODI, VY [C100], PIC 100]
                                                                                       MPITIE
                                                                                             0.8
                                                                                      MPOU
                                                                                             99
C INTERVAL RETWEEN SUCCESSIVE FLEMENTS OF OM IS DETERMINED
                                                                                       MPOU 100
       DELCH= (C42-3M1)/(NOM-1)
                                                                                       PPOU LOI
                                                                                       MPRU 102
C INTERVAL BETWEEN SUCCESSIVE ELEMENTS OF V IS DETERMINED
                                                                                       MPOU 103
                                                                                       MPOU 124
c
                                                                                       MPOU 105
C VECTOR V IS CONSTRUCTED WITH V(1) DROPPING FROM V2TO VI AS I GUES FROM MPOU 106
C 1 TO NYP
                                                                                       MPCU 107
       V111=V2
                                                                                       PP0U 108
   DO 10 I=2+NVP
10 V(1)=V(I-1)-DELV
                                                                                       MPOU
                                                                                            109
                                                                                       PPOU 110
                                                                                       4POU 111
C CHIJ) GOES FROM ONL TO OME AS J GOES FROM L TO NOM
                                                                                      MP0U 112
       DO 90 J=1+NOM
OM(J) # OM1 +(J=1)*DELOM
                                                                                       UCSM
                                                                                       MPAU
                                                                                            114
                                                                                       PPOU 115
C FOR A FIXED VALUE OF J. ALL VALUES OF I FROM 1 THROUGH NVP APE CONSIDERED. THUS EVALUTING COLUMN J OF INMODE DO 90 I=1.NVP
                                                                                       MPOU
                                                                                       MPOH
                                                                                            117
                                                                                       >POU 118
                                                                                       MPOU
C IJ IS NO. OF ELEMENT IN V TOR REPRESENTATION OF INPCDE WHICH CORRES-
C PONDS TO ELEMENT J OF ROW I IN MATRIX FORM OF INMODE
IJ=(J-1)=N$P + I
                                                                                       MPQU 120
                                                                                      PPOU
                                                                                            121
       VPHSE=V(1)
                                                                                       MPOU 123
                                                                                       MPOU
                                                                                            124
  NHOFN IS CALLED TO EVALUATE THE NORMAL MODE DISPERSION FUNCTION FOR
  FREQUENCY OP(1) AND PHASE VELOCITY V(1)
CALL NMOFH(OM(1), VPHSE, THETK, L, FPP, K)
                                                                                      MPOU 176
MPOU 177
  WHEN NORMAL MEDE DISPERSION FUNCTION DOES NOT EXIST (L.EQ.-1). INMODE
                                                                                       MPOU 129
                                                                                       PPOU 130
C(13) = 5
       1FIL .EC. -1) GO TO 50
                                                                                       PPOU 131
                                                                                      MPOU 132
C WEEN THE FUNCTION DOES EXIST AND IS FPP, INNODE(IJ) = 1+FPP/ABS(FPP)
                                                                                       MPOU 133
                                                                                       PPOU 134
       INMODE(1J) = 1
       IF (FPP.LE.O.O) INMODELIJI = -1
GO TO 80
                                                                                       MPOU 135
                                                                                       MPNU 136
                                                                                                  PPOGRAM
                                                                                      PPOU 137
    50 INMODE (13) = 5
                                                                                                     POUT
    BC CONTINUE
                                                                                       PPOU 138
                                                                                       MPOU 139
                                                                                                      PAGE
    OR COMPINITE
                                                                                       MPOU
       RE TURN
```

3

و سراد ه

END PPCU 141

PROGRAM T MPOUT

```
NAMPUE (SUBROUTINE)
                                                                                6/27/68
                                                                                                                                                 NAMP
                                                                                                                                                 KAMP
                                                                                                                                                 AAMP
                                     ----ABSTRACT----
                                                                                                                                                 NAMP
                                                                                                                                                 ...
   TITLE - HAMPDE
                 - NAMPDE
PROGRAM TO DETERMINE AN AMPÉITUDE FACTOR AMPETO OF A GUIDED
MCDE EXCITED BY A POINT ENERGY SOURCE IN THE ATMOSPHERE. THE
SOURCE IS AT ALTITUDE 2SCRCE KM AND THE OBSERVER IS AT ALTITUDE
20BS IN KM. THE PARTICULAR AMPLTO COMPUTED CORRESPONDS TO AN
ANGULAR FREQUENCY DMEGA (RAD/SEC), A PHASE VELOCITY VPHSE
(KM/SEC), AND A PHASE VELOCITY DIRECTION THETK (RADIANS) REC-
KONED COUNTER-CLOCKWISE FROM THE X AXIS. PARAMETERS DEFINING
THE AMBIENT ATMOSPHERE ARE PRESUMED TO BE STORED IN COMMON.
THE MORMAL MODE DISPERSION FUNCTION AMDE IS PRESUMED TO VANISH
FOR ARGUMENTS OMEGA.VPHSE, THETK.
                                                                                                                                                 A A MP
                                                                                                                                                 MAMP
                                                                                                                                                  4 A MP
                                                                                                                                                 MAMP
                                                                                                                                                              o
                                                                                                                                                 AND
                                                                                                                                                             10
                                                                                                                                                 NAMP
                                                                                                                                                             11
                                                                                                                                                 NAMP
                                                                                                                                                 AAAD
                                                                                                                                                 A A MP
                                                                                                                                                 KAMP
                 FOR ARGUMENTS OMEGA. VPHSE. THETK.
                                                                                                                                                 AAMO
                                                                                                                                                 MAYO
                                                                                                                                                             17
                 THE ACTUAL DEFINITION OF AMPLTO IS AS FOLLOWS. LET SI(2) \Delta N_{\rm D} S2(7) BE THE SOLUTIONS OF THE RESIDUAL EQUATIONS
                                                                                                                                                 F A40
c
                                                                                                                                                 ....
                                                                                                                                                             10
                                                                                                                                                 NAMP
                                                                                                                                                            20
                          D(S1)/U2 = (A11)+S1 + (A12)+S7
D(S7)/D2 = (A21)+S1 + (A22)+S2
                                                                                                                                                             21
                                                                                                                                 (1-4)
                                                                                                                                                 MAMP
                                                                                                                                                 MAMP
                                                                                                                                                            23
                  WHERE THE MATRIX A IS AS COMPUTED BY AAAA AND AS DEFINED BY
                                                                                                                                                 NAMP
                  A.O.PIERGE, J. COMP. PHYS., VOL. 1, NO. 3, FEB., 1967, PP. 343-366, EQS. 11. THE ELEMENTS OF A SHOULD BE CONSIDERED AS FUNCTIONS OF ALITHDE. WE DEFINE THE REDUCED PRESSURE ZEN(Z) AS
                                                                                                                                                 MAMP
                                                                                                                                                 NAMP
                                                                                                                                                            26
                                                                                                                                                            27
C
                                                                                                                                                 NAMP
                          ZFN(Z)= (G/C)+S1 - C+S2
                                                                                                                                                 NAMP
                                                                                                                                                            29
                                                                                                                                                             30
                                                                                                                                                 NAMP
C
                  WHERE G IS ACCELERATION OF GRAVITY AND C IS SOUND SPEED. THEN
                                                                                                                                                           32
33
                                                                                                                                                 NAMP
                                                     S2(7 SCRCE) *ZFN(ZORS)
                                                                                                                                                 NAMP
                   AMPLTD # (1/2)#
                                                                                                                                                 NAMP
                                                                                                                                 (3)
                                                                                                                                                             35
                                                   BOM(ZSCRCE) + INTEGRAL
                                                                                                                                                            36
                                                                                                                                                 NAMP
                  WHERE
                                                                                                                                                 MAMP
                                                                                                                                                            38
                          BUM(Z)=OMEGA -KX*VX(Z) -KY*VY(Z)
                                                                                                                                                 NAMP
                                                                                                                                                            40
                                                                                                                                                 NAMP
                                                                                                                                                            41
                  IS THE DOPPLER SHIFTED ANGULAR FREQUENCY. THE INTEGRAL IS 1/2 OF THE I-SURI DEFINED BY A.D.PIERCE, J. ACOUST. SCC. AMER., VOL. 37, NO. 2, FEB.,1965, PP. 218-227, EQ. (51). SPECIFICALLY
                                                                                                                                                 AAMD
                                                                                                                                                 NAMP
                  INTEGRAL . (INTEGRAL OVER 2 FROM 0 TO INFINITY) OF
                                                                                                                                                 NAMP
                                                                                                                                                 NAMP
                                                                                                                                                            47
                                          [BOH={{K**V*+KY*VY}/K}*YFN{Z}**2
                                                                                                                                                 MAMP
                                           + (K+C4F GA/BCM++3) + ZFN (Z) ++?
                                                                                                                                 (5)
                                                                                                                                                 NAMP
                                                                                                                                                 ALMP
                                                                                                                                                            50
                  WHERE K IS THE MAGNITUDE OF THE WAVE-NUMBER VECTOR (KX+KY) AND
                                                                                                                                                 LAMP
                                                                                                                                                 NAMP
                                                                                                                                                            52
                                                                                                                                                 N AMP
                          YFN(Z) = (1/C)+S1(Z)
                                                                                                                                                 NAMP
    PROGRAM NOTES
                                                                                                                                                 NAMP
                                                                                                                                                            55
                                                                                                                                                 MAMP
                             THE INTEGRAL IS COMPUTED BY SUBROUTINE TOTINT IN TWO PART AS X3+X7. THE FIRST IS OBTAINED BY CALLING TOTINT WITH IT=3, WHILE THE SECOND IS OBTAINED BY CALLING TOTINT WITH IT=7. THE IT PARAMETER GOVERNS THE CHCICE OF COEFFICIENT AL, A2, A3 RETURNED TO TOTINT BY SUBROUTINE USEAS. FOR
                                                                                                                                                 NAMP
                                                                                                                                                            57
                                                                                                                                                 NAMP
                                                                                                                                                 NAMP
                                                                                                                                                 NAMP
                                                                                                                                                            60
                                                                                                                                                 NAMP
                                                                                                                                                            61
                              FURTHER INFORMATION. SEE THE COCUMENTATION ON TOTINT AND
                                                                                                                                                 RAMP
                              USEAS.
                                                                                                                                                 NAMP
                                                                                                                                                 NAMP
                                                                                                                                                            64
                             THE NORMALIZATION OF S1 AND S2 CANNOT AFFECT AMPLTO.
HOWEVER, TOTINT ADDOPTS NORMALIZATION WHERE
S1 =-SORT(GG) *A12
                                                                                                                                                 NAMP
                                                                                                                                                 NAMP
                                                                                                                                                            66
67
                                                                                                                                                                    PROGRAM
                                                                                                                                                 NAMP
                                                                                                                                                                      NAMPDE
                              S2 = SQRT(GG)*(GG+A11)
AT THE MOTTOM OF THE UPPER HALF SPACE. THE NUMERATOR OF EQ. (3) IS ACCORDINGLY COMPUTED WITH SAME NORMALIZATION.
                                                                                                                                                NAMP
NAMP
                                                                                                                                                           68
                                                                                                                                                                          PAGE
```

```
HERE GG=SURT(411##2+A12#A21).
                                                                                                              AAMP
                                                                                                             NAMP
                                                                                                              MAMP
                      THE ONLY BOUNDARY CONDITION EXPLICITLY USED IS THE UPPER
                     BOUNDARY CONDITION WHEREBY BOTH S1(7) AND S2(7) DECREASE EXP MENTIALLY WITH INCREASING HEIGHT IN THE UPPER HALFSPACE. IF THIS CANNOT RE SATISFIED, THE PROGRAM RETURNS AMPLTD=0. THIS WOULD IMPLY THAT THE POINT CONSIDERED IS PRACTICALLY IDENTICAL TO ONE WHERE CMEGA IS THE CUTOFF FREQUENCY FOR THE GUIDEU MOUE UNDER
                                                                                                              NAMP
                                                                                                                       75
                                                                                                              NAMP
                                                                                                              NAMP
                                                                                                                       76
                                                                                                              NAMP
                                                                                                             4 V 4 b
                                                                                                                       79
                      CONSIDERATION.
                                                                                                             N'AMP
                                                                                                             NAMP
                      WHEN NPRNT IS POSITIVE, SEVERAL PARAMETERS DESCRIPING THE PROFILES OF SI AND S2 ARE PRINTED UNDER THE HEADING PROMIDED BY SUBROUTINE PARADE. SEE PAMPOE FOR THE DEFINI-
                                                                                                             . 440
                                                                                                             FAMP
                                                                                                             f AMP
                      TIONS OF THESE PARAMETERS.
                                                                                                             4444
                                                                                                                      5.5
                                                                                                              4445
C LANGUAGE
                   - FORTRAN IV (360, REFERENCE MANUAL C28-6515-4)
                                                                                                             11 A 4P
                                                                                                                      × 7
                                                                                                             RAMP
C AUTHOR
                   - A.C.PIERCE, M.I.T., JUNF, 1968
                                                                                                             6 A-40
                                                                                                             444
                            ---- CALLING SEQUENCE----
                                                                                                             440
                                                                                                                      01
                                                                                                             1.443
  SEE SUBROUTINE PAMPDE
                                                                                                             AAMP
        DIMENSION CI(100), VXI(100), VYI(100), HI(100)
                                                                                                             AAMO
                                                                                                                      94
         COMMON IMAX,CI,VXI,VYI,HI
                                                        (THESE MUST BE IN COMMON)
                                                                                                             P:AMP
                                                                                                                      45
         CALL NAMPDEIZSCRCE, ZORS, OMEGA, VPHSE, THE TK, AMPLTO, NPRNTI
                                                                                                             NAMP
                                                                                                                      46
                                                                                                             MAMP
                                                                                                                      97
                            ---- EXTERNAL SUBROUTINES REQUIRED----
                                                                                                             NAMP
         TOTINT, PMMM, AAAA, USE AS, UPINT, EL INT, BPHH, CAI, SAI
                                                                                                             NAMP 1CG
                                                                                                             NAMP 101
         ITHE FIRST THREE ARE EXPLICITLY CALLED. THE REMAINING SUBPOUTINES
                                                                                                                    102
          ARE IMPICITLY CALLED WHEN TOTINT IS CALLED.)
                                                                                                             NAMP
                                                                                                                    103
                                                                                                             NAMP 104
                      ----ARGUMENT LIST----
                                                                                                             NAMP.
                                                                                                                    106
         2SCRCE
                         R*4
                                            INP
                                                                                                             NAMP 107
         ZOBS
                                    ND
                                             INP
                                                                                                                    108
         CMEGA
                         R=4
                                   NO
                                             INP
                                                                                                             NAMP 109
                         R = 4
         VPHSE
                                            INP
                                                                                                             NAMP 110
                                    NO
                         R+4
                                    ND
                                             INP
         AMPLTD
                         R + 4
                                    ND
                                            OUT
                                                                                                             NAMP
                                                                                                             NAMP
         NPRNT
                         144
                                    NI)
                                             INP
                                                                                                                    113
                                                                                                             NAMP
  CCMMON STORAGE USED
                                                                                                             NAMP 115
                                                                                                             NAMP
         COMMON IMAX.CI.VX!.VYI.HI
                                                                                                                    116
                                                                                                             NAMP
         IMAX
                                    ND
                                             INP
                                                                                                             NAMP
                                                                                                                    118
                         R =4
                                    120
                                                                                                             NAMP 119
                                            INP
         CI
         1XV
                         R∓4
                                    100
                                              .0
c
         J YV
                         P#4
                                    100
                                            INP
                                                                                                             NAMP 121
                                                                                                             NAMP
                         R 4
                                            INP
                                    100
                                                                                                             MAMP
                            ---- INPUTS----
                                                                                                             NAMP
                                                                                                             KAMP
                           *HEIGHT OF SOURCE IN KM *HEIGHT OF OBSERVER
         ZSCRLF
                                                                                                             PAMP
C
         20 B S
                                                                                                             NA4P
                                                                                                                    127
                           =ANGULAR FREQUENCY IN RADIANS/SEC
=PHASE VELOCITY IN KM/SEC
=PHASE VELOCITY DIRECTION (PADIANS) RECKONED
         OMEGA
         VPHSE
                                                                                                             NAMP 129
         THETK
                                                                                                             NAMP
C
                                                                                                                    130
                           *PRINT OPTION INDICATOR (SEE NAME IN MAIN PROGRAM).
COUNTER-CLOCKWISE FROM X AXIS.
*NUMBER OF ATMOSPHERIC LAYERS WITH FINITE THICKNESS
                                                                                                             NAMP 132
                                                                                                             MAMP
         IMAX
                                                                                                                    133
                           #SOUND SPEED (KM/SEC) IN 1-TH LAYER
#X COMPONENT OF WIND VELOCITY (KM/SEC) IN 1-TH LAYER
#Y COMPONENT OF WIND VELOCITY (KM/SEC) IN 1-TH LAYER
                                                                                                             RAMP
         (1)15
         (1)1XV
(1)1YV
                                                                                                             NAMP 135
                                                                                                             NAMP
                                                                                                                    136
         HILL
                           THICKNESS IN KM OF I-TH LAYER
                                                                                                             NAMP
                                                                                                                              VAMPIDE
                                                                                                             NAMP 138
                             ----(1019015----
                                                                                                                    139
                                                                                                                                PAGE
```

-- 303 --

45

NA 4P 140

```
MAN2 141
        AMPLID
                        =AMPLITUDE FACTOR FOR GUIDED MAVE EXCITED BY POINT
                         ENERGY SOURCE. UNITS ARE KMF + (-1).
                                                                                                 NAMO 142
                                                                                                 1.4 VP 143
                         ----EX 4MPLE----
                                                                                                  NAMP 144
                                                                                                  NAMP 145
       SUPPOSE THE ATMOSPHERE IS ISOTHERMAL AND THERE ARE NO WINDS. THEN THERE IS DNLY ONE MODE, FOR MHICH VPHSE=C. FURTHERMORE, YEN(2) AMD S1(2) ARE BOTH ZERO. THE ZEN(7) DECREASES EXPONENTIALLY WITH MEIGHT AS EXP(~(0.3*G/C**21). THE RESULTING AMPLTO
                                                                                                 NAMP 146
                                                                                                 KAMP 147
                                                                                                  PA40 148
                                                                                                 1 AMP 149
        SHOULD BE
                                                                                                 MAMO 150
                                                                                                 MAMP 151
          AMPLTD=-(.3*G/C**2)*EXP(-.3*(G/C**2)*(7ORS+ZSCRCE))
       REGARDLESS OF VALUES OF OMEGA AND THETK. IF C=1/3 KM/SEC,
G=-01 KM/SEC+M2, ZOBS=0, ZSCRCE=C, THEN AMPLTO= .027 KM=+(-1).
                                                                                                 NAMP 152
                                                                                                 NAMO 153
                                                                                                 644P 154
                                                                                                 MAMP 1 FS
                         ----PROGRAM FOLLOWS BELCH----
                                                                                                 NAMP 156
                                                                                                 147 Och 4
C
                                                                                                 AAMD 164
        SUBROUTINE NAMPUE (ZSCRCE, ZOBS, GMEGA, VPHSF, THETK, AMPLITO, NPRFIT)
                                                                                                 LAND IFG
c
                                                                                                 NAME 14.5
        DIMENSION CICIODI, VXICIOCI, VYICIOCI, HICIOCI
                                                                                                  111 GPA4
DIMENSION 4(2,2),EM(2,2)

DIMENSION 2(1)/(2),S1(2),S2(2),VXIJZ(2),VYIJZ(2),CIJZ(2)

C DIMENSION STATEMENTS ADDED IN THE DERUG PROCESS

DIMENSION LAYJZ(2),UFLT(2),RPP(2,2),EMP(100,2,2),UMMY(2,2)

DIMENSION PHIL(100),PHIZ(100)
                                                                                                 4A" 2 162
                                                                                                 NA 4P 143
                                                                                                 NA40 : 64
                                                                                                 KAMP 165
                                                                                                 NAMP 166
        INTINATION TANK T NORMOS
                                                                                                 FAMP 167
C COMPUTE WAYS NUMBER VECTOR CHAPMENTS
                                                                                                 FAND 15P
                                                                                                 NAMP 169
        AKX=(NYE'A/VPHSE)*COS(THETK)
                                                                                                 NAMP 170
        AKY=(CMEGA/VPHSE) +SINE THE TK)
                                                                                                 NAMP 171
C THE SOURCE AND CREENER LOCATIONS ARE NUMBERED ACCORDING TO FEIGHT
                                                                                                 NAMP 172
                                                                                                 NAMP 173
        IF(ZSCRCE .GT. ZOHS) GO TO 10
ZIJZ(1)=ZSCRCE
ZIJZ(2)=ZOHS
                                                                                                 NAMP 174
                                                                                                 NAMP 175
                                                                                                 NAMP 176
        NSCRCF=1
                                                                                                 NAMP 177
        OC TO SO
                                                                                                 NAMP 178
                                                                                                 NAMP 179
    1C 21 JZ(1) = ZC9S
                                                                                                 N44P 180
                                                                                                 NAMP 181
NAMP 182
        21 J Z ( 2) =7 SCRCe
        NSLRCE=2
                                                                                                 NAMP 183
                                                                                                 NAMP 184
C WE DENOTE SI AND S2 AT BUTTOM OF UPPER HALFSPACE BY FI AND F2. THEIR
                                                                                                 NAMP 185
C COMPUTATION IS AS FOLLOWS.
20 17MAX=2
                                                                                                 NAMP 186
                                                                                                 NAMP 187
        J=IMAX+1
                                                                                                 BRI SMAN
        C=(1(J)
                                                                                                 NAMP 189
        VX=VXI(J)
                                                                                                 NAMP 190
                                                                                                 MAMP 101
        CALL ASAMINHEGA.AKX.AKY.C.VX.VY.A)
                                                                                                 NAMP 197
        X= A(1,1) == 2+A(1,2) +A(2,1)
                                                                                                 NAMP 193
        IFEX .LE. 0.0) GO TO 200
                                                                                                 NAMP 194
        G=SQRT(X)
                                                                                                 NAMP
        GRT= SORT(G)
                                                                                                 NASP 196
        F1=-GRT+4(1,2)
                                                                                                 NAMP 197
        F2=GPT=(A(1,1)+G)
                                                                                                 NAMP
                                                                                                       198
                                                                                                 NAMP 109
C WE COMPUTE IM REPRESENTING THE BOTTOM OF THE UPPER HALES ACE
                                                                                                 NAMP 200
                                                                                                 NAMP 201
        IF(IPAX .FQ. 0) GO YO 31
OO 30 IC=1,1MAX
                                                                                                 NAMP 202
                                                                                                 NAMP 203
    30 ZP=ZM+H1(1C)
                                                                                                 NAMP 204
                                                                                                 NAMP 205
C WE STORE FIP. F2P. ZMP
                                                                                                 NAMP 206
                                                                                                              PRICERAN
    31 F1P=F1
                                                                                                 NAMP 207
                                                                                                                NAMPDE
        F2P=F2
                                                                                                 NAMP 208
        ZMD=ZM
                                                                                                 NAMP 2C4
                                                                                                                  PAGE
c
                                                                                                 NAMP 210
                                                                                                                    46
```

```
C COMPUTATION OF LAYJZ(JZ) AND DELT(JZ)
C LAYJZ(JZ) IS THE INDEX OF THE LAYER IN WHICH ZIJZ(JZ) LIES.
C WHILE DELT(JZ) IS THE DISTANCE OF ZIJZ(JZ) ABOVE THE BOTTOM EDGE OF
                                                                                                  NAMP 211
                                                                                                  NAMP 212
                                                                                                        213
                                                                                                  NAMP
C THE LAYER
                                                                                                  NAMP 214
        00 35 JZ=1+2
LAYJZ(JZ)=1MAX+1
                                                                                                  NAMP 215
                                                                                                  NAMP 216
    32 DELT(JZ)=ZIJZ(JZ)-ZM
                                                                                                  MAMP 217
        IF(DELT(JZ)) .GT. 0.0) GO TC 35
IF(LAYJZ(JZ) .EQ. 1) GU TO 35
LAYJZ(JZ)=LAYJZ(JZ)-1
                                                                                                  NAMP 218
                                                                                                  KAMP 219
                                                                                                  NAMP 220
        ZM=ZM-HI(LAYJZ(JZ))
                                                                                                  NAMP 271
C AT THIS POINT ZM DENUTES THE SCTTOM OF THE LAYJZ(JZ) LAYER GC TO 32
                                                                                                  NAMP 222
                                                                                                  NAMP 223
                                                                                                  NAMP 224
                                                                                                  NAMP 225
C COMPUTATION OF EM MATRICES FOR ALL IMAX LAYERS OF FINITE THICKNESS C EM(IP,JP) FOR I-TH LAYER IS STORED AS EMP(I,IP,JP) DO 36 I=1,IMAX C=CI(I)
                                                                                                  NAMP 224
                                                                                                  NAMP 227
                                                                                                  NAMP 228
                                                                                                  884P 229
                                                                                                  NAMP 230
        VX=VX1(1)
        VY=VY[{[}
                                                                                                  KAMP 231
        H=H1(1)
                                                                                                  KAMP 232
                                                                                                  NAMP 232
        CALL MMM4{GMEGA, AKX, AKY, C, VX, VY, H, EM)
        00 36 IP=1.2
0C 36 JP=1.2
                                                                                                  MAMP 234
                                                                                                  NAMP 235
    36 EMP([, [P, JP)=EM([P, JP)
                                                                                                  NAMP 236
                                                                                                  NAMP 237
C COMPUTATION OF RPP MATRIX. THIS ACCOMPLISHES THE SAME AS CALLING
                                                                                                  NAMP 238
C SUBROUTINE RRRR
                                                                                                  NAMP 239
        RPP(1,1)=1.0
                                                                                                  NAMP 240
        RPP(1,21=0,0
                                                                                                  NAMP 241
        RPP(2,1)=0.0
                                                                                                  NAMP 242
        RPP(2,2)=1.0
DO 36 I=1,1MAX
                                                                                                  NAMP 243
                                                                                                  NAMP 244
         JASA= I MAX+1-!
                                                                                                  NAMP 245
        DO 37 1P=1,2
DO 37 JP=1,2
                                                                                                 NAMP 246
NAMP 247
    37 DUMMY(IP,JP)=EMP(JASA, IP, 1) *RPP(1, JP) +EMP(JASA, IP, 2) * RPP(2, JP)
        DC 38 IP=1,2
DC 38 JP=1,2
                                                                                                  NAMP 249
                                                                                                  NAMP 250
    38 RPP(IP, JP)=DUMMY(IP, JP)
                                                                                                  NAMP 251
C.
                                                                                                  NAMP 752
        QUOT = ABS(RPP(1,1))/(ABS(RPP(1,1))+ABS(RPP(1,2))+ABS(RPP(2,1))
                                                                                                  NAMP 253
        *ABS(RPP[2,2]))

IF ( QUOT ...T. 0.1 ) GO TO 120
F2HCT=F2P/RPP(1,1)
                                                                                                  NAMP 254
       1
                                                                                                  NAMP 255
                                                                                                  NAMP 256
        GD Tr 150
                                                                                                  NAMP 257
   120 QUOT = ABS(RPP(1,2))/(ABS(RPP(1,1))+ABS(RPP(1,2))+ABS(RPP(2,1))
                                                                                                  NAMP 258
        +ABS(RPP(2,2)))
IF ( QUOT .LT. 0.1 ) GO ' 130
F2BOT="F1P/RPP(1,2)
                                                                                                  NAMP 259
                                                                                                  NAMP 260
                                                                                                  NAMP 261
   GO TO 150
130 F280T=RPP(2+1)*F1P+RPP(2+2)*F2P
                                                                                                  RAMP 262
                                                                                                  NAMP 263
   150 F280T=F280T
                                                                                                  NAMP 264
        PHI1(11)=0.0
PHI2(1)=F280T
                                                                                                  NAMP 265
                                                                                                  NAMP 266
        KTOUP=1
                                                                                                  NAMP 267
        K=IMAX+1
                                                                                                  NAMP 268
        PHIL(KI=FIP
                                                                                                  14MP 269
        PHIZIK1 =FZP
                                                                                                  NAMP 270
   331 T1=PHI1(K)
T2=PHI2(K)
                                                                                                  NAMP 271
                                                                                                  NAMP 272
                                                                                                  NAMP 273
         IFIK
               .EQ. 11 69 19 400
                                                                                                  NAMP 274
        C=CI(K)
                                                                                                  NAMP 275
         VX=VX!(K)
                                                                                                  NAMP 276
                                                                                                               PROGRAM
        VY=VY[[K]
CALL A**AA[OMEGA;AKX;AXY;C;VX;VY;A]
                                                                                                  NAMP 277
                                                                                                                NAMPDE
                                                                                                  NAMP 278
         (=A(1,1) ** 2+A(1,2) *A(2,1)
                                                                                                  MAMP 279
                                                                                                                   PAGE
        IF(x .GT. 0.0) GO IN 340
                                                                                                  NA45 580
```

```
333 PH[](K) = EMP(K,1,1) = T]+EMP(K,1,2) = T2
PH[2(K) = EMP(K,2,1) = T]+EMP(K,2,2) = T2
                                                                                                                     1.44P 281
                                                                                                                     NAMP 292
         GO TO 331
                                                                                                                     MAMP 283
   34C D1=A(1+1)=T1+4(1+2)=T2
                                                                                                                     KAMP 224
        D2=A(2-1)=T1+A(1-2)=T2
D2=A(2-1)=T1+A(2-2)=T2
IF ( D1 .LT, 0.0 .ANO. T1 .LT. 0.0) GD TO 341
IF ( D1 .GT. 0.0 .AND. T1 .GT. 0.0 ) GD TO 341
IF ( D2 .LT. 0.0 .AND. T2 .LT. 0.0 ) GD TO 341
IF ( D2 .GT. 0.0 .AND. T2 .LT. 0.0 ) GD TO 341
                                                                                                                     NAMP 245
NAMP 246
                                                                                                                     KAMP 287
                                                                                                                     KAMP ZKR
                                                                                                                     NAMP 289
         GO TO 333
                                                                                                                     VVAL SOU
   341 CONTINUE
                                                                                                                     FA4P 201
C AT THIS POINT THE CURRENT VALUE OF K IS NOT ZERO OR CNE
                                                                                                                     AA40 202
                                                                                                                     MAND 203
         DC 360 K=2+KT 3UP
                                                                                                                     NAMP 294
         JET=K-1
T1=PH11(JET)
                                                                                                                     RAMP 245
                                                                                                                     MAMP 246
          T2 = PH12 (JET)
                                                                                                                      AA4P 297
   PHII(K)=EMP(JET,2,2)*T1-EMP(JET,1,2)*T2
360 PHI2(K)=EMP(JET,2,1)*T1+EMP(JET,1,1)*T2
400 IF (NPRNT.LT.0) GO TO 415
                                                                                                                     AA4P 248
                                                                                                                     NAVII 244
                                                                                                                      NAME 300
         N2C2 = 0
                                                                                                                     INF SPAN
                                                                                                                     NAMP 302
          IAPIMX = 1
                                                                                                                     NAMP
                                                                                                                             303
          IAP2MX = 1
                                                                                                                     NAMP 304
         APIMX = ARS(PHI)(1))
APZMX = ABS(PHI2(1))
                                                                                                                     RAMP 305
                                                                                                                     NAMP 306
          DO 4C7 LNM1=1+TMAX
                                                                                                                      NAMP 307
         LN = LNM1 + 1
AP1P = ARS(PHII(LN))
                                                                                                                     NAMP 308
                                                                                                                     NAMP 309
          IF (APIP.LE.APIMX) GO TO 403
                                                                                                                     NAMP 310
   IAPIMX = LN
APIMX = APIP
4C3 AP2P = ABS(PHI2(LN))
                                                                                                                     NAMP 311
                                                                                                                     NAMP 312
                                                                                                                     NAMP 313
              (AP2P.LE.AP2MX) GO TO 405
                                                                                                                      NAMP 314
         AP2MX = AP2P
IAP2MX = LN
                                                                                                                     NAMP 315
                                                                                                                     NAMP 316
   405 IF ((PHI)(LNM1)*PHI)(LN)).LT.0.0) NZC1 = NZC1 + 1
IF ((PHI2(LNM1)*PHI2(LN)).LT.0.0) NZC2 = NZC2 + 1
                                                                                                                     NAMP 317
                                                                                                                      NAMP 318
   407 CONTINUE
                                                                                                                     NAMP 319
          R1 = PHIL(IAPLMX)/AP2MX
R2 = PHI2(IAP2MX)/AP2MX
                                                                                                                      NAMP 320
                                                                                                                      NAMP 321
   R3 = PHIZ(1)/APZMX
WPITE (6,409) CMEGA, VPMSE, IAPIMX, R1, NZC1, IAPZMX, R2, NZC2, R3
409 FCRMAT (1H , 2F12.5, 9X, 13, F12.5, 9X, 13, F12.5, 9X, 13, F12.5)
                                                                                                                      NAMP 322
                                                                                                                      NAMP 323
                                                                                                                      NAMP 324
   415 DO 450 JE=1.2
                                                                                                                      NAMP 325
          TDA=LAYJ/(JZ)
                                                                                                                      NAMP 326
          C=CITICA)
                                                                                                                      NAMP 327
          VX=VXI+ICA)
                                                                                                                      NAMP 328
                                                                                                                      NAMP 329
          VY=VYICIDA)
          CIJZIJZ)=CICIDA)
                                                                                                                      NAMP 330
                                                                                                                      NAMP 331
          VXIJZ(JZ)=VXI(IDA)
          VY[JZ(JZ)*VY[[]DA]

[F[]DA .EQ. [MAX+1] GO TO 420

[F[]DA .LE. KTOUP] GO TO 430
                                                                                                                      NAMP 332
                                                                                                                      NAMP
                                                                                                                             333
                                                                                                                      NAMP 334
          JET #IDA+1
                                                                                                                      NAMP 335
          H=HI(IDA)-DELT(JZ)
                                                                                                                      NAMP
                                                                                                                             336
          CALL MMMG(0"CGA,AKX,AKY,C,VX,VY,H,EM)
$1(JZ)=EM(1,1)=PHI1(JET)+EM(1,2)=PHI2(JET)
$2(JZ)=EM(2,1)=PHI1(JET)+JM(2,2)=PHI2(JET)
                                                                                                                      NAMP 337
                                                                                                                      NAMP 338
                                                                                                                      NAMP 339
          GO TO 450
                                                                                                                      NAMP 340
   420 EON=EXP(-G*DELT(JZ))
$1(JZ)=F1P*EON
                                                                                                                      NAMP 341
                                                                                                                      NAMP 342
          $2 (JZ) =F2 P*E IN
                                                                                                                      NAMP 343
          GO TO 450
                                                                                                                      NAMP 344
   43C H= DELT(JZ)

CALL MMMM(DMEGA, AKX, AKY, C, VX, VY, H, EM)

51(JZ) = EM(2, 2) = PH(1 (1DA) - EM(1, 2) = PH(2 (1DA)

11(3) = EM(2, 1) = BM(1(1DA) + EM(1, 1) = PH(2(1DA)
                                                                                                                      NAMP 345
                                                                                                                      KAMP 346
                                                                                                                                     PROGRAM
                                                                                                                      NAMP 347
                                                                                                                                       NAMPDE
                                                                                                                     NAMP 348
          $2(JZ)=-EM(2,1)*PHI1(IDA)+EM(1,1)*PHI2(IDA)
   450 CONTINUE
                                                                                                                                          PAGE
                                                                                                                      NAMP 350
```

```
C AT THIS POINT S1(JZ), $2(JZ), CIJZ(JZ), ETC. ARE $TORED FOR JZ=1 AND 2.

C ME COMPUTE THE DOPPLER SHIFTED ANGULAR FREQUENCY AT SOURCE ALTITUDE.

100 BCM=OMEGA-AKX** VXIJZ(NSCRCE) -AK*** VYYIJZ(NSCRCE)

C ME COMPUTE ZFN AT OBSERVER ALTITUDE

2FN=(.0098/CIJZ(NOBS))*$1(NOBS)-CIJZ(NOBS)*$2(NOBS)

C HERE HE TAKE THE ACCELERATION OF GRAVITY TO BE .0098 KM/SEC**2.

C COMPUTATION OF INTEGRALS

1T=3

CALL TOTINT(OMEGA, AKX, AKY, IT, L, X3, PM11, PH12)

1F(L .EQ. -1) GO TO 200

1T=1

CALL TOTINT(OMEGA, AKX, AKY, IT, L, X7, PM11, PH12)

1F(L .EQ. -1) GO TO 200

C FINAL ANSWER

AMP 366

AMP 367

C FINAL ANSWER

AMPLTD= 0.5*$2(NSCRCE)*2FN/((X3+KT)**HOM)

RETURN

C IF YOU ARRIVE HERE, THE UPPER BOUNDARY CONDITION COULD NOT BE SATISF1E

NAMP 376

NAMP 377

NAMP 376

END
```

PROGRAM NAMPDE

```
c
           NADEN (SUBROUTINE)
                                                                         7/25/68
                                                                                                                                   NMDF
                                                                                                                                    NHOF
                                  ---- ABSTRACT----
                                                                                                                                    NMNE
                                                                                                                                    MOF
C TITLE - NMDFN
                SUBRCUTINE TO COMPUTE THE NORMAL MODE DISPERSION FUNCTION FPP
                                                                                                                                    NMDF
                FOR GIVEN ANGULAR FREQUENCY OMEGA, PHASE VELOCITY MAGNITUDE VPHSE AND PHASE VELOCITY DIRECTION THETK. FPP SHOULD VANISH IF BOTH UPPER AND LOWER BOUNCARY CONDITIONS ARE SATISFIED FOR
0000000
                                                                                                                                    NMOF
                                                                                                                                    NMDF
                                                                                                                                   NMDF
                THE SCLUTIONS OF THE RESIDUAL EQUATIONS
                                                                                                                                    NMDF
                                                                                                                                              10
                                                                                                                                    NMDF
                       D(PHII)/DZ = A(1.1)*PHII(Z) + A(1.2)*PHI2(Z)
                                                                                                                                   NMDF
                                                                                                                                              12
                                                                                                                                    NMOF
                                                                                                                                              13
                       D(PHI2)/DZ = A(2,1)*PHI1(Z) + A(2,2)*PHI2(Z)
                                                                                                                                    NMDF
00000
                                                                                                                                              15
                                                                                                                                   NMOF
                WHERE THE ELEMENTS OF THE MATRIX A VARY WITH HEIGHT Z. BUT ARE
                                                                                                                                   NMDF
               CONSTANT IN EACH LAYER OF A MULTILAYER ATMOSPHERE. THE OF A ARE FUNCTIONS OF OMEGA, AKX AND AKY AS DESCRIBED IN
                                                                                                           THE ELEMENT
                                                                                                                                   NMDF
                                                                                                                                              17
                                                                                                                                    NMDF
                                                                                                                                              18
                                                                                                                                    NMDF
00000000
                                                                                                                                   NMOF
                                                                                                                                              20
                       AKX= OMEGA+CO S(THETK)/VPHSE
                                                                                                                                   NMDF
                       AKY=OMEGA+SIN(THETK)/VPHSE
                                                                                                                                   NMDE
                                                                                                                                              23
               THE FUNCTION FPP IS DEFINED AS THE VALUE OF PHI1 AT THE GROUND (2=0) WHEN (1) THE UPPER BOUNDARY CONDITION CF PHI1 AND PHI2 DECREASING EXPONENTIALLY WITH HEIGHT IN THE UPPER HALFSPACE IS SATISFIED, AND (2) PHI1 AND PHI2 AT THE BCTTOM OF THE UPPER HALFSPACE ARE GIVEN BY A(1,2) AND -(G+A(1,1)) WHERE G=SORT(A(1,1)++2+A(1,2)+A(2,1)). THE ELEMENTS OF A HERE ARE THOSE APPROPRIATE TO THE UPPER HALFSPACE. CCNDITIONS (1) AND (2) ARE NOT INDEPENDENT. *CONDITION (1) IMPLIES THAT G++2.GT. AND CUNDITION (2) WITH G++2 POSITIVE IMPLIES (1). IF G++2 IS NEGATIVE, FPP DOES NOT EXIST AND L=-1 1S RETURNED. OTHERWISE L=1 IS RETURNED.
                                                                                                                                    NFDF
                                                                                                                                    NMDF
                                                                                                                                              25
                                                                                                                                              26
27
                                                                                                                                    AMDE
                                                                                                                                    NMDF
                                                                                                                                   NMDF
0000
                                                                                                                                   NMDF
                                                                                                                                              29
                                                                                                                                    MMDF
                                                                                                                                              30
                                                                                                                                    NMDF
                                                                                                                                              32
33
                                                                                                                                   AMDE
                                                                                                                                    MMDF
                                                                                                                                   NHOF
                L=1 IS RETURNED.
                                                                                                                                   NAUE
                                                                                                                                              35
                                                                                                                                   NHDF
   PROGRAM NOTES
                                                                                                                                    NPDF
                                                                                                                                   NMDF
                                                                                                                                              38
                           THE PARAMETERS DEFINING THE MULTILAYER MODEL ATMOSPHERE
                                                                                                                                    NMDF
                           ARE PRESUMED TO BE STORED IN COMMON.
                                                                                                                                   NMDF
                                                                                                                                              40
                                                                                                                                   APDE
                                                                                                                                              41
                           THE SUBROUTING RRRR IS USED TO GENERATE THE MATRIX RPP WHICH CONNECTS SOLUTIONS OF THE RESIDUAL EQUATIONS AT THE BOTTOM OF THE UPPER HALFSPACE TO SCLUTIONS AT THE GROUND. IN TERMS OF THIS MATRIX, THE NMDF IS GIVEN BY
                                                                                                                                   NMDF
                                                                                                                                   NMDF
                                                                                                                                              43
                                                                                                                                   NMDF
                                                                                                                                   NMDF
                                                                                                                                   NMDF
                            FPP= RPP(1.1) + A(1.2) - RPP(1.2) + (G+A(1.1))
                                                                                                                                   NMDF
   LANGUAGE
                     - FORTRAN IV (360, REFERENCE MANUAL C28-6515-4)
                                                                                                                                   NMDE
                                                                                                                                   MOF
                                                                                                                                              50
                       - A.C.PIERCE, M.I.T., AUGUST,1968
                                                                                                                                    NPOF
   AUTHOR
                                                                                                                                    NMDE
                                                                                                                                   NMDF
                                  ---- CALL ING SEQUENCE----
                                                                                                                                    NHOF
   SEE SUBROUTINES LNGTHN. WIDEN. MPOUT
                                                                                                                                   APDF
           DIMENSION CI(100); VXI(100); VYI(100); HI(100)
COMMON IMAX; CI; VXI; VYI; HI (THESE MUST BE STORED IN COMMON)
CALL NMOFN(OMEGA; VPHSE; THETK; L; FPP; K)
                                                                                                                                   NHDF
                                                                                                                                    MMDE
                                                                                                                                   NMDF
                                                                                                                                              58
                                                                                                                                   NMOF
                                  ----EXTERNAL SUBROUTINES REQUIRED----
                                                                                                                                   NMDF
                                                                                                                                              60
                                                                                                                                   NMOF
           RRRR, MMMF, AAAA, CAI, SAI
                                                                                                                                   NMDF
                                                                                                                                   NHOF
                                                                                                                                              63
                                  ---- ARGUMENT LIST----
                                                                                                                                   NMDF
                                                                                                                                              64
                                                                                                                                    NMDF
           OMEGA
                                                                                                                                              66
67
                              R=4
                                                      INP
                                                                                                                                   NADE
                                                                                                                                                     PROGRAM
           VPHSE
                                           ND
                                                      INP
                                                                                                                                   NMDF
                                                                                                                                                         NADEN
           THETK
                                                      INP
                                                                                                                                    NMOF
                                                     out
                               1=4
                                           ND
                                                                                                                                   NMDF
                                                                                                                                              69
                                                                                                                                                          PAGE
           FPP
                                                     OUT
                                                                                                                                   NMDF
```

```
OUT (ALWAYS RETURNED AS K=O)
                                                                                                                    NMDF
                                                                                                                    NMDF
NMDF
   CCPMON STORAGE USED
         COMMON IMAX, CI, VXI, VYI, HI
                                                                                                                    NMDF
                                                                                                                             75
76
77
                                                                                                                    NMDF
                                                                                                                    NHOF
          XAMI
                                     ND
                                               INP
                          Ω×4
R≠4
                                      100
                                                                                                                    NMDF
          VXI
                                                                                                                    NMDF
                                      100
                                               INP
                           R#4
                                      100
                                                                                                                    NADE
          VYI
                                               INP
                                                                                                                    NMDF
NMDF
                           R*4
                                      100
                                               INP
                              ---- INPUT S----
                                                                                                                    NMDF
                                                                                                                    MMOF
                                                                                                                    NMDF
         OMEGA
                            =ANGULAR FREQUENCY IN RAD/SEC
                            #ANGULAR FREQUENCY IN RAD/SEC
#PHASE VELOCITY MAGNITUDE IN KM/SEC
#PHASE VELOCITY DIRECTION RECKONED COUNTER CLOCKWISE
FROM THE X AXIS IN RADIANS
#NUMBER OF LAYERS OF FINITE THICKNESS
#SOUND SPEED IN KM/SEC IN I-TH LAYER
#X COMPONENT OF WIND VELOCITY IN I-TH LAYER (KM/SEC)
#Y COMPONENT OF WIND VELOCITY IN I-TH LAYER (KM/SEC)
#THICKNESS IN KM OF I-TH LAYER OF I-TH THICKNESS
                                                                                                                    NMDF
                                                                                                                    HMOF
         THETK
                                                                                                                    NMDF
          IMAX
                                                                                                                    NMDF
         AX1(1)
                                                                                                                    NMDF
                                                                                                                             89
                                                                                                                    NMDF
0000000000000
         VYECTE
                                                                                                                    NMDF
                                                                                                                    NMDF
         HI(I)
                                                                                                                    NMDF
                              ---- OUTPUTS----
                                                                                                                    NMDE
                                                                                                                    NMDF
                            =1 IF NORMAL MODE DISPERSION FUNCTION EXISTS, -1 IF IT DOES NOT. =NORMAL MODE DISPERSION FUNCTION =DUMMY PARAMETER ALWAYS RETURNED AS K=0
                                                                                                                    NMDF
                                                                                                                    NMDF
                                                                                                                    NHDF
                                                                                                                    NMDF 99
                              ---- PROGRAM FOLLOWS BELOW----
                                                                                                                    NMDF
                                                                                                                    NMDF 102
                                                                                                                    NMDF
         SUBROUTINE NMOFN(OMEGA, VPHSE, THETK, L, FPP, K)
                                                                                                                           103
C
                                                                                                                    NMDF
   DIMENSION AND COMMON STATEMENTS LOCATING PARAMETERS DEFINING MODEL
C
                                                                                                                    NMDF 105
  MULTILAYER ATMOSPHERE

DIMENSION CI(100), VXI(100), VYI(100), HI(100)

COMMCN IMAX, CI, VXI, VYI, HI
                                                                                                                    NMDF 106
                                                                                                                    NMDF 107
                                                                                                                    NMDF 108
                                                                                                                    HMDF 109
         DIMENS (CN A(2.2). RPP(2.2)
                                                                                                                    NMDF 110
                                                                                                                    NMDF 111
C COMPUTATION OF AKX AND AKY
AKX=OMEGA+COS(THETK)/VPHSE
                                                                                                                    NMOF 112
NMOF 113
          AKY=OMEGA+SIN(THETK)/VPHSE
                                                                                                                    NMDF
                                                                                                                   NMDF 115
NMDF 116
C CCMPUTATION OF MATRIX A AND G++2 FOR UPPER HALFSPACE
         J=IMAX+1
C=C1(J)
VX=VX1(J)
                                                                                                                    NMDF
                                                                                                                    NMDF 118
                                                                                                                    NMDF
                                                                                                                   NMDF
NMDF
          (L) IYV=YV
         CALL 44A4(OMEGA,AKX,AKY,C,VX,VY,A)
GUSQ=A(1,1)++2+A(1,2)+A(2,1)
                                                                                                                    NMDF
C
                                                                                                                    NMDF
         [F(GUSQ .GT. 0.0) GO TO 11
                                                                                                                    NMDF
                                                                                                                    NMDF
C GUSQ IS LESS THAN ZERO
                                                                                                                    NMDF
                                                                                                                    NMDF
         L=-1
RETURN
                                                                                                                   NMDF 128
NMDF 129
C GUSQ IS GREATER THAN ZERO
                                                                                                                    NMDF
                                                                                                                    NMDF 131
         GU=SQRT (GUSQ)
                                                                                                                    NADE
                                                                                                                           132
                                                                                                                    NMDF 133
NMDF 134
C COMPUTATION OF RPP MATRIX
CALL RRRR(OMEGÁ+AKX+AKY+RPP+K)
                                                                                                                    NMDF
                                                                                                                           135
C COMPUTATION OF FPP
FPP=RPP(1,1)*A(1,2)=RPP(1,2)*(GU+A(1,1))
                                                                                                                    NMDF 136
                                                                                                                                   PROGRAM
                                                                                                                    NMDF 137
                                                                                                                                      NMDFN
                                                                                                                    NMDF 138
                                                                                                                    NMOF 139
                                                                                                                                        PAGE
          RETURN
                                                                                                                    NMDF 140
```

and the state of

51

NMDF 141 END

PROGRAM NMDFN

```
NXMODE (SUBROUTINE)
                                                            6/24/68
                                                                                                              CMXA
                                                                                                              NXND
                                                                                                              NXMD
                            ----AB STR ACT----
                                                                                                              AXMD
                                                                                                              NXMD
C TITLE - NXMODE
                                                                                                              CMXA
             PROGRAM TO FIND A POINT WITH COORDINATES I * IFNO , J=JFNO IN AN
                                                                                                              MXMD
            GPX
                                                                                                              NYMO
                                                                                                              DMXM
                                                                                                                       10
                                                                                                              DMX/A
                                                                                                              NXHD
                                                                                                              NXMO
                                                                                                              NXMD
                                                                                                                       15
                                                                                                              NYMD
             THE FOLLOWING RULES.
                                                                                                              NXHD
                                                                                                                       18
                                                                                                              NX MD
                      1. IT MUST LIE BELOW OR TO THE LEFT OF A POINT WITH
                                                                                                              NXHD
                                                                                                                       20
                            OPPOSITE INMODE
                                                                                                              GMXA
                                                                                                                       21
                                                                                                              NX MO
                           IF MUST BE THE HIGHEST POINT (LOWEST I) IN THE REGION
                                                                                                              NXHD
                                                                                                                       23
                            SATISFYING CONDITION 1
                                                                                                              NXMD
                                                                                                              NXMD
                           IF MORE THAN 1 POINT SATISFY 1 AND 2, THEN THE POINT DETERMINED IS THAT FURTHEST TO THE LEFT.
                                                                                                              OMXM
                                                                                                                       26
                                                                                                              DMXM
                                                                                                              NXMD
                                                                                                                       28
                           ONLY POINTS IN THE RECTANGLE ARE CONSIDERED
                                                                                                              NXMD
                                                                                                              NXHD
            THE COMPUTATION ASSUMES REGION OF SUCCESSIVELY ADJACENT POINTS HAVING SAME INMODE IS SIMPLY CONNECTED AND THAT PHASE VELOCITY CURVES BEND DOWNWARDS, I.E., DIVP)/DIOM) .LT. O. (THIS CAN BE THE CASE PROVIDING VP IS GREATER THAN THE MAXIMUM WIND VELOCITY.) IF THE POINT IS FOUND, K=1, IF NOT FOUND, K=-1.
                                                                                                              NXMO
                                                                                                                       31
                                                                                                              DPXN
                                                                                                              NXMO
                                                                                                              OM XA
                                                                                                              NXMD
                                                                                                              NXMD
                   - FORTRAN IV (360, REFERENCE MANUAL C28-6515-4)
- A.D.PIERCE, M.I.T., JUNE, 1968
                                                                                                              NXMD
  LANGUAGE
                                                                                                                      37
                                                                                                              OMXN
                                                                                                              OMXIA
                                                                                                                      39
                                                                                                              DMXA
                            ----CALLING SEQUENCE----
                                                                                                                       40
                                                                                                              NXMD
  SEE SUBROUTINE ALLMOD
                                                                                                              NXMD
         DIMENSION INMODE(1)
                                                                                                              NXMD
                                                  (VARIABLE DIMENSIONING)
         CALL NXMODE (IST. JST. NOM, NVP, INMODE, IFND, JFND, K)
                                                                                                              NXMD
                                                                                                                      45
                                                                                                              OM XA
  NO EXTERNAL SUBROUTINES ARE REQUIRED
                                                                                                              NXMD
                                                                                                              DHXA
                      ---- ARGUMENT LIST----
                                                                                                              NX MO
                                                                                                                       48
                                                                                                              NXMD
         IST
                                            INP
                                                                                                              AXMO
                                                                                                                       50
                                            INP
                         1+4
                                                                                                              NXMD
                                   ND
         JST
         NOM
                          1+4
                                             INP
                                                                                                              NXMD
                                   ND
        NVP
                         1 + 4
                                   ND
                                            INP
                                                                                                              DMXA
                                                                                                                       53
         INMODE
                                   VAR
                                            INP
                                                                                                              NXMD
         TEND
                         1 *4
                                   ND
                                            OUT
                                                                                                              NX MD
         JF NO
                         1+4
                                   ND
                                            OUT
                                                                                                              NXHD
                                                                                                                       56
                                                                                                              NXMD
                                   ND
                                                                                                              NX MO
  NO COMMON STORAGE USED
                                                                                                              NX MD
                                                                                                              NXMD
                           ----INPUTS----
                                                                                                              CP XN
                                                                                                              1.X 40
                                                                                                                      62
                          *ROW INDEX OF START POINT

*COLUMN INDEX OF START POINT

*NO. OF COLUMNS OF ARRAY

*NO. OF ROWS OF ARRAY

*SIGN OF NORMAL MODE DISPERSION FUNCTION, I IF PCS.,

-1 IF NEG., 5 IF IT DOESN'T EXIST. LET I=L MOD NVP,

J={L-II/NVP+1. INMODE(L) IS SIGN OF NMOF FOR

OMEGA=C-4(J), PHASE VEL. = VP(I), WHERE OM(J) .GE. CM(J)
        151
                                                                                                              NXMD
        JST
                                                                                                              OP XA
         NOM
                                                                                                              NXMD
                                                                                                                      65
        NVP
                                                                                                              DMXA
                                                                                                                            PROGRAM
         INMODELLI
                                                                                                              DMXM
                                                                                                                      67
                                                                                                                              NX MODE
                                                                                                              NXHD
                                                                                                              OM X A
                                                                                                                                 PAGE
                                                                                                              GPXN
                                                                                                                                    53
```

```
AND VP(I) .LE. VP(I-1).
                                                                                                     NYMO
                                                                                                     AX MD
                                                                                                             72
                          ----OUT PUTS----
                                                                                                     NXMD
                                                                                                             74
75
                                                                                                     NXMD
                        =ROM INDEX OF FOUND POINT

=COLUMN INDEX OF FOUND POINT

=FLAG INDICATING IF'POINT (IFND, JFND) IS FOUND, 1 IF
        IFND
                                                                                                     NXMD
                                                                                                     NXMD
                                                                                                             77
                                                                                                     NXMD
                                                                                                     NXMD
                          YES. -1 IF NO.
                                                                                                             78
                                                                                                     NXMD
                          ----FX AMPI E----
                                                                                                     NXMO
                                                                                                             AΩ
                                                                                                     NXMD
                                                                                                             81
C SUPPOSE THE ARRAY OF INMODE VALUES IS AS SHOWN BELOW
                                                                                                     NXMD
                                                                                                     NXMD
                                                                                                             83
                                             NVP=8, NOM=11
                                                                                                     NXMO
                                                                                                             84
                    ******
                                                                                                     OM XA
                    5----+++
                                         IF IST=8.JST=5 THEN IFND=3.JFND=2.K=1
                                                                                                             86
87
                                                                                                     NXMD
                    55----+++
                                                              THEN IFAD=1,JFND=9,K=1
                                         IF IST=2,JST=5
                                                                                                     NXMD
                                         IF IST=3, JST=7
IF IST=8, JST=2
                    55----+
                                                              THEN 1FND=3,JFND=2,K=-1
                                                                                                     NXMD
                    55-----
                                                              THEN K =-1
                                                                                                     NXMD
                                                                                                             89
                                         IF IST=2.JST=11 THEN K=-1
                                                                                                     DH KA
                                                                                                             90
                                                                                                     DMXM
                                                                                                     NXMD
                                                                                                             92
                                                                                                             93
                                                                                                     NXMD
                          ---- PROGRAM FOLLOWS BELOW----
                                                                                                     NXMD
                                                                                                             95
                                                                                                     NXMD
                                                                                                     DMXA
                                                                                                             96
        SUBROUTINE NAMODE(IST.JST.NOM.NVP.INMODE.IFND.JFND.K)
                                                                                                     NXMD
c
                                                                                                     NX MO
                                                                                                             98
                                                                                                     NXMD
        DIMENSION INMODE(1)
     1 if( 1ST .GT. NVP .GR. JST .GT. NOM) GC TO 100

10 = INMODE((JST-1)=NVP+IST)
                                                                                                     NXMD 100
                                                                                                     NXMO 101
     3 IF( 10 .NE. 1 .AND. 10 .NE. -1) GO TO 100
                                                                                                     NXMD
                                                                                                            102
                                                                                                     DM XA
                                                                                                            103
C THE POINT (IST, JST) LIES IN THE ARRAY AND THE NORMAL MODE DISPERSION C FUNCTION EXISTS AT THIS POINT WITH A SIGN IC. WE FIRST GO UP UNTIL C A DIFFERENT INMODE IS ENCOUNTERED OR UNTIL WE REACH I=1
                                                                                                     NXMD 104
                                                                                                     NXMD
                                                                                                            105
                                                                                                     NXMD
                                                                                                            106
                                                                                                     NXMD 107
        I = IST
                                                                                                            108
         J=JST
                                                                                                     NXMD
    10 IF( I .EQ. 1) GO TO 30 I=I-1
                                                                                                     NXMD 109
                                                                                                     NXMD 110
        ICHK = INMODE ((J-1) +NVP+I)
         IF( ICHK .EQ. 10) GO TO 10
                                                                                                     NXMD 112
                                                                                                     NXMD 113
                                                                                                     NXMD
C THE CURRENT I IS NOT 1. IF THE ICHK OF THE POINT ABOVE IS NOT 5. WE C MOVE TO THE LEFT.

15 IF( ICHK .EQ. 5) GO TO 50

IF( I .EQ. 1) GO TO 20
                                                                                                     NXMD 115
                                                                                                     NXMD 116
                                                                                                     DMXA
                                                                                                     NXMD 118
                                                                                                     NXMD 119
        ICHK=INPCDE ((J-1)*NVP+I)
                                                                                                     NXMD
                                                                                                     NXMD 121
C IF THE ICHK-OF THE CONSIDERED NEW POINT IS IO, WE TRY TO GO HIGHER
                                                                                                     NXMD 122
C AGAIN.

IF(ICHK .EQ. 10) GO TO 10
                                                                                                     NXMD
                                                                                                     DHX A
                                                                                                            124
                                                                                                     DMXA
                                                                                                     NXMD 126
C WE MAVE -10 AROVE THE CURRENT POINT AND ARE FITHER ON THE FAR LEFT OF C THE TABLE OR FLSF HAVE A DIFFERENT SIGN AT THE POINT TO THE LEFT. C THIS IS INTERPRETED AS SUCCESS.
                                                                                                     NXMD
                                                                                                            127
                                                                                                     NXMD 129
NXMD 130
    20 K=1
        IFND=1
                                                                                                     NXMD 132
NXMD 133
        JFND=J
        RETURN
                                                                                                     NXMO 134
C THE CONSIDERED NEW POINT IS ON THE FIRST ROW. WE GO TO THE RIGHT.
30 IF( J .EQ. NOM) GO TO 60
J=J+1
                                                                                                     NXMO 135
                                                                                                     NXMD 136
                                                                                                                  PROGRAM
                                                                                                     NXMD 137
                                                                                                                    NXMODE
        ICHK=INMODE((J-1)*NVP+1)
IF( ICHK .EQ. (0) GO TO 30
                                                                                                     NXMD 138
                                                                                                     NX40 139
                                                                                                                       PAGE
                                                                                                     NXMD 140
```

```
AXMD 141
  IF THE POINT AT THE RIGHT OF CURRENT (1.J) IS -10. WE HAVE SUCCESS
         IF( ICHK .FQ. -10) GO TO 20
                                                                                                                AXMD 143
                                                                                                                AXMD 144
C IF IT IS NOT -10, WE ALLOW FOR POSSIBILITY OF INMODES=5 IN UPPER RIGHT C HAND CORNER OF THE TABLE AND TRY TO SKIRT THESE FIVES BY MOVING EITHER C DOWNWARDS OR TO THE RIGHT.
                                                                                                               AXMD 146
NXMD 147
    40 IFE 1 .EQ. NVP) GO TO 70
                                                                                                               NXMD 149
NXMD 150
         1=1+1
         ICHK=INMODE((J-1)*NVP+I)
  IF THIS ICHK IS +10 WE ARE IN A POSITION TO MAKE A TRY OF MOVING TO
                                                                                                               NXMO 152
                                                                                                               NXMD 153
C THE PIGHT.
                                                                                                                NXMD 154
    44 IFI ICHK .NE. 101 GO TO 80
                                                                                                                NYMO
                                                                                                                       155
  IF WE ARE ON THE RIGHT HAND SIDE OF THE TABLE THE DESIRED POINT CANNOT
                                                                                                               AXMD 156
C RE FOUND. WE RETURN WITH K=-1
                                                                                                               NXMD 157
    45 IFC J .EQ. NOM! GO TO 100
                                                                                                                NXMD 158
                                                                                                                AXMD 159
        J=J+1
                                                                                                               NXMD 160
C IT IS TAKEN FOR GRANTED THAT THE INMODE OF POINT ABOVE CURRENT (1, J)
C IS 5 SINCE IT WAS FOUND TO BE 5 TO THE LEFT AND AROVE. THE INMODE OF
C THE POINT TO THE LEFT IS 10. IF THE NEW INMODE IS +10, WE HAVE TO TRY
C TO MOVE FURTHER TO THE RIGHT.
ICHK=IN*CDE((J-1)*NVP+1)
IF (ICHK .EQ. IO ) GO TO 45
                                                                                                               NXMD
                                                                                                               NXMD 162
                                                                                                               NXMD 163
                                                                                                               NX40
                                                                                                               6.XMD 165
                                                                                                               NXM9 166
                                                                                                                NXMD 167
                                                                                                               NX40 168
  IF THE CURRENT ICHK IS 5. WE TRY TO GO DOWN AGAIN. THE OTHER POSS-IBILITY. ICHK=-10 INDICATES SUCCESS

IFI ICHK .EQ. -10) GO TO 20
                                                                                                               NX49 169
                                                                                                                NX40 170
                                                                                                               NXMD 171
                                                                                                               NX40 172
         GC TC 40
C WE CONTINUE HERE FROM 15. THE POINT ABOVE THE CURRENT (1.J) HAS C ICHK .EQ. 5. THE SITUATION IS SUCH THAT WE CAN RESUME CALCULATION C AT 45 AND TRY TO MOVE FURTHER TO THE RIGHT.
                                                                                                               NXMD 174
NXMD 175
                                                                                                                       176
    50 GO TO 45
                                                                                                                NX4D 177
                                                                                                               NX40 178
C WE CONTINUE HERE WITH I=1.J=NOM FROM STATEMENT 30. SINCE WE HAVE NO C PLACE TO GO THE SEARCH IS UNSUCCESSFUL. WE RETURN WITH K=-1.
                                                                                                                NXMD 180
    60 GO TO 100
                                                                                                               NXMD 181
                                                                                                                NX MD 182
C WE CONTINUE FERE FROM STATEMENT 40 WITH I .EO. NVP AND INMODERS TO THE C RIGHT OF THE CURRENT (1,J). WE RETURN WITH KR-1. 70 GO TO '
                                                                                                               AXMO 183
                                                                                                               NX40 184
                                                                                                                NXMD 185
                                                                                                               NXMD 186
C WE CONTINUE HERE FROM STATEMENT 44 WITH THE POINT BELOW HAVING
                                                                                                               NX40 187
  ICHK .NE. 10. THE POINT AT THE RIGHT HAS ICHK .EQ. 5. WE CANNOT SKIRT THE FIVES AND HENCE WE RETURN WITH K=-1.
                                                                                                               NXMD 199
     80 GO TC 100
                                                                                                               NXMD 190
                                                                                                                KX40 191
C WE CONTINUE MERE FROM 1.3.45.60.70.0R 80. THE SEARCH WAS UNSUCCESSFUL
                                                                                                               NXMD 192
                                                                                                               NX40 163
   100 K=-1
         KETUPN
         END
                                                                                                               NX40 145
```

128, GR 44

```
NXTPNT (SUBROUTINE)
                                                                                                                                                                  AXPT
                                                                                                                                                                   NXPT
                                                                                                                                                                  NYPT
                                         ---- ABSTRACT----
                                                                                                                                                                   AXPT
                                                                                                                                                                   NXPT
                  PROGRAM TO FIND THE NEXT POINT (12, J2) OF AN ARRAY OF NROW ROWS AND NCCL CLUMNS GIVEN THE PRECEDING PRINT (11, J1). POINT WILL BE USED IN SUBSPOUENT CALCULATION OF A PARTICULAR POINT ON THE PHASE VELOCITY VERSUS FREQUENCY CURVE OF A GIVEN GUIDED MODE. A TABLE OF VALUES OF THE SIGN OF THE NORMAL PCDE DISPERSION FUNCTION IS PRESUMED TO SETONED AS INMI(J-1)=NVP+11 FOR FACH PRINT (1, J) IN THE ARRAY. DIFFERENT COLUMNS (J) CORRESPOND TO DIFFERENT FREQUENCIES WHILE DIFFERENT REMS (I) CORRESPOND TO DIFFERENT PHASE VELOCITIES. SUCCESSIVE POINTS ARE CHARACTERIZE BY A TYPE, ITYPI IS TYPE OF (11, J1) WHILE TYPE IS TYPE OF SECOND POINT. THE TYPE INDEX IS I IF THE POINT DIRECTLY ABOVE THE CONSIDERED POINT HAS AN INM OF OPPOSITE SIGN. IT IS 2 IF THE POINT TO THE RIGHT HAS INM OF OPPOSITE SIGN. SINCE BOTH POSSIBILITIES CAN OCCUR, THE DESIGNATED TYPE INDEX ITYPI PENDTE
   TITLE - NYTENT
                                                                                                                                                                   AYPT
                                                                                                                                                                  KXPT
                                                                                                                                                                  NXPT
                                                                                                                                                                  NXPT
                                                                                                                                                                  NXPT
                                                                                                                                                                  NXPT
                                                                                                                                                                  AXPT
                                                                                                                                                                  NXPT
                                                                                                                                                                   NXPT
                                                                                                                                                                  NXPT
                                                                                                                                                                  NXPT
                                                                                                                                                                  KXPT
                                                                                                                                                                   AXPT
                                                                                                                                                                   NXPT
                  THE DERIVED VALUES OF 12, J2, ITYP2 ARE CALCULATED AS FOLLOWS.
                                                                                                                                                                  NXPT
                                                                                                                                                                  NXPT
                                                                                                                                                                  NXPT
                                                                                                                                                                   NXPT
                                                                                                                                                                   NX PT
                                1. IF ITYP1 IS 1 AND INM OF POINT TO RIGHT IS OPPOSITE OF IO=INM((J-1)*NVP+I). THEN IZ=I1.JZ*J1.ITYP2*2.
                                                                                                                                                                   NXPT
                                                                                                                                                                  NYPT
                                                                                                                                                                   NXPT
                                        THE POINT (12.J2) MUST FITHER BE THE DIRECTLY ADJACEN POINT TO THE RIGHT (11.J1+1), THE POINT DIRECTLY BELO (11+1.J1), OR THE ADJACENT POINT TO THE LOWER RIGHT
                                                                                                                                                                  NXPT
                                                                                                                                                                  NXPT
                                                                                                                                                                  NXPT
                                                                                                                                                                                ٦0
                                          (11+1.J1+1) IF CONDITION 1 BOES NOT HOLD
                                                                                                                                                                  NXPT
                                                                                                                                                                  NYPT
                                3. THE CHOSEN POINT MUST HAVE THE SAME INM AS (11,J1)
                                                                                                                                                                  NXPT
                                         AND HAVE A POINT EITHER DIRECTLY ARCVE OR DIRECTLY TO THE RIGHT WITH OPPOSITE INM.
                                                                                                                                                                  NXPT
                                                                                                                                                                  NXPT
                                                                                                                                                                               35
                                                                                                                                                                  NXPT
                                4. IN THE EVENT MORE THAN ONE POINT SATISFY CONDITIONS 2 AND 3, PRIORITY OF SELECTION IS (1) THE POINT TO THE RIGHT, (2) THE POINT DIRECTLY BELOW, (3) THE POINT TO THE LOWER RIGHT. IF THE S'LECTED POINT SATISFIES CRITERIA FOR BOTH ITYP2=1 OR 2, ITYP2=1 IS RETURNED. OTHERWISE, THE APPROPRIATE ITYP? IS RETURNED DEPENDING.
                                                                                                                                                                  KYPT
                                                                                                                                                                  NXPT
                                                                                                                                                                  NXPT
                                                                                                                                                                  NXPT
                                                                                                                                                                               40
                                                                                                                                                                  NXPT
                                                                                                                                                                  NXPT
                                         ON WHICH CRITERION IS SATISFIED.
                                                                                                                                                                  NYPT
                                                                                                                                                                  NXPT
                   THE COMPUTATION ASSUMES REGION OF SUCCESSIVELY ADJACENT POINTS
                                                                                                                                                                  NXPT
                   HAVING SAME INM TO BE SIMPLY CONNECTED AND THAT PHASE VELOCITY CURVES SEND DOWNWARDS, I.E., DIVPI/DICM) .LT. O. IF NEW POINT IS FOUND, K=+1. IF IT IS NOT FOUND, K=-1.
                                                                                                                                                                  NXPT
                                                                                                                                                                  NXPT
                                                                                                                                                                  NXPT
                                                                                                                                                                  AXPT
                            - FORTRAN IV (360, REFERENCL MANUAL C28-6515-4)
- A.O.PIERCE, M.I.T., JUNE,1968
C LANGUAGE
                                                                                                                                                                  NXPT
                                                                                                                                                                   NXPT
                                                                                                                                                                  NXPT
                                          ---- CALL ING SEQUENCE----
                                                                                                                                                                  NXPT
                                                                                                                                                                  NXP7
   SEC SUBPLUTINE MOUETR
                                                                                                                                                                  NXPT
            OIMFOSTEN (MMODE(1) (INMODE IS SAME AS INM)
CALL NXTPNT([],J],ITYP1,I2,J2,ITYP2,NRCW,NCOL,INMODE,K)
IF( K .EC. -1) GO SOMEWHERE
                                                                                                                                                                   NXPT
                                                                                                                                                                  NXPT
                                                                                                                                                                  NXPT
             USE 12.12.1TYP2
                                                                                                                                                                  NXPT
                                                                                                                                                                  TAXA
   NO EXTERNAL LIBRARY SUBROUTINES ARE REQUIRED
                                                                                                                                                                  NXPT
                                                                                                                                                                   AXPT
                                 ---- AP CHMENT LIST----
                                                                                                                                                                  NXPT
                                                                                                                                                                               63
                                                                                                                                                                  NYPT
                                                                  INP
             11
                                                                                                                                                                  NYPT
                                                                                                                                                                  NXPT
                                                                  INP
                                                                                                                                                                                        PROGRAM
                                                    NO
                                                                                                                                                                               66
             TTYPI
                                     1 44
                                                                  INP
                                                                                                                                                                  NX PT
                                                                                                                                                                                           NXTPNT
             12
J2
                                     1:4
                                                    ND
                                                                  Out
                                                                                                                                                                  NYPT
                                     1 - 4
                                                                                                                                                                                              PAGE
                                                                                                                                                                  NXPT
                                                    NU
                                                                  001
                                                                                                                                                                  KXPT
                                                                  nut
                                                                                                                                                                               70
```

6/24/58

```
C
         NROW
                                   ΝĐ
                                            INP
                                                                                                             NYDT
                                            INP
         NCOL
                                   ND
                                                                                                             NXPT
         INH
                                   VAR
                                                                                                             NXPT
                                   NO
                                            ถบา
                                                                                                             HYPT
                                                                                                             NXPT
                                                                                                                      75
   NC CCMMCN STORAGE USED
                                                                                                             NXPT
                                                                                                             NYPT
                            ---- INPUTS----
                                                                                                             NXPT
                                                                                                             NXPT
                          =ROW INDEX OF START POINT
=COLUMN INDEX OF START POINT
=TYPE INDEX OF START POINT, 1 MEANS POINT ABOVE HAS
         11
                                                                                                             NYPT
                                                                                                                      80
                                                                                                             NXPT
                                                                                                                      81
         ITYPL
                                                                                                             NXPT
                            DIFFERENT INM, 2 MEANS POINT TO RIGHT HAS DIFFERENT
                                                                                                             MYDT
                                                                                                                      83
                                                                                                             NXPT
                            INM.
                          INM.

**NUMBER OF KOWS IN ARRAY

**NUMBER OF COLUMNS IN ARRAY

**SIGN OF NORMAL MODE DISPERSION FUNCTION, 1 IF POS.,

-1 IF NEG., 5 IF IT DOESN'T EXIST. LET I**L MOD NVP,

J=(L-I)/NVP+1. INMIDE(L) IS SIGN OF NMDF FOR

OMEGA=OM(J), PHASE VEL. **VP(I), WHERE OM(J) .GE. CM(J

AND VP(I) .LE. VP(I-1)
         NROW
                                                                                                             NXPT
         NCOL
                                                                                                             NXPT
                                                                                                                      46
                                                                                                             NXPT
                                                                                                                      87
         INM
                                                                                                             NXPT
                                                                                                                      89
90
                                                                                                             NXPT
С
С
С
                                                                                                             NXYT
                                                                                                             NXPT
С
С
С
                                                                                                                      92
93
                                                                                                             AXPT
                            ----OUT PUTS----
                                                                                                             NAPT
                                                                                                             NXPT
                          =ROW INDEX OF FOUND POINT
=COLUMN INDEX OF FOUND POINT
=TYPE INDEX OF FOUND POINT
         12
                                                                                                             NXPT
                                                                                                                      95
                                                                                                             NXPT
         J2
ITYP 2
                                                                                                             NXPT
                           *FLAG INDICATING IF POINT (12,J2) IS FOUND, 1 IF YES, -1 IF NO
                                                                                                             NXPT
                                                                                                                      QR
                                                                                                             NXFT
                                                                                                             NXPT 100
                            ---- FXAMPLE ----
                                                                                                             MXPT 101
                                                                                                             NXPT 102
                                                                                                             NXPT 103
   SUPPOSE THE ARRAY OF INM VALUES IS AS SHOWN BELOW
                                                                                                             NXPT 104
                                                                                                             NXPT 105
                                                NRCW#8. NC UL=11
                       +++++++--
                                                                                                             NXPT 106
                                            NXPT 107
NXPT 108
                       5-----+++
                      55----+++
                      55----+
                                                                                                             NXPT 109
                                            IF Il=1,J1=9,ITYP1=2 THEN 12=2,J2=10,
                                                                                                             NXPT 110
                      55----+
                                                 ITYP2=1,K=1
                                                                                                             NXPT 111
                      55----+
                                                                                                             NXPT 112
                                                                                                             NXPT 113
                                            IF 11=3,J1=7,1TYP1=1 THEN 12=3,J2=7,
                                                                                                             NXPT 114
                                                 1TVP2=2,K=1
                                                                                                             NXPT 115
                                            1F 11=3,J1=11,TTYP1=1 THEN K=-1
                                                                                                             NXPT 116
                                                                                                             NXPT 117
                                                                                                             NXPT 118
                            ----PROGRAM FOLLOWS BELOW----
                                                                                                             NXPT 119
c
                                                                                                             NXPT 120
                                                                                                             NXPT 121
         SUBROUTINE NXTPNT(11,J1,ITYP1,12,J2,ITYP2,NROW,NCOL,INM,K1
                                                                                                             NXPT 122
c
                                                                                                             NXPT 123
      9!MENSION [NM(1)

!O#!NM((JI-1)*NROW+!!)

! IF( !O .EQ. 5 .OR. !! .GT. NROW .OR. J! .GE. NCCL) GO TO 30
                                                                                                             NXPT 124
                                                                                                             NXPT 125
                                                                                                             NXPT 126
                                                                                                             NXPT 127
NXPT 128
C IR IS INM OF POINT TO THE RIGHT. TO IS INM ME POINT (11, J1).
      5 [R= INM((J))*NKOW+[1)
6 [F( IR .NE. 10 ) GO TO 15
7 [F( ]] .EQ. [ ) GO TO 30
                                                                                                             NXPT 129
                                                                                                             NXPT 130
                                                                                                             NXPT 131
                                                                                                             NXPT 132
C IR HAS THE SAME SIGN AS 10. WE CHECK IRU REPRESENTING INM OF UPPER C RIGHT POINT. IF THIS IS -10, THE RIGHT POINT IS THE DESIRED POINT.
C IF IT IS NOT -10, WE CANNOT FIND (12, J2).
10 IPJ=[NM((J1)*NROH+11-1)
11 IF( IRU .NE. -10 ) GG TO 30
                                                                                                             NXPT 133
                                                                                                             NXPT 134
                                                                                                             NXPT 135
                                                                                                             NXPT 136
NXPT 137
                                                                                                                            PROGRAM
                                                                                                                              NX TPNT
         [TYP2=1
                                                                                                             NXPT 138
                                                                                                             NXPT 139
NXPT 140
         12=11
                                                                                                                                PAGE
         J2=J1+1
```

```
NXPT 141
NXPT 142
NXPT 143
C
C WE ARRIVE HERE FROM STATEMENT 6. THE POINT TO THE RIGHT HAS A C DIFFERENT INM. IF THIS IS -10 AND ITYP1=1, WE HAVE (12,J2)=(11,J1) C WITH ITYP2=2. IF THIS IS 5, WE CANNOT FIND (12,J2). 15 IF( IR .EQ. 5 ) GO TO 30
                                                                                                                        NXPT 144
                                                                                                                       NXPT 145
NXPT 146
                                                                                                                        NXPT 147
                                                                                                                        NXPT 148
C IR=-10 AT THIS POINT
IF( ITYP1 .NE. 1 ) GO TO 25
12=11
                                                                                                                        NXPT 149
                                                                                                                       NXPT 150
NXPT 151
                                                                                                                       NXPT 152
          ITYP2=2
                                                                                                                       NXPT 153
NXPT 154
          RETURN
                                                                                                                        NX PT 155
                                                                                                                       NXPT 156
NXPT 157
NXPT 158
C IR=-IC. ITYP1 IS 2. WE CONTINUE FROM STATEMENT 15. IF WE ARE ON THE C BOTTOM ROW, WE CANNOT FIND NEW POINT 25 IF (II. EQ.NROW) GO TO 30
                                                                                                                       NXPT 159
                                                                                                                       NXPT 160
C WE CONSIDER PCINTS BELOW AND TO LOWER RIGHT ID=INM((J1-1)*NROW+I1+1)
IDR=INM((J1)*NROW+I1+1)
                                                                                                                        NXPT 161
                                                                                                                       NXPT 162
NXPT 163
C
                                                                                                                        NXPT 164
C IF 1DR IS 5. WE CANNOT FIND THE NEW POINT 26 IF1 IDR .EQ. -5 1 GO TO 30
                                                                                                                       NXPT 165
                                                                                                                        NXPT 166
                                                                                                                       NXPT 167
C IF 10R IS IC. THE NEXT POINT IS THE DR POINT 27 IF( IDR .NE. TO ) GO TO 28 I2=I1+1 J2=J1+1
                                                                                                                       NXPT 168
                                                                                                                       NXPT 169
                                                                                                                       NXPT 170
                                                                                                                       AXPT 171
NXPT 172
          1 TYP2 = 1
         K=1
PETURN
                                                                                                                       NXPT 173
                                                                                                                       NXPT 174
NXPT 175
C IR=-10, ITYP1 IS 2, IOR IS -10. WE CONTINUE FROM STATEMENT 27.
28 IF( ID .NE. IO ) GO TO 30
                                                                                                                       NXPT 176
                                                                                                                       NXPT 177
                                                                                                                       NXPT 178
C THE NEXT POINT IS THE DOWN POINT
                                                                                                                       NXPT 179
          12=1)+1
J2=J1
                                                                                                                       NXPT 180
                                                                                                                       NXPT 181
          ITYP2=2
                                                                                                                       NXPT 182
                                                                                                                       NXPT 183
          RETURN
                                                                                                                       NXPT 184
C WE ARRIVE HERE FROM 1,7,11,15,25,26. THE NEXT POINT CANNOT BE FOUND
                                                                                                                       NXPT 185
NXPT 186
     30 K=-1
RETURN
                                                                                                                        AXPT 187
                                                                                                                       NXPT 188
          END
                                                                                                                       NXPT 189
```

PROGRAM NXTPNT

```
C
          PAMPDE (SUBROUTING)
                                                                     7/30/68
                                                                                                                             PAMP
                                                                                                                             PAMP
                                ---- AB STRACT----
                                                                                                                             PAMP
                                                                                                                             PAMP
   TITLE - PAMPDE
                                                                                                                             PAMP
               PROGRAM TO COMPUTE AND STORE, AMPLITUDE FACTORS AMP(J) AND FACT
                                                                                                                             PAMP
               AND SCALING FACTOR ALAM. THE QUANTITY AMPLIJI IS OMNODIJI AND THE PHASE VELOCITY IS VPMODIJI. IT CORRESPONDS TO THE NMODE-TH GUIDED MODE WHEN J IS BETWEEN KST(NMODE) AND KFIN(NMODE), INCLUSIVE. THE QUANTITY FACT IS DEPENDENT ON
                                                                                                                             PAMP
                                                                                                                             PAMP
                                                                                                                             PAMP
                                                                                                                             PAMP
                                                                                                                                       10
               KFININMODE), INCLUSIVE. THE QUANTITY FACT IS DEPENDENT ON SOURCE ALTITUDE ZSCRCE AND OBSERVER ALTITUDE ZOBS AND IS GIVEN
                                                                                                                             PAMP
                                                                                                                             PAMP
                                                                                                                             PAMP
                                                                                                                             PAMP
                  FACT = CONST+CI(1)+UED+(PSCRCE/1.E6)++0.3333333
                                                                                                                             PAMP
              WHERE CONST=4.0/SQRT(2*PI), CI(1) IS THE SOUND SPEED AT THE GROUND, (PSCRCE/1.66) IS THE AMBIENT PRESSURE AT ZSCRCE DIVIDED BY THE AMBIENT PRESSURE AT THE GROUND. THE CUANTITY UED IS THE SQUARE ROOT OF (AMBIENT DENSITY AT ZOBS)/(AMBIENT DENSITY A
                                                                                                                             PAMP
                                                                                                                             PAMP
                                                                                                                             PAMP
               ZSCRCE ). THE SCALING FACTOR ALAM IS GIVEN BY
                                                                                                                             PAMP
                                                                                                                                       20
                                                                                                                             PAMP
                  ALAM = (1.E6/PSCRCE)++(0.333333)+(CI(1)/CI(ISCR)
                                                                                                                             PAMP
                                                                                                                             PAMP
                                                                                                                                       23
               WHERE CI(ISCR) IS THE SOUND SPEED AT THE SOURCE ALTITUDE.
                                                                                                                             PAMP
               SIGNIFICANCE OF THESE QUANTITIES IS EXPLAINED IN SUBROUTINE
                                                                                                                             PAMP
                                                                                                                             PAMP
               PPAMP.
                                                                                                                                       26
   PROGRAM NOTES
                                                                                                                             PAMP
                                                                                                                                       28
                                                                                                                             PAMP
                         THE PARAMETERS IMAX.CI.VXI.VYI.HI DEFINING THE MULTILAYER
                                                                                                                             PAMP
                         ATMOSPHERE ARE PRESUMED STORED IN COMMON. THE AMBIENT PRESSURES ARE COMPUTED BY CALLING SUBROUTINE AMBNT WHICH ALSO COMPUTES THE INDICES IOBS AND ISCR OF THE LAYERS IN WHICH OBSERVER AND SOURCE, RESPECTIVELY, LIE.
                                                                                                                             PAMP
                                                                                                                                       31
                                                                                                                             PAMP
                                                                                                                                       32
                                                                                                                             PAMP
                                                                                                                             PAMP
                                                                                                                             PAMP
                         IN COMPUTING AMBIENT DENSITIES, THE IDEAL GAS LAW RHO= GAMMA*P/C**2 IS USED. THUS UED = (CI(ISCR)/CI(IDRS))
                                                                                                                             PAMP
                                                                                                                             PAMP
                                                                                                                                       37
                          SQRT(POBS/PSCRCE).
                                                                                                                             PAMP
                                                                                                                                       38
                                                                                                                             PAMP
                         IF NPRNT IS POSITIVE, A HEADING IS PRINTED FOR A TABLE TO BE PRINTED BY SUBROUTINE NAMPDE. SEE FORMAT STATEMENT 19 FOR THE DEFINITIONS OF TERMS IN THE HEADING. PHI1 AND PHI2 SATISFY THE RESIDUAL EQUATIONS PRESENTED IN THE
                                                                                                                             PAMP
                                                                                                                                       40
                                                                                                                             PAMP
                                                                                                                             PAMP
                                                                                                                             PAMP
                                                                                                                                       43
                         ABSTRACT OF NAMPDE.
                                                                                                                             PAMP
                                                                                                                             PAMP
   LANGUAGE - FORTRAN IV (360, REFERENCE MANUAL C28-6515-4)
                                                                                                                             PAMP
                                                                                                                                       46
                                                                                                                             PAMP
   AUTHORS
                      - A.D. PIERCE AND J. PUSEY, M.I.T., JULY, 1968
                                                                                                                             PAMP
                                                                                                                             PAMP
                                                                                                                              PAMP
                                ---- CALLING SEQUENCE----
                                                                                                                             PAMP
   SEE THE MAIR PROGRAM
                                                                                                                             PAMP
   DIMENSION CI(100), VXI(100), VYI(100, +HI(100)
DIMENSION KST(1), KFIN(1), OMMOD(1), VPMOD(1), AMP(1)
THE PROGRAM USES VARIABLE DIMENSIONING FOR QUANTITIES IN ITS
                                                                                                                              PAMP
                                                                                                                                       54
55
                                                                                                                             PAMP
                                                                                                                             PAMP
    ARGUMENT LIST.
                                                                                                                              PAMP
          COMMON IMAX.CI.VXI,VYI.HI THESE MUST BE STORED IN COMMON)
CALL PAMPDE(ZSCRCE,ZOBS,MDFND,KST,KFIN,OMMCD,VPMOD,AMP,ALAM,
                                                                                                                             PAMP
                                                                                                                             PAMP
        1 FACT. THETK , NPRNT)
                                                                                                                             PAMP
                                                                                                                             PAMP
                                                                                                                                       60
                                                                                                                             PAMP
                                ---- EXTERNAL SUBROUTINES REQUIRED----
                                                                                                                             PAMP
                                                                                                                             PAMP
          AMBNT, NAMPDE, TOTINT, MMMM, AAAA, USEAS, UPINT, ELINT, 8888, CAI, SAI
                                                                                                                             PAMP
                                 ---- ARGUMENT LIST----
                                                                                                                             PAMP
                                                                                                                             FAMP
                                                                                                                                              PROGRAM
                                                                                                                                       66
          ZSCRCE
                                                   INP
                                                                                                                             PAHP
                                                                                                                                                PAMPDE
                                        ND
NO
          ZOBS
                             8#4
                                                   INP
                                                                                                                             PAMP
                                                                                                                                       68
           MDFND
                                                                                                                             PAMP
                                                   INP
                                                                                                                                                   PAGE
                                                                                                                             PAMP
                                         VÁR
```

```
KFIN
                                                                                                                                                      PAMP
             OMMOD
                                   R # 4
                                                 VAR
                                                             INP
                                                                                                                                                      PAMP
              VPHOD
                                   R#4
                                                 VAR
                                                                                                                                                      PAMP
                                                             INP
             AMP
                                   R*4
                                                             OUT
             AL AM
                                   R#4
                                                 NO
                                                             OUT
                                                                                                                                                      PAMP
             FACT
                                   R#4
                                                 ND
                                                             OUT
                                                                                                                                                     PAMP
PAMP
             THETE
                                   R * 4
                                                 ND
                                                                                                                                                     PAMP
PAMP
             NPRNT
                                   1+4
                                                 NO
                                                             INP
                                                                                                                                                                  79
    COMMON STORAGE USED
                                                                                                                                                      PANP
                                                                                                                                                                  80
            COMMON IMAX,CI,VXI,VYI,HI
                                                                                                                                                     PAMP
PAMP
                                                             INP
             1 MAX
                                   1#4
                                                                                                                                                      PAMP
            CI
                                   R*4
                                                 100
                                                             INP
                                                                                                                                                     PAMP
            1 X V
                                   R#4
                                                 100
                                                                                                                                                      PAMP
                                                             INP
                                                                                                                                                                  85
            VYI
                                   2+4
                                                 100
                                                             INP
                                                                                                                                                     PAMP
                                                 100
                                                             INP
                                                                                                                                                     PAMP
                                                                                                                                                                  87
                                                                                                                                                      PAMP
                                                                                                                                                                  88
                                       ----INPUTS----
                                                                                                                                                     PAMP
                                                                                                                                                     PAMP
                                                                                                                                                                  90
                                     NHEIGHT IN KM OF BURST ABOVE GROUND
NHEIGHT IN KM OF OBSERVER ABOVE GROUND
NUMBER OF GUIDED MODES FOUND
            ZSCRCE
                                                                                                                                                      PAMP
             2085
                                                                                                                                                     PAMP
PAMP
                                                                                                                                                                  93
                                     EINDEX OF FIRST TABULATED POINT IN N-TH MODE INDEX OF LAST TABULATED POINT IN N-TH MODE. IN GERERAL, KFIN(N)=KST(N+1)-1.
            KST(N)
                                                                                                                                                     PAMP
            KFIN(N)
                                                                                                                                                     PAMP
                                                                                                                                                                  95
                                    GERERAL, KFIN(N)=KST(N+1)-1.

**ARRAY STORING ANGULAR FREQUENCY ORCINATE (RAC/SEC) OF POINTS ON DISPERSION CURVES. THE NMODE MODE IS STORE FOR N BETWEEN KST(NMODE) AND KFIN(NMODE), INCLUSIVE.

**ARRAY STORING PHASE VELOCITY ORDINATE (KM/SEC) OF POINTS ON DISPERSION CURVES. THE NMODE MCDE IS STORE FOR N BETWEEN KST(NMODE) AND KFIN(NMODE).

**DIRECTION IN RADIANS TO OBSERVER FRCM SOURCE, RECKONE COUNTER CLOCKWISE FROM X AXIS.

**PRINT OPTION INDICATOR (SEE NAM! IN MAIN PROGRAM).

**NUMBER OF LAYERS OF FINITE THICKNESS.

**SOUND SPEED IN KM/SEC IN 1-TH LAYER

**X COMPONENT OF WIND VELOCITY IN 1-TH LAYER (KM/SEC)

**Y COMPONENT OF WIND VELOCITY IN 1-TH LAYER (KM/SEC)

**THICKNESS IN KM OF 1-TH LAYER CF FINITE THICKNESS
                                                                                                                                                     PAMP
            OMMODICAL
                                                                                                                                                     PAMP
                                                                                                                                                     PAMP
                                                                                                                                                                 98
            VPKCDINI
                                                                                                                                                     PAMP
                                                                                                                                                               100
                                                                                                                                                     PAMP
                                                                                                                                                               101
                                                                                                                                                     PAMP
            THETK
                                                                                                                                                     PAMP
                                                                                                                                                               103
                                                                                                                                                     PAMP
                                                                                                                                                               104
            NPRNT
                                                                                                                                                     PAMP
             IMAX
                                                                                                                                                     PAMP 106
            (1)15
                                                                                                                                                     PAMP 107
            VX1(1)
                                                                                                                                                     PAMP 108
             111144
                                                                                                                                                     PAMP 109
            HI(I)
                                     =THICKNESS IN KM OF I-TH LAYER CF FINITE THICKNESS
                                                                                                                                                     PAMP
                                                                                                                                                     PAMP 111
                                                                                                                                                     PAMP
                                       ----OUTPUTS----
                                                                                                                                                              112
                                                                                                                                                     PAMP
            AMP(J)
                                    *AMPLITUDE FACTOR FOR GUIDED WAVE EXCITED BY POINT
                                                                                                                                                     PAMP 114
                                    *AMPLITUDE FACTOR FOR GUIDED MAVE EXCITED BY POINT ENERGY SOURCE. UNITS ARE KM**(-1). THE J-TH ELEMENT CORRESPONDS TO ANGULAR FREQUENCY OMMOD(J) AND PHASE VELOCITY VPMOD(J). THE AMPLITUDE FACTOR IS APPROPRIA TO THE NMODE-TH MODE IF J .GE. KST(NMODE) AND J .LE. KF IN(NMODE). THE AMP(J) IS THE SAPE AS AMPLTO COMPUT BY SUBROUTINE NAMPOE.
                                                                                                                                                     PAMP
                                                                                                                                                     PAMP
                                                                                                                                                     PAMP 117
                                                                                                                                                     PAMP
                                                                                                                                                     PAMP
                                                                                                                                                     PAMP
                                                                                                                                                              120
                                     *A SCALING FACTOR DEPENDENT ON HEIGHT OF BURST, EQUAL TO CUBE ROOT OF (PRESSURE AT GROUND)/(PRESSURE AT
            AL AM
                                                                                                                                                     PAMP
                                                                                                                                                     PAMP
                                                                                                                                                              122
                                       BURST HEIGHT) TIMES (SCUND SPEED AT GROUND)/(SOUND
                                                                                                                                                     PAMP
                                     SPEED AT BURST HEIGHT).

AGENERAL AMPLITUDE FACTOR DEPENDENT ON BURST HEIGHT
AND OBSERVER HEIGHT. A PRECISE DEFINITION IS GIVEN
IN THE ABSTRACT.
                                                                                                                                                    PAMP
PAMP
            FACT
                                                                                                                                                              125
                                                                                                                                                     PAMP
                                                                                                                                                     PAMP
                                                                                                                                                              127
                                                                                                                                                     PAMP
                                                                                                                                                               128
                                      ----PROGRAM FOLLOWS BELOW----
                                                                                                                                                    PAMP
PAMP
                                                                                                                                                              1 30
            SUBROUTINE PAMPOELZSCRCE, ZOBS, MUFNO, KST, KFIN, OMMCD, VPMOC, AMP, ALAM.
                                                                                                                                                    PAMP
                                                                                                                                                    PAMP
PAMP
          1 FACT, THETK, NPRNT)
                                                                                                                                                              133
C DIMENSION AND COMMON STATEMENTS
                                                                                                                                                     PAMP
            DIMENSION ([(100), VX[(100], VY[(100], H[(100)
DIMENSION KST(10), KFIN(10), CMMOD((1000), VPMOD((1000), AMP(1000)
                                                                                                                                                    PAMP
                                                                                                                                                              135
                                                                                                                                                    PAMP
                                                                                                                                                                         PROGRAM
                                                                                                                                                              136
                                                                                                                                                    PAMP 137
PAMP 138
            COMMON IMAX,CI,VXI,VYI,HI
                                                                                                                                                                          PAMPDE
            MDFND = MDFND
                                                                                                                                                    PAMP
                                                                                                                                                                               PAGE
            1F (NPRNT . LT. 0) GO TO 20
                                                                                                                                                    PAMP 140
```

```
C PRINT HEADING FOR PHIL AND PHIL PROFILE DATA TO BE PRINTED BY NAMPDE
                                                                                                                                 PAMP 141
     WRITE (6,19)
19 FORMAT (1H1,41X,26HPH11 AND PH12 PROFILE DATA ///63H01AP1MX = NC.
                                                                                                                                  PAMP 142
        1 OF LAYER FOR WHICH ABSIPHII(TAPINX): IS A MAXIMUM/63H TAP2MX = NO.
2 OF LAYER FOR WHICH ABSIPHII(TAPINX): IS A MAXIMUM/63H TAP2MX = NO.
3 OF LAYER FOR WHICH ABSIPHII(TAP2MX)): /42H R? = PHI2(TAP2MX) / ABSIPH
4 IZ(TAP2MX) / 3/H R3 = PHI2(T) / ABSIPHIZ(TAP2MX)) /40H NZCT
5 = NO. OF TIMES PHII CHANGES SIGN /40H NZCZ = NC. OF TIMES PHIZ C
6 HANGES SIGN.
                                                                                                                                  PAMP 144
                                                                                                                                 PAMP
                                                                                                                                           145
                                                                                                                                  PAMP
                                                                                                                                 PAMP
                                                                                                                                          147
                                                                                                                                  PA4P 148
         SHANGES SIGNI
     20 CONTINUE
                                                                                                                                  PARP 150
C DO LOOP TO COMPUTE AMP(J)

DO 25 II=1,MOFND

IF (NPRNT-LT-0) GO TO 23
                                                                                                                                 PAMP 151
                                                                                                                                  PAMP
                                                                                                                                 PAMP 153
     WRITE (6,27) 11
22 FORMAT (1H ///// 1H ,51x,5HMODE ,12 /// 1H ,7x,5HOMEGA,7x,5HVPHSE 1,6X,6HIAP1Mx,10X,2HR1,8X,4HNZC1,6X,6HIAP2MX,10X,2HR2,8X,4HNZC2,10X
                                                                                                                                  PAMP 154
                                                                                                                                 PAMP
         2.2HR3 /1
                                                                                                                                  PAMP 157
     23 J1=KST(11)
                                                                                                                                  PAMP
           J2=KFIN(II)
                                                                                                                                  PAMP 159
                                                                                                                                  PAMP 160
           DO 25 J=J1,J2
                                                                                                                                 PAMP 161
          OMEGA = CMMOD(K)
                                                                                                                                  PAMP 162
           VPHSE = VPMOD(K)
                                                                                                                                  PAMP 163
           CALL NAMPOF (ZSCRCE, ZOBS, OMEGA, VPHSE, THETK, X, NPRNT)
                                                                                                                                  PAMP 164
           AMP(K) = X
                                                                                                                                  PA4P 165
     25 CONTINUE
                                                                                                                                  PAMP 166
C END OF DU LOOP
                                                                                                                                  PAMP 167
                                                                                                                                  PAMP 168
C COMPUTATION OF AMBIENT PRESSURES
                                                                                                                                 PAMP 169
          CALL AMENT(7SCRCE,PSCRCE,ISCR)
CALL AMENT(7985,POBS,1085)
                                                                                                                                  PAMP 170
                                                                                                                                  PAMP
C COMPUTATION OF SQRT(DENSITY RATIO)
                                                                                                                                  PAMP 172
                                                                                                                                  PAMP
                                                                                                                                          173
           UED = (CI(1SC4)/CI(108S)) * SQRT(POBS/PSCRCE)
                                                                                                                                  PAMP
                                                                                                                                  PAMP 175
C CCMPUTATION OF ALAM AND FACT

ALAM#(1.66/PSGRCE)**(0.333333)*(CI(1)/CI(ISCR))

C NOTE THAT CI(1) IS SOUND SPEED AT THE GROUND

CONST = 4.0/SORT(2.0*3.141593)

FACT = CONST*(CI(1)*UED*(PSCRCE/1.66)**(0.3333333))
                                                                                                                                  PAMP
                                                                                                                                  PAMP
                                                                                                                                  PAMP 178
                                                                                                                                  PAMP 179
                                                                                                                                  PAMP 180
     IF(NPRNT .NE. 1) RETURN
WRITE (6,31) ZSCRCE, ZOBS, FACT, ALAM
31 FORMAT(1H1, ZOX, 36HTABULATION OF
                                                                                                                                  PAMP 181
                                                                                                                                  PAMP 182
        ##11 (0,31) 25CRCE, 2005, FACT, ALAM

FORMATITHI, 20x, 36HTABULATION OF SOURCE FREE AMPLITUDES,

1 23H FROM SUBROUTINE PAMPDE //21x, 19HHEIGHT OF BURST =,

1 F8.3, 3H KM / 21x, 19HHFIGHT OF CHSERVER=, F8.3, 3H KM/

1 21x, 4HFACT, 14x, 1H=, F8.3, 7H KM/SFC/ 21x,4HALAM,14x, 1H=,
                                                                                                                                  PAMP 183
                                                                                                                                  PAMP 184
                                                                                                                                 PAMP 185
                                                                                                                                  PAMP
         1 F8.31
                                                                                                                                  PAMP 187
     1 F8.3)
DO 50 II =1, MOFND
WRITE (6,41) II
41 FORMAT( 1H /// 1H , 5HMODE , I3/ 1H , 20X,5HOMEGA,
1 15X, 5HVPHSE, 17X, 3HAMP)
                                                                                                                                 PAMP 188
                                                                                                                                  PAMP 185
                                                                                                                                  PAMP 190
                                                                                                                                 PAMP 191
                                                                                                                                  PAMP 192
                                                                                                                                 PAMP 193
PAMP 194
           K2=KFIN(II)
     00 50 J=K1,K2
50 WRITE (6,51) OMMOD(J),VPMOD(J),AMP(J)
                                                                                                                                  PAMP 195
      51 FORMAT(1H ,4X,F20.5,F20.5,F20.8)
                                                                                                                                 PAMP 196
           RETURN
                                                                                                                                  PAMP 197
                                                                                                                                 PAMP 198
```

PROGRAM PAMPDE

```
PHASE ISUBROUTINES
                                             8/15/68
                                                                                 PHAS
                                                                                 PHI S
                                                                                 PHAS
                      ---- ABSTPACT ----
                                                                                 PHAS
                                                                                 PHAS
C TITLE - PHASE
                                                                                 PHAS
          CONVERSION OF A COMPLEX NUMBER FROM RECTANGULAR FORM TO POLAR
          FORM
                                                                                 PHAS
                                                                                 PHA S
                GIVEN TWO REAL NUMBERS RR AND RI. A MAGNITUDE R AND AN
                                                                                 PHAS
                ANGLE PHI ARE COMPUTED SUCH THAT
                                                                                 PHAS
                                                                                 PHAS
                      RR + [#R] = R + [XP[ [*PH] ]
                                                                                 PHAS
                                                                                 PHA S
                WHERE 1 = (-1)=+0.5 .
                                                                                 PHAS
                                                                                 PHAS
C LANGUAGE - FORTRAN IV (360, REFERENCE MANUAL C28-6515-4)
                                                                                 PHAS
                                                                                 PHAS
             - A.C.PIFRCE AND J.POSEY. M.I.T., AUGUST, 1968
                                                                                PHAS
                                                                                       19
20
C AUTHORS
                                                                                 PHAS
                                                                                PHAS
PHAS
                     ----US AGE ----
      NO SUBROUTINES ARE CALLED
                                                                                 PHAS
                                                                                 PHAS
                                                                                PHAS
C FORTRAN USAGE
                                                                                 PHAS
      CALL PHASE(RR.RI.R.PHI)
                                                                                PHAS
                                                                                       29
3 C
3 I
                                                                                 PHAS
                                                                                PHAS
PHAS
C INPUTS
                REAL PART OF THE COMPLEX NUMBER BEING CONVERTED
                                                                                 PHAS
                                                                                PHAS
                                                                                 PHAS
     RI
R×4
                IMAGINARY PART OF COMPLEX NUMBER BEING CONVERTED
                                                                                 PHAS
                                                                                PHAS
                                                                                 PHAS
                                                                                PHAS
PHAS
  CUTPUTS
                                                                                       39
                MAGNITUDE OF THE COMPLEX NUMBER
       R * 4
                                                                                PHAS
                                                                                PHAS
     PHI
                PHASE OF THE COMPLEX NUMBER (RADIANS) (-PI.LT.PHI.LE.PI)
                                                                                PHAS
PHAS
                                                                                 PHAS
                     ---E XAMPLE S----
                                                                                       47
                                                                                 PHAS
                                                                                PHAS
      CALL PHASE(0.0,1.0,R.PHI)
                                                                                 PHAS
                                                                                       50
                                                                                PHAS
              R = 1.0 AND PHI = 1.570796 ARE RETURNED
                                                                                PHAS
                                                                                PHAS
                                                                                       53
54
55
      CALL PHASEIL.O.-1.0.R.PHII
                                                                                PHAS
                                                                                PHAS
                P = 1.414214 AND PHI = -C.7853972 ARE RETURNED
                                                                                PHAS
                                                                                PHAS
                                                                                PHAS
                     ---- PROGRAM FOLLOWS BELOW----
                                                                                PHAS
                                                                                PHAS
                                                                                PHAS
      SUBPOUTINE PHASEIRR, RI, R, PHI)
                                                                                       61
                                                                                PHAS
PHAS
      2=ABS(RR)+ABS(RT)
                                                                                       63
      1F1Q-1.E-251 1.1.37
                                                                                       64
    1 R = 7.0
PH[=0.0
                                                                                PHAS
                                                                                       66
                                                                                           PREGRAM
                                                                                PHAS
                                                                                PHAS
                                                                                             PHASE
      RETUPA
                                                                                PHAS
PHAS
                                                                                       68
69
   30 48 = RK/7
                                                                                               PAGE
      ALPRI/S
      A+5Q4T ( AR ++ ++ A 1 ++ 21
```

f

R=Q*A
PH1=ARSIN(ABS(AI1/A)
PH35 72
IF(RR) 50,60,60
PHAS 73
50 IF(RI) 300,300,20C
PHAS 74
60 IF(RI) 40C,400,100
PHAS 75
ICC PHI=PHI
RETURN
PHAS 77
200 PH1=3,1415927-PHI
RETURN
PHAS 78
RETURN
PHAS 78
RETURN
PHAS 79
RETURN
PHAS 80
PHI=PHI-3,1415927
PHAS 81
RETURN
PHAS 81
RETURN
PHAS 82
END

~ ~~ \$ 585 to 2

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PRCGRAM PHASF

```
PPAMP (SUBROUTINE)
                                                      7/30/68
                                                                                                  DDAM
                                                                                                  PPAM
                         ----ABSTRACT----
                                                                                                  PPAH
                                                                                                  PPAM
C TITLE - PPAMP
                                                                                                  PPAM
           PROGRAM TO COMPUTE AND STORE APPLITUDE ARRAY AMPLITO AND PHASE ARRAY PHAS 3 FOR GUIDEO WAVES EXCITED BY A POINT ENERGY SOURCE WITH TIME DEPENDENCE CORRESPONDING TO A NUCLEAR EXPLOSION OF
                                                                                                  PPAM
                                                                                                  PPAM
                                                                                                  PPAM
            ENERGY DENOTED BY YIELD IN KT. THE VALUES FOLAR ARE TO BE SUBSEQUENTLY USED BY TMPT ACCORDING TO THE RELATION
           ENERGY DENOTED BY YIELD IN KT.
                                                                                                  PPAM
                                                                                                  PPAM
                                                                                                          10
            IPRESSURE IN DYNES/CM##2 FOR A GIVEN MODEL#SORTION
                                                                                                  PPAM
                                                                                                  PPAM
               * INTEGRAL OVER OMEGA OF AMPLITO+COS(OMEGA*(T-R/VP)+FHASQ)
                                                                                                  PPAM
            THE QUANTITIES AMPLTO AND PHASY ARE BOTH DEPENDENT ON ANGULAR
                                                                                                  PPAM
           FREQUENCY AND ARE DIFFERENT FOR DIFFERENT MODES.
                                                                                                  PPAM
  PROGRAM NOTES
                                                                                                  PPAM
                   IN THE FORMULATION FOR A PCINT ENERGY SOURCE. THE ENERGY
                                                                                                  PPAM
                    EQUATION IS WRITTEN
                                                                                                  PPAM
                     DP/DT - (C##21D(RHQ1/DT # 4*PI*C #*2*F(T)*(DELTA FNCTN )
                                                                                                  PPAM
                   AN EXPRESSION FOR F(T) IS
                                                                                                  PPAM
                                                                                                  PPAM
                     FIT1 #1(L*#21/CS)#POS#(INTEGRAL OVER X FROM 0 TO CS#T/L
                                                                                                  DPAM
                             OF UNIVERSAL FUNCTION FUNIVIXIE
                                                                                                  PPAM
                   WITH L=(ENERGY/POS)=#(1/3) AND POS.CS REPRESENTING PRESSUR AND SOUND SPEED AT THE SOURCE. IF FIKT(T) IS THE PRESSUR AT A DISTANCE OF 1 KM FRUM A 1 KT EXPLOSION AT SEA LEVEL
                                                                                                 PPAM
                                                                                                          30
                                                                                                 PPAM
                                                                                                          31
                                                                                                  PPAM
                    AND WITH TIME ORIGIN COPRESPONDING TO BLAST WAVE ONSET.
                                                                                                  PPAM
                                                                                                  PPAM
                                                                                                  PPAM
                     FUNIV(x)=((L1*PO1)=*(-1))*F1KT(L1*X/C1)
                                                                                                  PPAN
                                                                                                          36
                   THE FOURIER TRANSFORM OF FIT) IS ACCORDINGLY FOUND TO BE
                                                                                                  PPAM
                                                                                                  PPAM
                     G(CMEGA)= (1/(2*P1))*(Y**(2/3))*(C1/CS)*(POS/PC1)**(1/3)
                                                                                                          40
                                                                                                  PPAM
                      *(1/(-1*CMEGA))*FTMAG(OMERAT)*EXP([*FTPHSE(CMERAT))
                                                                                                  PPAM
                                                                                                          47
                   WHERE Y IS YIELD IN KT, I=SORT(-1). AND CMERAT=ALAM=
                                                                                                  PPAM
                   OMEGA*Y**(1/3).
                                         THE FUNCTIONS FTMAG AND FTPHSE ARE AS
                                                                                                  PPAM
                                                                                                         45
                   COMPUTED BY SUBROUTINE SOURCE. THE QUANTITY ALAI
(C1/CS) + (P01/P0S) ++ 1/3 AS COMPUTED BY SUBROUTINE
                                                             THE QUANTITY ALAM IS
                                                                                                  PPAM
                                                                                                  FPAM
                                                                                                  PPAM
                                                                                                         48
                   A LENGTHY DERIVATION NOT GIVEN HERE INDICATES THAT
                                                                                                  PPAM
                      AMPL TO*EXP (~[*PHASQ)
                                                                                                  PPAM
                                                                                                  PPAM
                         = -4#SQRT(K) #G(OMEGA) #C S#UED#SQRT(2 P1)#AMP
                                                                                                  PPAM
                                                                                                  PPAM
                   WHERE AMP IS THE SAME AS THE AMPLTO COMPUTED BY NAMPDE AN WHERE UPD IS THE DENSITY FACTOR (CS/COBS)*SORT(PSCRCE/POB COMPUTED IN SURROUTINE PAMPDE. INSERTING GOMEGA) INTO THE ABOVE, WE IDENTIFY
                                                                                                 PPAM
                                                                                                          56
                                                                                                 PDAM
                                                                                                          58
                                                                                                          59
                                                                                                 PPAM
                                                                                                  PPAM
                      PHASO =(3/4)*PI - FTPHSE(OMERAT)
                                                                                                 PPAM
                                                                                                          61
                                                                                                  PPAM
                                                                                                         62
                      AMPLIDEFACT MAMPM(Y**(2/3))*FTMAG(OMERAT)*SQRT(K)/OMEGA
                                                                                                 PPAM
                                                                                                 PPAM
                   WHERE FACT IS 4/SQRT(2*PI)*C1*UEO*(PS/P1)**(1/3) AND IS
                                                                                                  PPAH
                                                                                                         65
                   COMPUTED BY SUBROUTINE PAMPOC.
                                                                                                 PPAM
                                                                                                               PROSRAM
                                                                                                 PPAM
                                                                                                         67
                                                                                                                 PPAMP
                   THE QUANTITIES FACT, ALAM, AND AMP ARE IN THE INPUT LIST OF THE SUBROUTINE. MOTE THAT THESE ARE YIELD INDEPENDENT
                                                                                                 PPAM
                                                                                                          69
                                                                                                 DDAM
                                                                                                                   PAGE
                                                                                                  PPAM
                                                                                                          70
                                                                                                                     64
```

```
ŘÍHĖSČCHEME OF STORAĞE FORSAMPLTDIJJ AND PHASOUJÍ ISSTHE
SAMESAS FORZUMMODIJY AND VPMODIJY SEE SUBROUTINE ARLMOD
                                                                                                                 PPAH
                                                                                                                 PPAH
                    ESFORTRANTY 1360; REFERENCE MANUAL C28 -6515-41:
                                                                                                                          74
75
   LANGUAGE
                                                                                                                  PPAM.
                                                                                                                  PPAM
   AUTHORS.
                    - A.D.PIERCE AND J.POSEY, M.I.T., JULY, 1968
                                                                                                                  ₽ΡÂ₩
                                                                                                                           7.7
78
                                                                                                                  PPAM
                                                                                                                  PPAH
                              ----CALLING. SEQUENCE----
                                                                                                                  PPAM
   SEE THE MAIN, PROGRAM
                                                                                                                  PPAH.
                                                                                                                           ۴Ñ
         DIMENSION KST (1) FOR IN(1) FOR MOD (1) FOR MOD (1) AMP (1)
                                                                                                                 PPAM.
          DIMENSTON APPLID (1) . PHASQ (1)
   DIMENSION APPLICATION APPLICATION ASSICMED PROGRAM-USES VARIABLE DIMENSIONING SER ACTUAL DIMENSIONS ASSICMED SEE THE MAIN PROGRAM.
                                                                                                                  PPA4
                                                                                                                  PPAM
                                                                                                                          84
85
         CALL PRAMP (YIELD, MOFNO, KST, KFIN, OMMCD, VPMCD, AMP, ALAM, FACT,
        1 AMPLTD, PHASQ1
                                                                                                                 PPÂM
                                                                                                                 PPAM
                                                                                                                           27
                             ---- EXTERNAL SUBROUTINES REQUIRED ----
                                                                                                                           883
                                                                                                                 PPAM'
         SOURCE: PHASE
c
                                    (PHASE IS CALLED BY SPURCE)
                                                                                                                  PPAM:
                                                                                                                           90
                                                                                                                  PPAM
                                  --ARGUMENT LIST----
                                                                                                                 PPAM
                                                                                                                 PPAM
PPAM
                                                                                                                          ∕ ĝ3,
σόσοδοδοσοσ
         VIELD
                                     ND
                                              ·INP
                                                                                                                          -94
          4DF NO
                                     N۵
         KST
                                     VAR
                                              INP
                                                                                                                  PAA
         KEIN
                                     VAR
                                              INP
                                                                                                                  PPAM-
                                                                                                                           97
                                     VAR
                                                                                                                  PPAM
                                                                                                                           98
          UPHOD.
                                     VAR
                                              INP
                                                                                                                  PPAM
                                                                                                                          99
          AMP
                          R=4
                                     VAR
                                              INP
                                                                                                                  PPAM®1 CO
          AL Á4
                                     ĊŃ,
                                                                                                                  PPAM
                                              INP
         FACT
                           9-4
                                     ND
                                                                                                                  PPAM
          AMPLI'D
                                     VAR
                                              OUT
                                                                                                                  PPAM 103
          PHASC
                                     VAR
                                                                                                                  PPAM
                                              OUT:
                                                                                                                         104
   -NO COMMON STORAGE IS USED
                                                                                                                  PPAM- 106
                                                                                                                 PPAM: 107
                             ---- INPUTS----
                                                                                                                  PPAM-108
                                                                                                                  PPAM 109
C.
C.
                            *ENERGY" RELEASE "OF" EXPLOSION" IN "EQUIVALENT" KILOTONS .OF
         VIELD'
                                                                                                                 PPAM-110
                              TNT. 1 KT = 4.2E19 ERGS.
                                                                                                                  PPAM°111
                                                                                                                  PPAM
0000000
                            *NUMBER OF MODES FOUND IN PREVIOUS TABULATION OF
          MOEND
                                                                                                                  PPAM: 113
                             DISPERSION CURVES.
                                                                                                                 PPAM 114
                            *INDEX: OF FIRST TABULATED POINT IN-NETH MODE.
                                                                                                                 PPAH
                           FINDEX OF LAST TABULATED POINT IN N-TH MODE. IN GENERAL, KFIN(N)=KST(N+1)-1.
         KFIN(N)
                                                                                                                  PPAM
                                                                                                                  PPAM 117
                            GENERAL, KFININ)=KST(N+1)-1.

#ARRAY STORING ANGULAR FREQUENCY ORCINATE OF POINTS
ON DISPERSION CURVES. THE MMODE MCDE IS STORED FOR
N BETWEEN KST (MMODE) AND KFININMODE).

#ARRAY STORING PHASE VELOCITY CROINATE OF POINTS ON
DISPERSION CURVES. THE NMODE MODE IS STORED FOR
N BETWEEN KST(NMODE) AND KFININMODE).

#AMPLITUDE FACTOR INDECENDENT OF YIELD COMPUTED BY
SUBROUTING PAMPOE CORRESPONDING TO ANGULAR FREQUENCY
OMMODIN) AND PHASE VELOCITY VPMODIA).
          04400 (N)
                                                                                                                  PPAK
                                                                                                                  PPAM
C
         VPMOD(N)
                                                                                                                  PPAM
                                                                                                                         121
                                                                                                                  PPAM
                                                                                                                  PPAM
         AMPINI
                                                                                                                  PPAM 124
                                                                                                                  PPAN
                            OMMODIN) AND PHASE VELOCITY VPMODIA).
= A SCALING FACTOP DEPENDENT ON HEIGHT OF BURST, EQUAL
0000000000000000
                                                                                                                 PPAM 126
         AL AM
                                                                                                                         127
                             TO CUBE ROOT OF (PRESSUPE AT GROUND)/(PRESSURE AT BURST HEIGHT) TIMES (SCUND SPEED AT GROUND)/SOUND SPEED AT BURST HEIGHT).
                                                                                                                  PPAÑ
                                                                                                                  PPAN 129
                                                                                                                  PPAM
                                                                                                                        130
          FACT
                             -A GENERAL AMPLITUDE FACTOR DEPENDENT ON BURST HEIGHT
                                                                                                                  ррд ч
                             AND OBSERVER HEIGHT. A PRECISE DEFINITION IS GIVEN IN THE LISTING 'F SUBROUTINE PAMPLE.
                                                                                                                  PPAM
                                                                                                                  PPAM
                                                                                                                         133
                              ----OUTPUTS----
                                                                                                                  PPAM
                                                                                                                  PPAM
                                                                                                                         136
                                                                                                                                 PRITGRAM
          AMPLTC(N)
                            =AMPLITUDE FACTOR REPRESENTING TOTAL MAGNITUDE OF
                                                                                                                                    ордир
                             FOURTER TRANSPORM OF THE CONTRIBUTION TO THE WAVEFORM OF A SINGLE GUIDED MODE AT EREQUENCY DAMOD(N). IT
                                                                                                                  PPAM
                                                                                                                  PPAM
                                                                                                                         139
                                                                                                                                      PAGE
                              REPRESENTS THE AMPLITUDE OF THE NMODE-TH MODE IF N IS
                                                                                                                                        65
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PRIMERY KST(NEGDE), AND RELATINGUED, INCLUSIVE. THE PRECISE DEFINITION IS GIVEN IN THE ABSTRACT.

PRESE LAG. AT FREQUENCY OMMONING EOP MYDDE-THE MODE WHE IS BETWEEN KST(NMODE) WAND REINGHOUDD). INCLUSIVE, THE STYTEGRAMD IS UNDERSTOOD TO HAVE THE FORM APPLYD*COS COMMODE CRIME-DISTANCE/VUMPOD*PHASOI.
                                                                                                                                                PPAM 141
FPAM 142
PPAM 143
50000
            PHATOINE
                                                                                                                                                 PPAM 144
PPAM 145,
PPAM 146
0,000,00
                                                                                                                                                 PPAM 147
                                                                                                                                                 PPAM-148
                                      ####PROGRAM FOULOWS BELOWHER
                                                                                                                                                 PPAH
          SUBROUTINE PÁNYŘÍ Ý TELO, MOENO, KST., KÉ ÌN, GMÝNO, , VPMČO, ĄMŘ, A LAM, FĄČT, PÁNPLTO; PHÁSOÍ
                                                                                                                                                  PPAN 150
                                                                                                                                                 PPAM 151
PPAM 152
 Ğ DIMENSION STATEMENTS USING VARIABLE DIMENSIONING
DIMENSION KST(4), KEIG(1), CMM(D(1), VPM(D(1), AMP(1))
DIMENSION AMPLID(1), PHASO(1)
                                                                                                                                                 PPAÑ 154
                                                                                                                                                  PPAM-155
٠C.
                                                                                                                                                  PPAM 157
             Q=(Y.TEUD) +=(0.-333333)
-ALAMP=G=ALAM
                                                                                                                                                  PPAM 158
                                                                                                                                                  PPAM' 159
 PPAN 161
                                                                                                                                                  PPAM 162
                                                                                                                                                  PPAM-163
              KZ=KFIN(11)
                                                                                                                                                  PPAM 164
                                                                                                                                                  PPA 165.
OC 27 J#K1.K2

C-CCMPUTATION OF SCAUED TREQUENCY UMERATE
("MERAT" CMMODIJ) #AL'AMP

C CCMPUTATION OF SORTIKE)

AKAY=SORTIONMODIJ)/PMODIJE)
                                                                                                                                                  PPAM 166
                                                                                                                                                  PPAM 167
                                                                                                                                                  PPAM 168
PPAM 169
 ď.
        (ALL 'SOUPCE(PMERÁT, FTMÁG, FTPHSE (DMAG, DPHSE)'
APPLTO(1) = (DFMZ) FFACT *FTMAG*AMP'(Y) *AKAY/OMMOD(Y)
20 PHASO(1) = 7573.14159-FTPHSE
                                                                                                                                                  PPAM -171
                                                                                                                                                  PPAM 172
                                                                                                                                                  PRAM 173
                                                                                                                                                  PPAM 174
 IC FRO OF DI LOPP
                                                                                                                                                  PPAN 1.75
                                                                                                                                                  PPAM 176
              RETHRN
              END
```

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> ₽ AG= 65

```
c
C
       PŘÁTÁD (SUBROÚŤINE)
                                                      -8/1/63
                                                                                                  PŘŤŘ
                                                                                                  PRTM.
                          ---- ARSTRACT----
                                                                                                  PPTM
·C
                                                                                                  PRITH
C TITLE - PRATMO
                                                                                                 PPTM
PPTM
            - PPOGRAM: TOUME INT. OUT PARAMETERS DEFINING THE MODEL MULITLAYER
- ATMOSPHERE. A LISTING IS PRINTEDION DAYER NUMBER, - HEIGHT OF
LAYER BOTTOM, HEIGHT OF LAYER TOP, LAYER THICKNESS, SCUND SPEED:
                                                                                                 PRTM-
                                                                                                 PPTM
            AND OF X AND Y COMPONENTS OF WIND VELUGITY.
                                                                                                  DRTM.
                 - FARTRAN IV (1360) REFERENCE MANUAL CZÁ-6515-4);
                                                                                                  PRTM
G LANGUAGE
 C AUTHORS
                 - A.D.P.TERCE AND J.POSEY; M.I.T., AUGUSTA1968
                                                                                                  ∢pp T#
                                                                                                  PPTM
                                                                                                  PF.TM
                          ----CALLING SEQUENCE----
                                                                                                  PRTM
                                                                                                  PR TM
   SEE THE MAIN PROGRAM
        OTHERS TOUS CT (190) , VXTT 100) , VYTT 190) ; HTT (190)
CCMMON TMAX , CT , VX I, VY I , HT - (THESE MUST RE IN COMMON)
CALU PRATM):
                                                                                                  PR TM
                                                                                                  PRTM
                                                                                                         20
                                                                                                 PŘT M
                          +---EXTERNÁIC SUBROUT ÎNES REQUIRED----
                                                                                                  PŘŢŃ
                                                                                                  PPT 4
   NO FETERNAL, SURROUTINES ARE REQUIRED.
                                                                                                  PR TH
                                                                                                  PRTM
PPTM
                          ---- ARGIMENT LIST ----
                                                                                                         26
27
· C:
                                                                                                  PRTM
 C' CCMMON STORAGE USED
                                                                                                  PFTM
                                                                                                  PHTM.
: 0-
        COMMON THUX CT AX 1 AX 1 HIS
                                                                                                          29
                                                                                                         30
C.
         XAPI
                                                                                                  PRTM
                                        INP
INP
                                                                                                         32
33
C
        CI
                       274.
                                100
                                                                                                 PPTM.
        VXI.
                                                                                                  PRTM
                       R 14
                                100
                       Rr 4
                                 100
                                                                                                  PRTM
C.
        41
                       R +4
                                100
                                        INP
                                                                                                  PRTM
                                                                                                  PFTM
                                                                                                          36
                          ---- INPUTS----
                                                                                                  PRTM
                                                                                                  PRIM
                        *NUMBER OF LAYERS OF FINITE THICKNESS
                                                                                                  PRTM
        :IMAX
.C.
                        **THICKNESS IN KM OF I-THICKNESS IN KM OF I-THICKNESS.
        CILLI
        (1) 1×v.
                                                                                                  PRIM
                                                                                                  PRTM
        441(1)
                                                                                                  FRTM
                                                                                                  PRIM
                          ---- jurpurs----
                                                                                                  PRIM
                                                                                                         45
  THE CNLY OUTPUT IS A PRINTOUT;
                                                                                                  PRIM
                                                                                                  PPTM
                                                                                                         48
                          ----CX AMPL C----
                                                                                                  PETM
                                                                                                         50
                     MODEL ATMOSPHERE OF 10 LAYERS
                                                                 (TOP OF NEW PAGE)
                                                                                                  PRTM
                                                                 (IMAX = 91
                                                                                                  PRTM
                                                                                                  PPTM-
                                                                                                          53
    LAYER
                     24
                     22.57
                                INFINITE
                                                INFINITE
                                                                  0.2972
                                                                                 0.0082
                                                                                                  PHTM
        10
                                                     2.50
                                                                  0.2958
0.2938
                     20.00
                                    22.50
                                                                                 0.0093
                                                                                                 PRTM
PRTM
                                                                                                          56
                                                                                 C.G118
                                                                                                         57
          8
7
                     15.00
                                    17.50
                                                     2.50
                                                                  0.2531
                                                                                 C. 0144
                                                                  0.2931
                     12.50
                                                                                0.0165
                                                                                                 PPTM
PPTM
                                    15.00
                                                     2.50
                                                                                                          50
                     10.00
7.50
                                                     2.50
2.50
                                    12.50
                                                                                                         60
                                                                  0.3012
                                                                                 0.0144
                                    10.00
                                                     2.50
                      5.97
                                     7.50
                                                                  0.3117
                                                                                 0.0116
                                                                                                  PRIM
                                                                                                  PRTM
                      2.57
                                                                  C. 326F
                                     5.00
                                                                                 C.OCRE
                                                                                                         63
                                                                                 0.0057
                                                                                                 PR T₩
PT 99
                                                                                                         65
                      ZBEHEIGHT HE LAYER BUTTOM IN KM
                                                                                                         66
                                                                                                               DRUCHVA
                      ZT=HEIGHT OF LAYER TOP
                                                   IN KM
                                                                       (THE VY COLUMN IS
                                                                                                  PRTM
                                                                                                                PRATMO
                      H -WIDTH OF LAYER IN KM
C = SCUND SPEED IN KM/SPC
                                                                         NOT SHOWN RECAUSE
OF LACK OF SPACE.
IT DOES APPEAR ON
                                                                                                  PF TM
                                                                                                  PPTM
                                                                                                                   PAGE
                      VX=X CAMP. AF WIND VEL. IN KM/SEC
                                                                                                                     57
```

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365 Pars 1, 5

A CONTRACTOR OF THE PROPERTY O

Committee to the second

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ŧς
                       VÝ=Y COMP. OF WEND-VEL. HN-KMASEC
                                                                              PRINTOUT ...
₹Ċ
                                                                                                         PR TH.
C
                           ++-#PRÓGRAM/FÜLLOŴS/ÁELÒW-#--
                                                                                                         PRTM
C
        "SUBROUTINE PRATHO.
                                                                                                        PRIM.
 C DIMENSTON AND COMMON STATEMENTS LOCATING INPUT
        *DIMENSTON CI(100), VXI(100), VVI(100); HI(100), LI(100)
COMMON IMAX; CI, VXI; VVI, HI
                                                                                                         PRTY
                                                                                                         PRTM
IC LET JET DENOTE THE INDEX OF THE UPPER HALFSPACE
                                                                                                         PRTM
         JET = I MAX+1
                                                                                                         PR TH
C PRINTING OF HEADING,
MRITE (6.11) JET:
11 FORMAT (-141, 16x, 194MODEL ATMOSPHERE CF., 14.7H LAYERS//)
                                                                                                         PRTM
                                                                                                         PPTM
                                                                                                         PRTM
     21 FORMAT(1H: +2X+5HLAYER+7X+2HZB+10X+2HZT+11X+1HH+11X+1HG+11X+2HVX+
                                                                                                         PRTH
        110x; 2HVY)
                                                                                                         PRTM
٠Ç
         IFCIMAX .EQ. 01 GO TO 33
                                                                                                         PRTM
                                                                                                         PRTM
C ZILLI DENOTES THE HEIGHT OF TOP OF LETH LAYER OF FINITE THICKNESS
                                                                                                         PRTM
         Z1(1) = H1(1)
                                                                                                         PRTM
     IF(IMAX .EÚ...1). GO TO 31
DO 30 I=2. IMAX
30 ZI(II=21(I=1)+HI(I)
                                                                                                         PRTM
                                                                                                                  95
                                                                                                         PRTM
                                                                                                                 96
                                                                                                         PRITM
    315 CONTINUE
                                                                                                         PRTM
                                                                                                         PRTM
C. PRINTOUT FOR UPPER HALFSPACE
                                                                                                         PRTM
                                                                                                                100
         XUV=ZILIMAX),
                                                                                                         PP TM
     33 IF (IMAX, . EQ. 0) XUV=0.0
                                                                                                         PRTM
         C=CI(JET)
                                                                                                         PRTM
                                                                                                                103
     VŶ¥ŶŶĬĊŨĔŤĬ
₩ŘĬŦĔ (6,61); JET, XUV, Č, VX, VY
$1°FORMĄŤ(ŢĤŤĨŢĴFĨŽŶŽŶ4X,ŘĤĬŇŔĬŇĨŤĔ,¥X,ŘĤINFĬŇĨŤĔ,ĴŔŢŽ°4)
                                                                                                         PPTM
                                                                                                         PRTM
                                                                                                                106
                                                                                                         PRTM
                                                                                                                107
                                                                                                         PRTM
         ÎFLÎMÂX .EQ. 07 GO TO 60
TFLIMAX .EQ. 1) GO TO 52
                                                                                                         PRTM
                                                                                                                109
                                                                                                         PRTM.
                                                                                                                110
                                                                                                         PRT# 111
C TABUCATION FOR LAYERS 2 THROUGH HAX
                                                                                                         PR-TM=112
         DO 50' J=2.1MAX
                                                                                                         PRTM
         1=1MAX+2-J
     IL=I-1
50 WRITE (6,51) I.ZI(IL),ZI(I),HI(I),CI(I),VXI(I),VYI(I)
51 FORMAT(IH ,17,3F12.2,3F12.4)
                                                                                                         PR TM
                                                                                                         PPTM
                                                                                                         PPTM
                                                                                                         PRŢM
G TABULATION FOR LAYER 1
                                                                                                         PPTM
                                                                                                         PR TM
         USTED=0.0
         WRITE (6,51) -[,USTED,Z[(1],H[(1],C[(1),VX[(]),VY[(])
                                                                                                         PRIM
C PRINTOUT OF EXPLANATIONS
                                                                                                         PRTM-
    PRINTOD OF EXPLANATIONS

60 WRITE (6.61)

61 FORMAT(140.15x.314ZH=HEIGHT OF LAYER HOTTOM IN KM/ 1H +15x.28HZT=H
1EIGHT OF LAYER TOP IN KM/IH +15x.23HH =WIDTH OF LAYER IN KM/IH +
215x.24HC =SCUND SPFED IN KM/SEC/IH +15x.33HVx=x COMP. OF WIND VEL.
3 IN KM/SEC/IH +15x.33HVY=Y COMP. OF WIND VEL. IN KM/SEC)
                                                                                                         PRIM
                                                                                                         PRTM
                                                                                                         PRTM
                                                                                                         PPTM
                                                                                                                129
                                                                                                         PRTM
                                                                                                                130
         RETURN
         FND
                                                                                                         PPTM 132
```

PROGRAM PRATMO was about the state of the state of

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1

the second is a second

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RRRR
                                                       8/1/68
        TRRR (SUBROUTINE)
C
                                                                                                    ....
                                                                                                    PRRR
                          ----ARSTRACT----
                                                                                                    RRRR
            - RRRR
THIS SUBROUTINE COMPUTES A 2-BY-2 TRANSFER MATRIX WHICH CONNECT
SOLUTIONS OF THE RESIDUAL EQUATIONS AT THE ROTTOM OF THE UPPER
HALFSPACE TO SOLUTIONS AT THE GROUND BY THE RELATIONS
  TITLE
                                                                                                    RRRR
00000
                                                                                                    892R
                                                                                                    RRRR
                                                                                                    RRRR
                   PHIL(GROUND)= RPP(1,1)*PHIL(ZT(SMAX))+RPF(1,2)*PHI2(ZT(IMA
                                                                                                    0000
                                                                                                            10
                                                                                                    RRRR
C
                   PHI2(GROUND)= RPP(2.1)*PHI1(ZT(IMAX))+RPP(2.2)*PHI2(ZT(IMA
                                                                                                    RRRR
0000
                                                                                                    RRRR
            WHERE ZT(IMAX) IS THE HEIGHT OF THE TOP OF THE IMAX LAYER AND CONSEQUENTLY THE HEIGHT OF THE BOTTOM OF THE UPPER HALFSPACE. THE FUNTIONS PHIL(Z) AND PHIL(Z) SATISFY THE RESIDUAL EQUATIONS
                                                                                                    RRPR
                                                                                                            15
16
                                                                                                    RRRR
RRRR
                                                                                                     RRRR
                                                                                                            18
19
                                                                                                    808D
                   D(PHI1)/OZ = A(1.1)*PHI1(Z) + A(1.2)*PHI2(Z)
                                                                                                    RRRR
 00000000
                                                                                                     RRRR
                                                                                                             ZO
                   D(PHI2)/DZ = A(2.1)*PHI1(Z) + A(2.2)*PHI2(Z)
                                                                                                     ....
                                                                                                             21
             WHERE THE ALL +JE ARE FUNCTIONS OF ALTITUDE BUT CONSTANT IN EACH
                                                                                                     RPRR
                                                                                                     RRRR
                                                                                                             23
                                                                                                     RRRR
             IF WE LET EM(I) BE THE EM MATRIX (COMPUTED BY SUBROUTINE MMMM) FOR THE I-TH LAYER. THEN (IN MATRIX NOTATION)
                                                                                                     RRRP
                                                                                                     RRRR
                                                                                                             26
                                                                                                     RRRR
                                                                                                     RRRR
                 RPP = EM(1)=EM(2)=....+EM(IMAX-1)=EM(IMAX)
                                                                                                             29
30
                                                                                                     RORR
                                                                                                     RRPR
             THE AROYE FORMULA IS USED TO COMPUTE THE RPP(I.J).
                                                                                                     RRRR
RARR
RBRR
             THE PARAMETERS DEFINING THE MULTILAYER ATMOSPHERE ARE PRESUNED
                                                                                                             33
             TO BE STORED IN COMMON.
                                                                                                             34
35
                                                                                                     RRRR
                                                                                                     RRRR
                   - FORTRAN IV (360, REFERENCE MANUAL C28-6515-4)
 C LANGUAGE
                                                                                                     RRRR
                                                                                                     RERR
                   - A. D. PIERCE. M. I.T. . AUGUST. 1968
 C AUTHOR
                                                                                                     RRRR
                                                                                                     RREK
                                                                                                             39
                           ----CALLING SEQUENCE----
                                                                                                     RRRR
                                                                                                     RPRR
RRRR
    SEE SUBROUTINE NADEN
DIMENSION CI(100).VXI(100).VYI(100).HI(100)
OTHERS OF THE CI-VXI.VYI.HI (THESE MUST BE STORED IN COMMON
                                                                                                      RRRR
                                                                                                     RRRR
RRRR
          DIMENSION RPP(2+2)
          CALL RERE (OMEGA, AKX, AKY, RPP.K)
                                                                                                      RRRR
                                                                                                      RRRR
                           ---- EXTERNAL SURROUTINES REQUIRED----
                                                                                                      RRRR
                                                                                                      RRRR
RRRR
          MMMM. AAAA. CAT. SAT
                                                                                                      RRRR
                            ---- ARGUMENT LIST---
                                                                                                      RRRR
                                                                                                              52
  CCCC
                                                                                                      RRRR
                         K#4
                                   ND
                                           INP
          OMEGA
                                                                                                              54
55
                                                                                                      RRRR
                                           INP
                         R+4
                                   ND
                                                                                                      RRRP
                         ...
                                   ND
                                           INP
          RPP
                                                                                                      RRRR
                                 2-8Y-2 OUT
                         R#4
                                                                                                      RRRR
RRRR
                                                                                                              57
                                           OUT
                                                  (ALWAYS OUTPUT AS K=0)
                                   ND
                          1+4
                                                                                                      RRRR
     COMMON STORAGE USED
                                                                                                      RRRR
                                                                                                              60
                                  I.VYI.HI
           COMMON THAX.CI.VX
                                                                                                      RRRR
                                                                                                       RRER
                                                                                                              62
                                   ND
           XAMI
                          144
                                                                                                       RRRR
                                                                                                              63
                          R#4
                                    160
                                            INP
           CI
VXI
                                                                                                       RRPR
                                           INP
                                   100
                          2*4
                                                                                                       RRRR
                                                                                                              65
                          R+4
                                    100
                                            INP
           VYI
                                                                                                       RRRR
                                                                                                                    PROGRAM
                          R44
                                    100
                                            INP
           HI
                                                                                                       9999
                                                                                                               67
                                                                                                                       RRRR
                                                                                                       RRRR
                                                                                                               68
                             ----INPUTS----
                                                                                                               69
70
                                                                                                       RRRR
                                                                                                                        PAGE
                                                                                                                           69
                                                                                                       RRRR
                           -ANGULAR FREQUENCY IN RADISEC
           OMEGA
```

```
=X COMPONENT OF HORIZONTAL WAVE NUMBER VECTOR IN 1/KM =Y COMPONENT OF HORIZONTAL WAVE NUMBER VECTOR IN 1/KM
        AK X
                                                                                          REER
Č
                                                                                          RRRR
                                                                                                 72
73
                      #WIMBER OF LAYERS OF FINITE THICKNESS
#SOUND SPEED IN KM/SEC IN I-TH LAYER
#X COMPONENT OF WIND VELOCITY IN I-TH LAYER (KM/SEC)
#Y COMPONENT OF WIND VELOCITY IN I-TH LAYER (KM/SEC)
        IMAX
                                                                                           RRRR
C
        CI(I)
                                                                                           RRRR
       VXICED
                                                                                           ....
                                                                                                 75
                                                                                           RRRR
                                                                                                 76
77
Ċ
                      STHICKNESS IN KM OF 1-TH LAYER OF FINITE THICKNESS
                                                                                           RRRR
                                                                                           RRRR
                       ----OUTPUTS----
C
                                                                                          RRER
                                                                                          RRRR
                                                                                                 80
       RPP
                      =7-BY-2 TRANSFER MATRIX WHICH CONNECTS SELUTIONS OF
                                                                                          RRRR
                      THE RESIDUAL EQUATIONS AT THE COTTOM OF THE UPPER MALFSPACE TO SOLUTIONS AT THE GROUND.
                                                                                          RRRR
C
                                                                                          RRRR
                                                                                          RRRR
                                                                                                  84
                                                                                          RRRR
                                                                                                 85
                       ----PROGRAM FOLLOWS BELOW----
                                                                                          RKRR
C
                                                                                          RRRR
       SUBROUTING RRRR (OMEGA. AKX. AKY. RPP. K)
                                                                                          RRRR
                                                                                                 88
                                                                                          RRRR
                                                                                                 89
  DIMENSION AND COMMON STATEMENTS LOCATING PARAMETERS DEFINING THE MODEL
                                                                                          RRRR
C MULTILAYER ATMOSPHERE
                                                                                          RRRR
       DIMENSION CI(100). YXI(100). YYI(100). HI(100)
                                                                                          RRRR
                                                                                                 92
       COMMON IMAX, CI, VXI, VYI, HE
                                                                                          RRRH
                                                                                                 93
£
                                                                                          RRRR
       DIMENSION EM(2.2).AINT(2.2).RPP(2.2)
                                                                                          RRRR
                                                                                          RRRR
                                                                                                 96
C RPP AT TOP OF IMAX LAYER IS THE IDENTITY MATRIX
                                                                                          RRER
                                                                                                 97
                                                                                          RRRR
                                                                                                 98
       RPP(1.1)=1.0
                                                                                          RRRR
       RPP(1.21=0.0
                                                                                          RRRR 100
       RPP(2-11=0.0.
                                                                                          RRRR 101
       RPP(2.2)=1.0
                                                                                          RRRR 102
                                                                                          RRRR 103
C START OF DO LOOP RUNNING THROUGH IMAX LAYERS IN DESCENDING ORDER
                                                                                          RRRR
       DO 100 JASA=1. IMAX
                                                                                          RRRR 105
       IASA=IMAX+1-JASA
                                                                                          RRRR 106
C IASA IS THE INDEX OF THE LAYER CURRENTLY UNDER CONSIDERATION
                                                                                          RRRR 107
                                                                                          RRRR 108
C COMPUTATION OF EM MATRIX FOR IASA LAYER
                                                                                          RRRR 109
       C=CITIASAI
                                                                                          RRRR 110
       VX=VX1(TASA)
                                                                                          RRRR 111
       VY=VYI(IASA)
                                                                                          RRRR
       H-HI ( IASA)
                                                                                          RRRR 113
       CALL MMMM(OMEGA, AKX, AKY, C. VX, VY, H, EM)
                                                                                          RRRR 114
                                                                                          RERR 115
C MULTIPLICATION OF RPP AT TOP OF IASA LAYER BY EM FOR IASA LAYER
                                                                                          RRRR 116
       00 80 1=1.2
00 80 J=1.2
                                                                                          RRRR 117
                                                                                          RRRR 118
   80 AINT([+J]=EM([+1]=RPP(1+J)+EM(1+2)*RPP(2+J)
                                                                                          RRRR 119
                                                                                                120
C CURRENT AINT- IS RPP AT BOTTOM OF IASA LAYER
                                                                                          RRRR
       DO 85 I=1.2
DO 85 J=1.2
                                                                                          RRRR 122
RRRR 123
   85 RPP(I.J)=AINT(I.J)
                                                                                          RRRR
                                                                                                124
                                                                                          RRRR
  100 CONTINUE
                                                                                          RRRR
                                                                                                126
C PHD OF OUTER DO LOOP
                                                                                          RRRR 127
                                                                                          RRRR 128
C CURRENT RPP IS THAT AT BOTTOM OF FIRST LAYER
                                                                                          RRRR 129
                                                                                          RRRR 130
RRRR 131
       RETURN
                                                                                                130
       FND
```

PROGRAM RRQR

```
7/25/68
                        SAT (FUNCTION)
                                                                                                                                                                                                                                                                                                     SAI
                                                                                                                                                                                                                                                                                                      SAI
                                                                           ----ABSTRACY----
                                                                                                                                                                                                                                                                                                     SAI
SAI
SAI
         TITLE - SAI
                                    PROGRAM TO EVALUATE FUNCTION SAI(K) FOR GIVEN VARIABLE X.

IF X IS NEGATIVE, SAI(X)=SIN(Y)/Y WITH Y=SORT(-X). IF X IS
POSITIVE, SAI(X)=SINH(Y)/Y WITH Y=SORT(X). THE FUNCTION IS
 CCC
                                                                                                                                                                                                                                                                                                     SAT
SAT
SAT
SAT
SAT
                                     ALSO REPRESENTABLE BY THE POWER SERIES
                                                                                                                                                                                                                                                                                                                        10
11
                                                    SAI(X)= 1 + X/(3FACT) + X==2/(SFACT) + X==3/(7FACT) + ...
                                                   - FORTRAM IV (360. REFERENCE MANUAL C28-6515-4)
                                                                                                                                                                                                                                                                                                                         13
                                                                                                                                                                                                                                                                                                                        14
                                                                                                                                                                                                                                                                                                     SAI
SAI
SAI
SAI
SAI
SAI
SAI
         AUTHOR
                                                    - A.D.PIFRCE, M.I.T., JULY,1968
 C
                                                                           ----CALLING SEQUENCE----
                                                                                                                                                                                                                                                                                                                         18
 CCC
                        SATIANY R#4 ARGUMENT) MAY BE USED IN ARITHMETIC EXPRESSIONS
                                                                                                                                                                                                                                                                                                                         20
21
                                                                           ---- EXTERNAL SUBROUTINES REQUIRED ----
 00000000
                                                                                                                                                                                                                                                                                                                         22
23
                                                                                                                                                                                                                                                                                                    SAITS 
                        NO EXTERNAL SUBROUTINES ARE REQUIRED
                                                                                                                                                                                                                                                                                                                        24
25
26
27
                                                                            ----ARGUMENT LIST----
                                                               R#4
                                                                                                                      OUT
                                                                                                                                                                                                                                                                                                                        Ž8
                                                                                                                                                                                                                                                                                                                        29
30
31
 C
        NO COMMON STORAGE IS USED
 CCC
                                                                           ---- PROGRAM FOLLOWS BELOW----
                                                                                                                                                                                                                                                                                                                        34
35
36
37
                        FUNCTION SAI(X)
 C
                1 IF( ABS(X) .GT. 1.E-15 ) GO TO 9
                                                                                                                                                                                                                                                                                                                        38
39
40
41
        ABSIX) IS SO SHALL THAT SAI IS VIRTUALLY 1.0
                        SAI=1.0
RETURN
C CONTINUING FROM 1
9 Y=SORT(ABS(X))
1F(X) 10.10.11
                                                                                                                                                                                                                                                                                                                        42
43
                                                                                                                                                                                                                                                                                                                        44
45
46
47
C x IS LESS THAN 0.
10 SAT-SIN(Y)/Y
RETURN
                                                                                                                                                                                                                                                                                                                        48
49
50
51
 C x is positive. SAI= SINH(Y)/Y.
             11 E=EXP(Y)
SAT=0.5+(E-1./E)/Y
                          RETURN
                                                                                                                                                                                                                                                                                                                        53
                          END
                                                                                                                                                                                                                                                                                                     SAT
```

PROGRAM SAT PAGE

```
SOURCE (SUBROUTINE)
                                                8/15/48
                                                                                      SRCE
SRCE
                                                                                       SRCE
                       ----ARSTRACT----
                                                                                      SRCE
                                                                                      SECE
  TITLE - SOURCE
                                                                                      SRCE
          EVALUATION OF FOURIER TRANSFORM OF NEAR FIELD ACOUSTIC RESPONSE
                                                                                      SRCE
                                                                                      SRCE
                                                                                      SRCF
                 SOURCE COMPUTES THE FOURTER TRANSFORM OF THE NEAR FIELD
                                                                                      SRCE
                                                                                             10
                 PRESSURE AT 1 KM FROM A 1 KT EXPLOSION AT SEA LEVEL. THE AMBIENT PRESSURE IS ASSUMED TO BE 1.66 DYNES/CM+02 AND THE TIME LAPSE FROM TIME ZERO IS NEGLECTED. AN EMPIRICAL
                                                                                      SRCE
                                                                                      SRCE
                                                                                      SRCE
                                                                                             13
                 FORMULA FOR THIS PRESSURE IS
                                                                                             14
15
                                                                                      SRCE
                                                                                      SRCE
                     F(T) = PAS = (1 - (T/TAS)) = EXPT -T/TAS ) . T .GT. 0
                                                                                      SRCE
                                                                                      SRCE
                                , T .LT. 0
                                                                                             16
                          = 0
                                                                                      SRCF
                                                                                      SRCE
                 WITH #AS = {34.45E+3} + (1.61) DYNES/CH++2
                                                                                      SRCE
                                                                                             20
                 AND TAS - 0.48 SEC .
                                                                                      SRCE
                                                                                      SRCE
                                                                                             22
                 THEREFORE, ITS FOURIER TRANSFORM IS
                                                                                      SRCE
                                                                                             23
24
                                                                                      SRCE
                     FT(OMEGA) = -1 + OMEGA + PAS / (1/TAS ~ I + OMEGA) ++2
                                                                                      SRCE
                                                                                      SRCE
                                                                                             26
                                                                                      SRCE
                 WHERE I = (-1)++0.5 .
                                                                                      SRCE
C LANGUAGE
              - FORTRAM IV (360, REFERENCE MANUAL C28-6515-4)
                                                                                      SRCE
                                                                                      SRCE
                                                                                             30
               - A.D.PIERCE AND J.POSEY, M.I.T., AUGUST, 1968
C AUTHORS
                                                                                             31
                                                                                      SACE
                                                                                      SRCE
                       ----USAGE----
                                                                                      SRCE
                                                                                            35
      SUBROUTINE PHASE IS CALLED
                                                                                      SRCE
                                                                                             36
                                                                                      SRCE
C FORTRAN USAGE
                                                                                      SRCE
                                                                                             38
                                                                                      SRCE
                                                                                             39
                                                                                      SRCE
                                                                                             40
      CALL SOURCE (OMEGA.FTMAG.FTPHSE.DMAG.DPHSE)
                                                                                      SRCE
C INPUTS
                                                                                      SRCE
                                                                                      SRCE
                                                                                             43
      OMEGA
                 ANGULAR FREQUENCT (RADIANS/SEC)
                                                                                      SRCE
                                                                                             44
45
        R#4
                                                                                      SRCE
                                                                                      SRCE
                                                                                      SRCE
C DUTPUTS
                                                                                      SRCE
                 MAGNITUDE OF FT(OMEGA) DEFINED ABOVE IN SUBROUTINE ABSTRA
                                                                                      SRCE
      FTMAG
                 ( (DYNES/CH##2) / (RAD/SEC) )
                                                                                      SRCE
                                                                                             50
                                                                                      SECE
                                                                                      SRCE
     FTPHSE
                 PHASE OF FTIOMEGAL DEFINED ABOVE IN SUBROUTINE ABSTRACT
                                                                                      SRCE
       R#4
                 (RADIANS)
                                                                                      SRCE
                 DERIVATIVE OF FINAG WITH RESPECT TO ONEGA ( (DYNES/CH+2)
      DMAG
                                                                                      SRCE
                                                                                             55
                 / (RAD/SEC)++2 )
                                                                                      SRCE
       R#4
                                                                                             56
                                                                                      SRCE
      DPHSE
                 DERIVATIVE OF FYPHSE WITH RESPECT TO OMEGA (RAD / IRAD/
                                                                                      SRCE
        R#4
                 SEC) )
                                                                                      SRCE
                                                                                            60
                                                                                      SRCE
                       ----PROGRAM FOLLOWS BELOW----
                                                                                      SRCE
                                                                                      SRCE
SRCE
                                                                                            64
                                                                                      SRCE
                                                                                            65
       SUBROUTINE SOURCE(OMEGA.FTMAG.FTPHSE.DMAG.DPHSE)
                                                                                      SRCE
SRCE
                                                                                            66
       HE ASSUME INVERSE R DEPENDENCE
                                                                                                 PROGRAM
PAS=(34-45E+3/1-01+(1-61)
C PAS IS IN DYNES/CM++2
C THIS IS THE PEAK CYERPRESSURE AT 1 KM
                                                                                                  SOURCE
                                                                                      SRCE
                                                                                            68
                                                                                      SRCE
                                                                                                     PAGE
       TAS=0.48
```

_	TAS IS THE LENGTH OF THE POSITIVE PHASE	SRCE	71
l.		SRCE	72
	OMO=1.0/TAS	SACE	73
	nenda=daegaeae+dacaees		
	FTHAG=PASOOMEGA/DENOM	SRCE	74
	DHAG=PAS/DENOM-2.0+PAS+OMEGA++2/DENOH++2	SRCE	75
	Under 37 Sender - Secretary Control	SACE	76
	CALL PHASELONG. GREGA. X. PHI)	SRCE	77
r	PHI IS THE ARCTAN OF OMEGA/OMO		
••	FTPHSF=-3.1415927/2.0+2.0+PHI	SRCE	78
	DPHSE=2.0*OMO/DENGM	SRCE	79
	UPHSE=2.0 - UPHSH	SRCE	80
C	THE DERIVATIVE OF THE ARCTAN IS 1./(1.+Y**2)		
	RETURN	SRCE	81
	END	SRCE	82
	ENU		

PROGRAM SOURCE

> 78. 73

```
SUSPET (SUBROUTINE)
                                                                    7/19/68
                                                                                                                           SPCT
                                                                                                                            SPCT
                                 ----ARSTRACT---
                                                                                                                            SPCT
                                                                                                                           SPCT
  TITLE - SUSPCT
                                                                                                                            SPCT
              EVALUATION OF SUSPICION INDEX OF ELEMENT (N.M.) OF MATRIX INMODE
                                                                                                                            SPCT
                        SUSPCT EVALUATES THE SUSPICION INDEX, ISUS, OF THE ELEMEN IN ROW N. COLUMN M OF THE MATRIX INMODE ( (N.M) MUST BE AN INTERIOR ELEMENT). THE NEIGHBORS OF (N.M) ARE DEFINED TO BE THE EIGHT ELEMENTS WHICH FORM THE THREE BY THREE ELEMENT SQUARE WHICH HAS (N.M) AT ITS CENTER. THEY ARE NUMBERED FROM ONE TO HINE BEGINNING IN THE UPPER LEFT AND PROCEEDING CLOCKWISE (NO. 1 AND NO. 9 ARE SAME ELEMENT). EACH ELEMENT OF MATRIX INMODE MUST HAVE ONE OF THREE VALUES, -1. 1, OR 5. (N.M) IS NOT SUSPICIOUS AND ISUS = O IF ANY ONE OF THE FOLLOWING CONDITIONS HOLDS.
C.
                                                                                                                           SPCT
                                                                                                                           SPCT
                                                                                                                           SPCT
                                                                                                                                     10
                                                                                                                           SPCT
                                                                                                                           SPCT
                                                                                                                           SPCT
                                                                                                                                     13
                                                                                                                           SPCT
                                                                                                                            SPCT
                                                                                                                           SPCT
                                                                                                                           SPCT
                                                                                                                                     17
                                                                                                                           SPCT
                                       ELEMENT (W.M) = 5
ANY OF ITS NEIGHBORS = 5
NOWHERE IN THE 3X3 ARRAY OF (N.M) AND ITS NEIGH-
BORS DOES THERE APPEAR TO BE A DISPERSION CURVE
                                                                                                                           SPČT
                                                                                                                           SPCT
                                                                                                                           SPCT
                                        WITH POSITIVE SLOPE
                                                                                                                            SPCT
                                                                                                                           SPCT
SPCT
                                                                                                                                     25
                        OTHERWISE ISUS IS SET EQUAL TO THE NUMBER OF THE QUADRANT IN WHICH THE POSITIVE SLOPE APPEARS. THE QUADRANTS ARE NUMBERED BEGINNING IN THE UPPER LEFT AND PROCEDING CLOCK-
                                                                                                                                     26
27
                                                                                                                           SPCT
                                                                                                                           SPCT
                                                                                                                           SPCT
SPCT
SPCT
                         WI SE.
                                                                                                                                     30
                    - FORTRAM IV (360, REFERENCE MANUAL C28-6515-4)
  LANGUAGE
                                                                                                                           SPCT
                                                                                                                           SPCT
  AUTHORS
                     - A.C.PIERCE AND J.POSEY, M.I.T.. JUNE.1968
                                                                                                                           SPCT
SPCT
                                                                                                                                     34
35
                                 ----USAGE----
                                                                                                                           SPCT
SPCT
SPCT
SPCT
         NC FORTRAN SUBROUTINES ARE CALLED
                                                                                                                                     38
   FORTRAN USAGE
          CALL SUSPCTIN, M. NROW, INHONE, ISUS)
                                                                                                                           SPCT
                                                                                                                           SPCT
C INPUTS
C
                         ROW NUMBER OF ELEMENT UNDER CONSIDERATION (MAY NOT BE
                                                                                                                           SPCT
           1+4
                         FIRST OR LAST ROW!
                                                                                                                           SPCT
                                                                                                                           SPCT
                         COLUMN NUMBER OF ELEMENT UNDER CONSIDERATON (MAY NOT BE
                                                                                                                           SPCT
C
                         FIRST OR LAST COLUMN)
                                                                                                                           SPC T
                                                                                                                                     48
                                                                                                                           SPCT
        NROW
                         TOTAL NUMBER OF ROWS IN INMODE
                                                                                                                                     50
                                                                                                                           SPCT
           1+4
                                                                                                                           SPCT
        INMODE
                         MATRIX UNDER CONSIDERATION STORED IN VECTOR FORM, COLUMN
                                                                                                                           SPCT
           1+4(0)
                        AFTER COLUMN. EACH ELEMENT MUST BE -1. 1. OR 5.
                                                                                                                           SPCT
                                                                                                                           SPC T
                                                                                                                                     55
   OUTPUTS
                                                                                                                                     56
                                                                                                                           SPCT
                         SUSPICION INDEX OF ELEMENT (N.M). SEE ABSTRACT ABOVE FOR
                                                                                                                           SPCT
SPCT
        1 SUS
                                                                                                                                     58
           144
                        DEFINITION.
                                                                                                                                     59
                                                                                                                           SPCT
                                                                                                                           SPCT
                                                                                                                                     61
                                                                                                                           SPCT
SPCT
                                ---EXAMPLES----
                                                                                                                                     63
   CALLING PROGRAM
                                                                                                                           SPCT
                                                                                                                                     64
                                                                                                                           SPCT
SPCT
                                                                                                                                    65
          DIMENSION INMODE(9)
                                                                                                                                    66
                                                                                                                                           PROGRAM
         INMIDE = -1. -1. 1. 1. -1. 1. 1. -1 CALL SUSPETION.2, 3, INMODE, ISUS)
                                                                                                                           SPCT
                                                                                                                                             SUSPCT
                                                                                                                           SPC T
                                                                                                                                    68
C WRITE (6,200) ISUS
C 200 FORMAT (10M EXAMPLE 1,6x, 6HISUS =,12)
                                                                                                                                                PAGE
```

```
INMODE = -1. -1. 1. 1. -1. -1. 1. 1. 1
CALL SUSPCT(2.2.3.INMODE.ISUS)
WRITE (6.300) ISUS
                                                                                                              SPCT
                                                                                                              SPCT
                                                                                                              SPCT
  300 FORMAT (10H EXAMPLE 2.6X. 6HISUS =,12)
                                                                                                              SPCT
         END
                                                                                                              SPCT
                                                                                                             SPCT
SPCT
C TABLES OF INMODE
                                                                                                              SPCT
                                                                                                             SPCT
SPCT
               EXAMPLE 1
                                     EXAMPLE ?
                                                                                                                      80
                                                                                                             SPCT
SPCT
               -++
                                                                                                                      81
               --+
                                                                                                              SPCT
                                                                                                             SPCT
C PRINTOUT
                                                                                                                      85
                                                                                                             SPCT
C
                                                                                                                      86
                                                                                                              SPCT
         EXAMPLE 1
                               ISUS = 3
                                                                                                                      87
                              1 SUS = 0
         EXAMPLE 2
                                                                                                              SPCT
                                                                                                              SPCT
                                                                                                              SPCT
                                                                                                                      90
                             ----PROGRAM FOLLOWS BFLOW----
                                                                                                             SPCT
                                                                                                             SPCT
                                                                                                              SPCT
ť.
         SUBROUTINE SUSPCTIN-M-NROW-INMODE-ISUS)
                                                                                                              SPCT
                                                                                                             SPCT
SPCT
                                                                                                                      95
C VARIABLE DIMENSIONING OF INMODE DIMENSION (PP(9). (QUANGA). (NMODE(1)
                                                                                                                      96
                                                                                                              SPCT
                                                                                                              SPCT
                                                                                                                      98
C ELEMENT (N.M) OF INMODE IS ICEN
ICEN= INMODE((M-1)*NROW+N)
ISUS= 0
                                                                                                             SPCT 99
SPCT 100
                                                                                                              SPCT 101
                                                                                                              SPCT 102
C IF ICEN IS 5. IT IS NOT SUSPICIOUS AND ISUS = 0
IFICEN .FO. 5) WETURN
                                                                                                              SPCT 103
                                                                                                              SPCT 104
                                                                                                             SPCT 105
SPCT 106
C [PP(N) IS NEIGHBOR NO. N (SEE ARSTRACT ABOVE FOR NUMBERING SCHEME)
[PP(1)= INMODE((M-2)*NROW*(N-1))
[PP(2)= INMODE((M-1)*NROW*(N-1))
                                                                                                              SPCT 107
                                                                                                              SPCT 108
         IPP(3)= INMODE((M-0)*NROW*(M-1))
IPP(4)= INHODE((M-0)*NROW*(M-0))
IPP(5)= INHODE((M-0)*NROW*(N+1))
                                                                                                             SPCT 109
SPCT 111
                                                                                                              SPCT 11.
         IPP(6)= INHODE((M-1)*NROW+(N+1))
                                                                                                              SPCT 112
         IPP(7)= INMODE((M-2)*NROW+(N+1))
IPP(8)= INMODE((M-2)*NROW+(N+0))
                                                                                                              SPCT 113
                                                                                                             SPCT 114
         IPP(9)= 1PP(1)
                                                                                                              SPCT 115
         NX = 0
DO 10 1=1+8
                                                                                                              SPCT 116
                                                                                                              SPCT 117
         IF(IPP(I) .EO. 5) NX=NX+1
                                                                                                              SPCT 118
    10 CONTINUE
                                                                                                             SPCT 119
C NX IS THE NUMBER OF NEIGHBORS WHICH EQUAL +5
                                                                                                              SPCT 120
                                                                                                              SPCT 121
C IF MORE THAN THE NEIGHBOR IS EQUAL TO +5. THEN ISUS=0
                                                                                                              SPCT 122
         IF (NX .GY. 1) RETURN
                                                                                                              SPCT 123
                                                                                                             SPCT 124
SPCT 125
C IF NFIGHBOR 3 IS THE ONLY ONE FOUAL TO +5 AND FITHER NEIGHBOR 2 OR C NEIGHBOR 4 DOES NOT AGREE WITH ICEN. THEN ISUS=2

ISUM = IABS( ICEN + IPP(2) + IPP(4))
                                                                                                              SPCT 126
                                                                                                              SPCT 127
         IF (IPP(3).EQ.5 .AND. ISUM.NE.3) ISUS=2
IF (NX.GT.0) RETURN
                                                                                                              SPCT 128
                                                                                                             SPCT 129
SPCT 130
SPCT 131
IF (NX.GT.O) RETURN

30 DD 50 1=1.9

50 IPP(I)=(IABS(IPP(I)+ICEN))/2

C IPP(I) IS 1 IF NFIGHBOR I AGREES WITH ICEN. IT IS 0 IF THEY DISAGREE

C (TO REACH THIS POINT. NEITHER ICEN NOR ANY DF ITS NEIGHBORS COULD BE 5
                                                                                                              SPCT 132
                                                                                                             SPCT 133
SPCT 134
                                                                                                             SPCT 135
         IF( IPP(1) .EQ. C .AND. IPP(2) .EQ. 1 .AND. IPP(8) .EQ. 1)
                                                                                                              SPCT 136
                                                                                                                            PROGRAM
          RETURN
                                                                                                              SPCT 137
                                                                                                                              SUSPCT
         IF( IPP(8) .EQ. O .AND. IPP(2) .EQ. O) RETURN
                                                                                                             SPCT 138
         ISUS = ?
                                                                                                                                 PAGE
                                                                                                              SPCT 139
         IF ( IPP(2) .EQ. O .AND. IPP(3) .EQ. 1) RETURN
                                                                                                             SPCT 140
```

```
IF( IPP(3) .EQ. 1 .AND. IPP(4) .EQ. 0) RETURN

ISUS = 3

IF( IPP(5) .EQ. 0 .AND. IPP(4) .EQ. 1 .AND. IPP(6) .EQ. 1)

RETURN

IF( IPP(4) .EQ. 0 .AND. IPP(6) .EQ. 0) RETURN

IF( IPP(4) .EQ. 0 .AND. IPP(6) .EQ. 0) RETURN

SPCT 144

SPCT 145

SPCT 146

SPCT 146

SPCT 147

IF( IPP(6) .EQ. 0 .AND. IPP(7) .EQ. 1) RETURN

SPCT 147

IF( IPP(7) .EQ. 1 .AND. IPP(8) .EQ. 0) RETURN

SPCT 148

SPCT 149

RETURN

ENO

SPCT 150
```

PROGRAM SUSPCT

```
TABLE (SUBROUT INF)
                                                             7/19/68
                                                                                                               748£
                                                                                                               TABL
                                                                                                               TARI
                      ----ABSTRACT----
                                                                                                               TABL
C TITLE - TABLE
                                                                                                               TABL
                                                                                                               TABL
             GENERATION OF SUSPICIONLESS TABLE OF NORMAL MODE DISPERSION
C,
                                                                                                               TABL
C
             FUNCTION SIGNS
                                                                                                               TARE
                                                                                                               TABL
                      TABLE CALLS SUBROUTINE HPOUT TO CONSTRUCT THE MATRIX OF
                                                                                                               TABL
                      NORMAL MODE DISPERSION FUNCTION SIGNS INNODE (STORED IN
VECTOR FORM COLUMN AFTER COLUMN) FOR REGION IN FREQUENCY-
                                                                                                               TABL
                                                                                                               TARE
ccc
                      PHASE VELOCITY PLANF (OMILE-OMEGA-LE-OM2-AND-VI-LE-VP-LE

-V21. SUBROUTINE SUSPCT IS CALLED TO EVALUATE THE SUSPI-
                                                                                                               TABL
                                                                                                               TABL
                      CION INDEX .ISUS, OF EACH INTERIOR ELEMENT IN THE MATRIX SCANNING FROM LEFT TO RIGHT, TOP TO BOTTOM. IF ISUS .NE. O , INMODE IS ALTERED AS FOLLOWS.
Č
                                                                                                               TABL
                                                                                                                        15
                                                                                                               TABL
0000
                                                                                                               TABL
                              ISUS=1 ROW ADDED ABOVE SUSPICIOUS ELEMENT AND COLUMN
                                                                                                               TABL
                                    ADDED TO ITS LEFT

=2 COLUMN ADDED TO RIGHT OF SUSPICIOUS ELEMENT
AND ROW ADDED ABOVE IT
                                                                                                               TABL
                                                                                                               TABL
                                                                                                                       20
                                                                                                               TABL
                                                                                                                       21
                                    =3 ROW ADDED BELOW SUSPICIOUS ELEMENT AND COLUMN
                                                                                                              TABL
С
С
                                        ADDED TO ITS RIGHT
                                                                                                               TABL
                                    *4 COLUMN ADDED TO LEFT OF SUSPICIOUS ELEMENT
                                                                                                               TABL
                      AND ROW ADDED TO LEFT OF SUSPICIOUS ELEMENT
AND ROW ADDED BELGW IT
HOWEVER, NEITHER THE NUMBER OF ROWS NVP NOR THE NUMBER OF
COLUMNS NOM WILL BE INCREASED BEYOND 100. IF ISUS CALLS
FOR AN ADDITIONAL ROW WHEN NVP = 100, THE MESSAGE
(NVP = 100 N = XX M = XX) WILL BE PRINTED.
N IS ROW NO. OF SUSPICIOUS ELEMENT. M IS COLUMN NO. IF
ISUS CALLS FOR ADDITION OF A COLUMN WHEN NOM = 100, THE
MESSAGE (NOM = 100 N = XX M = XX) IS PRINTE
MESSAGE (NOM = 100 STANDED SCAMPING IS DECIMED AT THE
Ċ
                                                                                                               TABL
                                                                                                                       25
                                                                                                              TABL
                                                                                                               TABL
C
                                                                                                               TABL
Č
                                                                                                               TABL
                                                                                                                       29
                                                                                                               TABL
                                                                                                                       30
C
                                                                                                               TABL
                                                                                                              TABL
                       WHEN INMODE HAS BEEN EXPANDED SCANNING IS RESUMED AT THE
                                                                                                               TABL
                      ELEMENT IN NEW MATRIX WITH SAME ROW AND COLUMN NOS. AS THOSE OF SUSPICIOUS ELEMENT IN OLD MATRIX. IF NOPT IS POSITIVE INMODE WILL BE PRINTED AS IT IS PETURNED FROM
                                                                                                               TABL
                                                                                                                       34
35
                                                                                                               TABL
                                                                                                               TABL
                       MPOUT AND IN ITS FINAL FORM.
                                                                                                               TABL
                                                                                                               TABL
                                                                                                                       38
                   - FORTRAN IV 1360. REFERENCE MANUAL - C28-6515-41
                                                                                                               TARL
C LANGUAGE
                                                                                                                       39
                                                                                                              TABL
                                                                                                                       40
C
                                                                                                               TABL
  AUTHOR
                   - J.W.POSEY. M.I.T.. JUNE.1968
                                                                                                               TABL
                                                                                                               TABL
                                                                                                                       43
                             ----USAGF----
                                                                                                              TABL
                                                                                                               TABL
         SUBPOUTINES MPOUT. SUSPCT. LINGTHN. WIDEN, NMOFN ARE CALLED IN TABLE.
                                                                                                               TABL
                                                                                                               TABL
   FORTRAN USAGE
                                                                                                               TABL
                                                                                                                       48
         CALL TABLE(OM1.OM2.V1.V2.NOM.NVP.THETK.OM.V.INMODE.NOPT)
                                                                                                               TABL
                                                                                                                       49
                                                                                                               TABL
                                                                                                                       50
C.
   INPUTS
                                                                                                               TABL
                                                                                                               TABL
                      MINIMUM VALUE OF ERFOLIENCY TO BE CONSIDERED.
C
       ONI
                                                                                                               TABL
                                                                                                                       53
                                                                                                               TABL
          2#4
CCC
                      MAXIMUM VALUE OF FREQUENY TO RE CONSIDERED
       OH2
                                                                                                               TABL
          R#4
                                                                                                               TABL
                      MINIMUM VALUE OF PHASE VELOCITY TO BE CONSIDERED
       V1
                                                                                                               TABL
                                                                                                                       57
č
          RP4
                                                                                                               TABL
                                                                                                                       58
       V2
                      MAXIMUM VALUE OF PHASE VELOCITY TO BE CONSICERED
                                                                                                               TABL
          P=4
                                                                                                               TABL
       MOM
                      INITIAL NO. OF FREQUENCIFS TO RF CONSIDERED
                                                                                                               TABL
          1 44
                                                                                                              TABL
                                                                                                               TABL
       NYP
                      INITIAL NO. OF PHASE VELOCITIES TO BE CONSIDERED
                                                                                                                       63
          1+4
                                                                                                               TABL
Ĉ
       THETK
                      PHASE VELOCITY DIRECTION (RADIANS)
                                                                                                               TABL
                                                                                                                       65
                                                                                                                       66
67
          R#4
                                                                                                              TABL
                                                                                                                             DROGRAM
c
c
       NOPT
                      PRINT OUT OPTION.
                                                 IF NOPT = -1. NO PRINT. IF NOPT = 1.
                                                                                                               TABL
                                                                                                                                TAPLE
          1*4
                       INMODE IS PRINTED IN ITS INITIAL FORM (GENERATED BY MPOUT
                                                                                                              TABL
                                                                                                                       68
                      AND IN ITS FINAL FORM.
                                                                                                               TABL
                                                                                                                                  PAGE
                                                                                                              TABL
```

C

```
C OUTPUTS
                                                                                             TABL
                                                                                                     72
73
                                                                                             TARL
                   TOTAL NO. OF FREQUENCIES CONSIDERED
      NOM
                                                                                              TABL
                                                                                              TABL
      NYP
                   TOTAL NO. OF PHASE VELOCITIES CONSIDERED
                                                                                              TABL
                                                                                                     75
         1+4
                                                                                                     76
77
                                                                                              TABL
      OM
                   VECTOR WHOSE FLEMENTS ARE THE VALUES OF ANGULAR FREQUENCY
                                                                                             TABL
         R#4(D)
                   CORRESPONDING TO THE COLUMNS OF THE INMODE MATRIX
                                                                                              TABL
                                                                                             TABL
                                                                                                     79
                   VECTOR WHOSE ELEMENTS ARE THE VALUES OF PHASE VELOCITY
                                                                                                     80
                                                                                              TABL
         R*4(D)
                   CORRESPONDING TO THE ROWS OF THE INMODE MATRIX
                                                                                              JEAT
                                                                                              TABL
      INMODE
                   EACH ELEMENT OF THIS MATRIX CORRESPONDS TO A POINT IN THE
                                                                                              TABL
                                                                                                     83
                  FREQUENCY (OM) - PHASE VELOCITY (V) PLANE. IF THE NORMAL MODE DISPERSION FUNCTION (FPP) IS POSITIVE AT THAT POINT. THE ELEMENT IS +1. IF FPP IS NEGATIVE. THE ELEMENT IS -1. IF FPP DOES NOT EXIST. THE ELEMENT IS 5. INMODE HAS NVP ROWS AND NOM COLUMNS. MATRIX IS STORED AS A VECTOR. COLUMN AFTER COLUMN.
         [+4(D)
                                                                                             TABL
                                                                                                     84
                                                                                              TABL
                                                                                             TABL
                                                                                                     87
                                                                                              TABL
                                                                                                     88
                                                                                              TABL
                                                                                              TABL
                                                                                                     90
                                                                                              TABL
                                                                                                     91
92
                         ----EXAMPLE----
                                                                                              TABL
  TABL
                                                                                                     95
                                                                                              TABL
                                                                                              TABL
                                                  THETK = 3.14159
                                                                                                     96
           V = 1.0, 2.0, 3.0, 4.0
                                                                                              TABL
C (VALUES NOT CORRECT, FOR ILLUSTRATION ONLY)
                                                                                              TABL
                                                                                                     98
C THEN THE TABLE WILL BE PRINTED AS FOLLOWS.
                                                                                              TABL
                                                                                                     99
                                                                                              TABL 100
                                                                                              TABL 101
                  NORMAL MODE DISPERSION FUNCTION SIGN
C VPHASE
                                                                                             TABL 102
   1.00000
                                                                                             TABL 103
¢
                -+++
                 X-++
                                                                                              TABL 104
    2.00000
    3.00000
                                                                                              TABL 105
    4.00000
                                                                                             TABL 106
                                                                                              TABL 107
         OMEGA 1234
                                                                                              TABL 108
                 PHASE VELOCITY DIRECTION IS
                                                      90.000DEGREES
                                                                                              TABL 109
                                                                                             TABL 110
  OMEGA =
                                                                                              TABL 111
      0.10000E 01
                        0.15000E 01
                                        0.20000E 01
                                                           0.25000F 01
                                                                                              TABL
                                                                                              TABL 113
                                                                                              TABL 114
                         ---- PROGRAM FULLOWS BELOW----
                                                                                              TABL 116
C
                                                                                             TABL 117
        SUBPOUTINF TABLE (OM1. OM2. VI. VZ. NOM. NYP. THETK. OM. V. INMODE, NOPT)
                                                                                              TABL 118
                                                                                              TABL 119
C
        DIMENSION OM(100).V(100).INHODE(10000).DORN(100).KQRN(100)
                                                                                              TABL 120
                                                                                              TABL 121
        COMMON TMAX.CI(100).VXI(100).VYI(100).HI(100)
                                                                                              TABL 122
  MPOUT IS CALLED TO PRODUCE INMODE MATRIX AND OM AND V VECTORS. CALL MPOUT(GM1.0M2.V1.V2.NOM.NVP.INMODE.OM.V.THETK)
                                                                                              TABL
                                                                                              TABL
                                                                                                   124
                                                                                              TABL 125
C
  IFLAG = 1 INDICATES FIRST TIME THROUGH WRITE PROCEDURE LETAG = 1
                                                                                              TABL
                                                                                                   126
                                                                                              TABL 127
                                                                                             TARL 128
C IMMODE IS PRINTED IF NOPT IS POSITIVE IF (NOPT-GE-0) GO TO 123
                                                                                             TABL 129
                                                                                              TABL 130
     5 IFLAG = 0
                                                                                             TABL 131
                                                                                             TABL 132
        NOPER=0
C NOPER IS THE NUMBER OF EXPANSION OPERATIONS PERFORMED IN THE PRESENT C SCAN OF THE MATRIX. THUS. NOPER IS THE NUMBER OF SUSPICIOUS POINTS C FOUND IN THE PRESENT SCAN.
                                                                                             TABL 133
                                                                                              TABL
                                                                                             TABL 135
                                                                                                          PROGRAM
                                                                                             TABL 136
C BEGIN SCANNING OF INTERIOR ELEMENTS OF INMODE IN UPPER LEFT CORNER
                                                                                              TABL 137
                                                                                                             TABLE
                                                                                             TABL 138
                                                                                                              PAGE
        M = 2
                                                                                             TABL 139
    10 CALL SUSPCTIN. H. HVP. INMODE. ISUS)
                                                                                             TABL 140
```

, S.

```
C C POINT (N.M) IS SUSPICIOUS IF ISUS.NE.0 IF(ISUS.NE.0) GO TO 60
                                                                                                              7451 341
                                                                                                             TARL 142
                                                                                                             TABL 144
TABL 144
TABL 145
C CHECK FOR END OF ROW
20 If (M+LT.(NOM-1)) GO TO 30
                                                                                                             TABL 147
TABL 147
TABL 148
C CHECK FOR LAST ROW

IF (No.LT.(NVP-1)) GO TO 40

GO TO 121
                                                                                                             TABL 149
                                                                                                             TABL 150
                                                                                                             TABL 151
C MOVE ONE COLUMN TO RIGHT
                                                                                                             TABL 152
TABL 153
    30 M = M+1
GO TO 10
                                                                                                             TABL 154
                                                                                                             TABL 155
C ADVANCE UNE ROW AND START AT COLUMN TWO
                                                                                                             TABL 156
    40 N = N+1
M = 2
                                                                                                             TABL 157
TABL 158
        GO TO 10
                                                                                                             TABL 159
C CHECK FOR MAXIMUM VALUE OF NVP
                                                                                                             TABL 160
                                                                                                             TABL 161
TABL 162
TABL 163
    CHECK FOR MAXIMUM VALUE OF NV

50 IF(NVP.LT.100) GO TO 62

61 FORMAT (24H NVP = 100

WRITE (6.61) N.K

GO TO 20

62 IF(NOM .LT. 100) GO TO TO

63 FORMAT(24HNOM = 100

64 WRITE(6.63) N.M

GO TO 20

20 IE(15US .ME. 1) GO TO 75
                                                       H =.13.8H
                                                                            K =. [3)
                                                                                                             TABL 164
                                                                                                             TABL 165
TABL 166
                                                       N=.13. 8H
                                                                              M-, 13)
                                                                                                             TABL 167
                                                                                                             TABL 168
                                                                                                             TABL 169
TABL 170
    70 IF(ISUS .NE. 1) GO TO 75
                                                                                                             TABL 171
C ADD ROW ABOVE SUSPICIOUS POINT
                                                                                                             TABL 172
                                                                                                             TABL 173
TABL 174
        N1=N-1
    ADD A COLUMN TO LEFT OF SUSPICIOUS POINT
                                                                                                             TABL 175
        M1=M-1
GO TO 100
                                                                                                            TABL 176
TABL 177
    75 IF(ISUS .NE. 21 GO TO 80
                                                                                                             TABL 178
    ADD A COLUMN TO RIGHT OF SUSPICIOUS POINT
C
                                                                                                             TABL 180
                                                                                                            TABL 181
TABL 182
        M1=M
                                                                                                             TABL 183
    ADD ROW ABOVE SUSPICIOUS POINT
        N1=N-1
GO TO 700
                                                                                                             TABL 184
                                                                                                            TABL 185
TABL 186
    80 IF(ISUS .NE. 3) GO TO 85
                                                                                                             TABL 187
    ADD A COLUMN TO RIGHT OF SUSPICIOUS POINT
C
                                                                                                             TABL 188
        M1=M
                                                                                                            TABL 189
TABL 190
TABL 191
TABL 192
    ADD ROW BELOW SUSPICIOUS POINT
        MION
        60 TO 100
                                                                                                            TABL 193
TABL 194
TABL 195
TABL 196
   ADD ROW BELOW SUSPICIOUS POINT
    85 N1=N
                                                                                                            TABL 197
    ADD A COLUMN TO LEFT OF SUSPECTOUS POINT
  M1=M-1
100 CONTINUE
                                                                                                            TABL 199
                                                                                                            TABL 200
        CALL LNGTHN(OM.V.INMODE.NOM.NVP.NVPP.N1.1.THETK)
CALL WIDEN(OM.V.INMODE.NOM.NOMP.NVPP.N1.1.THETK)
                                                                                                            TABL 201
TABL 202
TABL 203
         NY P-NYPP
         NOM-NOMP
                                                                                                            TABL 204
TABL 205
TABL 206
        NOPER-NOPER+1
        GO TO 10
                                                                                                                           PROGRAM
  121 CONTINUE IFINDPER . WY O .AND. NVP .LT. 100 .AND. NOM .LT. 100) GD TO 5
                                                                                                            TABL 207
                                                                                                                              TABLE
                                                                                                            TABL 208
                                                                                                            TABL 209
TABL 210
C C DO NOT PRINT INHODE IF NOPT IS NEGATIVE
                                                                                                                               PAGE
79
```

```
TABL 211
TABL 212
TABL 213
          IF(NOPT .LT. O) RETURN
C LABELING
    127 FORMAT (6HIVPHSF+6X+36HNOPMAL MODE DISPERSION FUNCTION SIGN/)
                                                                                                                       TABL 214
   123 WRITE (6-122)
101 133 1=1.NVP
101 128 J=1.NOM
1F (INMODE((J-1)*NVP+1)-1) 126.125.124
                                                                                                                       TABL 215
TABL 216
                                                                                                                       TABL 217
TABL 218
   124 CONTINUE
                                                                                                                       TABL 219
                                                                                                                       TARL 220
TABL 221
C IF INMODE = 5. DORN = 1HX
          DATA Q1/1HX/
DORN(J) = 91
                                                                                                                       TABL 222
                                                                                                                       TARL 223
   GO TO 127
125 CONTINUE
                                                                                                                       TABL 224
TABL 225
                                                                                                                       TABL 276
C IF INMODE = 1. DURN = 1H+
                                                                                                                       TABL 228
          DATA 02/1H+/
DORN(J) = 02
GO TO 127
                                                                                                                       TABL 230
                                                                                                                       TABL 231
TABL 232
TABL 233
    126 CONTINUE
C IF INMODE = -1. DORN = 1H-
DATA Q3/1H-/
DORN(J) = Q3
                                                                                                                       TABL 234
                                                                                                                       TABL 235
TABL 236
    127 CONTINUE
                                                                                                                       TABL 237
    124 CONTINUE
                                                                                                                       TABL 238
TABL 239
C PRINT BOW I OF TABLE

WRITE (6.130)V(I).(DORN(J). J=1.NOM)

130 FORMAT(IM .FR.5.3X.100Al)
                                                                                                                       TABL 24C
TABL 241
                                                                                                                       TABL 242
                                                                                                                       TABL 243
TABL 244
          310 = 10
00 150 J=1.NOM
                                                                                                                       TABL 245
 C MIMBER COLUMNS
   150 KORN(J) = MON(J.Jin)
MRITE (6.213) (KORN(J). J=1.NOM)
213 FORMAT (6HODMEGA.6X.10011)
                                                                                                                       TABL 247
TABL 248
TABL 249
                                                                                                                       TABL 250
                                                                                                                       TABL 251
TABL 252
TABL 253
 C CONVERT THETK FROM PADIANS TO DEGREES
    X = THETK+1RO/3.14159

X = THETK+1RO/3.14159

HRITE (4.413) X

413 FORMAT F1H .11X.27HPHASE VELOCITY DIRECTION IS.E9.3.

1 RHDEGREES 1

HRITE (6.513)
                                                                                                                       TABL 254
                                                                                                                       TABL 255
TABL 256
TABL 257
    513 FORMAT ( RHOOMEGA =)
                                                                                                                       TABL 258
TABL 259
 C LIST VALUES OF OMEGA WHICH CORRESPOND TO COLUMNS OF TABLE WRITE (6,673) (OM(I)+1=1.NOM)
613 FORMAT.( 1H .5E14-5)
                                                                                                                       TABL 260
TABL 261
                                                                                                                       TABL 262
         SUSPICION ELIMINATION HAS NOT REEN PERFORMED, BEGIN IT AT THIS TIME TABL 263
                                                                                                                       TABL 264
TABL 265
           IFITELAG. FO. 11 GO TO 5
           OF THEN
                                                                                                                       TABL 266
           FND
```

PROGRAM TABLE PAGE BO

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TABPRT (SUBROUTINE)
                                                                                                          7/31/69
                                                                                                                                                                                               TBPR
                                                                                                                                                                                               TBPR
                                                  ----ABSTRACT----
                                                                                                                                                                                               TBPR
                                                                                                                                                                                               TRPR
     TITLE - TARPET
                       TARPRT
PRIGRAM TO PRINT OUT LISTS OF FREQUENCY, PHASE VELOCITY,
AMPLITUDE, AND PHASE FOR EACH GUIDED MODE EXCITED BY A NUCLEAR
EXPLOSION OF GIVEN VIELD. THE SIMULTANEOUS LISTING OF FREQUENC
AND PHASE VELOCITY REPRESENTS THE DISPERSION CURVE FOR THE
GUIDED MODE. THE QUANTITIES AMPLTO AND PHASE DEPEND ON SOURCE
AND OBSERVER HEIGHTS AS WELL AS THE MODEL ATMOSPHERE. HOWEVER,
THE LATTER INFORMATION IS NOT LISTED BY TABPRT AND IS PRESUMED
TO BE LISTED BY ANOTHER SUPROUTINE. THE SUBROUTINE TABPRT
SHOULD NOT BE CALLED UNTIL ALL THE QUANTITIES TO BE LISTED
HAVE BEEN COMPUTED AND STORED IN THE MACHINE. NORMALLY,
ATMOS. TABLE. ALLMOD, PAMPDE, AND PPAMP WOULD BE CALLED BEFORE
                                                                                                                                                                                               TAPR
                                                                                                                                                                                              TRPP
                                                                                                                                                                                               TBPR
                                                                                                                                                                                              TRPR
                                                                                                                                                                                               TAPR
0000
                                                                                                                                                                                               TBPR
                                                                                                                                                                                                             10
                                                                                                                                                                                              TBPR
                                                                                                                                                                                              TAGO
                                                                                                                                                                                                              12
                                                                                                                                                                                               TBPR
                                                                                                                                                                                              TBPR
C
                                                                                                                                                                                               TBPR
                                                                                                                                                                                              TRPR
                                                                                                                                                                                                             16
                       TABPRT.
                                                                                                                                                                                              TRPR
                                                                                                                                                                                                             17
                                                                                                                                                                                              TBPR
                                                                                                                                                                                                             18
                                 - FORTRAN IV (360, REFERENCE MANUAL C28-6515-4)
- A.D.PTERCE AND J.POSEY. M.I.T., JULY-1968
     LANGUAGE
                                                                                                                                                                                              TBPR
     AUTHORS
                                                                                                                                                                                              TBPR
                                                                                                                                                                                                             20
                                                                                                                                                                                              TRPR
                                                 ----CALLING SEQUENCE----
                                                                                                                                                                                              TRPR
                                                                                                                                                                                              TAPR
     DIMENSION KST(1).KFIN(1).OMMOD(1).VPMOD(1).AMPLTD(1).PHASQ(1)
THE SUBROUTINE USES VARIABLE DIMENSIONING. THE TRUE DIMENSIONS MUST
BE GIVEN IN THE PROGRAM WHICH DEFINES THESE QUANTITIES. SEE THE
DIMENSION STATEMENTS IN THE MAIN PROGRAM.
                                                                                                                                                                                              TBPR
                                                                                                                                                                                              TRPR
                                                                                                                                                                                                             25
                                                                                                                                                                                              TBPR
                                                                                                                                                                                              TBPR
               CALL TABPRT(YIELD. MDFND. KST. KFIN. OMMOD. VPMOD. AMPLTD. PHASO)
                                                                                                                                                                                              TBPR
                                                                                                                                                                                              TRPR
     NO EXTERNAL SUBROUTINES ARE REQUIRED
                                                                                                                                                                                              TRPR
                                                                                                                                                                                                             30
                                                                                                                                                                                              TRPS
                                                ----ARGUMENT LIST----
                                                                                                                                                                                              TBPR
                                                                                                                                                                                             TRPR
                YIELD
                                                              ND
                                                                                                                                                                                              TBPR
                MDFND
                                            1 *4
                                                              ND
                                                                              INP
                                                                                                                                                                                              TBPR
CCC
               KST
                                            1#4
                                                              VAR
                                                                             INP
                                                                                                                                                                                              TBPR
                                            144
                                                              VAR
                                                                             INP
                                                                                                                                                                                              TRPR
                                                                                                                                                                                                             37
               OMMOD
                                                                                                                                                                                             TRPR
                                                                                                                                                                                                             38
                VPMOD
                                            R #4
                                                              VAR
                                                                              INP
                                                                                                                                                                                              TBPR
C
                AMPI TO
                                            2+4
                                                              VAR
                                                                             IND
                                                                                                                                                                                             TRPR
                                                                                                                                                                                                             40
                PHASO
                                            R*4
                                                             VAR
                                                                                                                                                                                             TBPR
                                                                             INP
                                                                                                                                                                                                             41
                                                                                                                                                                                              TBPR
     NO COMMON STORAGE USED
                                                                                                                                                                                              TBPR
                                                                                                                                                                                              TRPR
                                                ----INPUTS----
                                                                                                                                                                                             TAPR
                                                                                                                                                                                                            45
Ċ
                                                                                                                                                                                              TBPR
                                              =ENERGY Y(ELD OF EXPLOSION IN EQUIVALENT K(LOTONS (KT) OF TNT. 1 KT = 4.2X(10) ==19 ERGS. =NUMBER OF NORMAL MODES FOUND
               YIELD
                                                                                                                                                                                             TRPR
Ċ
                                                                                                                                                                                             TAPR
                HDFND
                                                                                                                                                                                             TBPR
                                                                                                                                                                                                             49
                                              =INDEX OF FIRST TABULATED POINT IN N-TH MODE
=INDEX OF LAST TABULATED POINT IN N-TH MODE.
Ĉ
                                                                                                                                                                                              TBPR
                                                                                                                                                                                                             50
                KF IN(N)
                                                                                                                                                                                              TRPR
                                                 GENERAL. KFIN(N)=KST(N+1)-1.
                                                                                                                                                                                             TRPR
CCC
                                             #ARRAY STORING ANGULAR FREQUENCY ORDINATE (RAD/SEC) OF POINTS ON DISPERSION CURVES. THE NMODE MODE IS STORE FOR N RETMEEN KST(NMODE) AND KFIN(NMODE).

#ARRAY STORING PHASE VELOCITY ORDINATE (KM/SFC) OF POINTS ON DISPERSION CURVES. THE NMODE MODE IS STORE FOR N RETMEEN KST(NMODE) AND KFIN(NMODE).

#AMPLITUDE FACTOR REPRESENTING TOTAL MAGNITUDE OF FOURIFR TRANSFORM OF THE CONTRIBUTION TO THE WAVEFORM FROM A SINGLE GUIDED MODE AT FREQU'NCY OMMODIN).

ITS UNITS SHOULD BE (DYNES/CM**2)* (KM**(1/2))*SEC.

IT REPRESENTS THE AMPLITUDE OF NMODE—TH MODE IF N IS BETWEEN KST(NMODE) AND KFIN(NMODE), INCLUSIVE. FOR PRECISE DEFINITION. SEE SUBROUTINE PPAMP.

#PHASE LAG IN RADIANS AT FREQUENCY OMMOD(N) FOR THE NMODE—TH MODE HHEN N IS BETWEEN KST(NMODE) AND KFIN(NMODE). INCLUSIVE. THE INTEGRAND IS UNDERSTOOD TO HAVE THE FORM AMPLITD**COS(OMMOD**(TIME-DISTANCE/VPMO**) FOR A PRECISE DEFINITION. SEE SUBROUTINE
               OMMOD (N)
                                               *ARRAY STORING ANGULAR FREQUENCY ORDINATE (RAD/SEC) OF
                                                                                                                                                                                             TRER
                                                                                                                                                                                                             53
                                                                                                                                                                                             TBPR
                                                                                                                                                                                              TRPR
Ċ
               VPMOD (N)
                                                                                                                                                                                             TBPR
                                                                                                                                                                                                             56
                                                                                                                                                                                             TBPR
                                                                                                                                                                                                             57
                                                                                                                                                                                              TBPR
               AMPLTD(N)
                                                                                                                                                                                              TBPR
                                                                                                                                                                                             TRPR
                                                                                                                                                                                                            60
                                                                                                                                                                                             TBPR
                                                                                                                                                                                                            61
000
                                                                                                                                                                                             TBPR
                                                                                                                                                                                              TBPR
                                                                                                                                                                                             TRPR
                                                                                                                                                                                             TRPR
                                                                                                                                                                                                            65
               PHASQ(N)
                                                                                                                                                                                             TRPR
                                                                                                                                                                                                                       PROGRAM
                                                                                                                                                                                                            66
                                                                                                                                                                                             TRPR
                                                                                                                                                                                                                          TABPRT
                                                                                                                                                                                             TRPR
                                                                                                                                                                                                                              PAGE
                                                                                                                                                                                             TRPR
                                                 +PHASO). FOR A PRECISE DEFINITION. SEE SUBROUTINE
```

T 55.57

```
PPAMP.
C.
                                                                                     TSPR
                                                                                            72
73
                                                                                     TRPP
                     ---- OUTPUTS----
                                                                                     TRPR
                                                                                     TEPR
  PRINTOUT. THE ONLY FUNCTION OF TABPET IS TO PRINT OUT RESULTS.
                                                                                     TBPR
                                                                                     THPR
                     ----EXAMPLF----
                                                                                     TBPR
                                                                                     THPR
C THE DUTPUT FORMAT IS ILLUSTRATED BELOW.
                                                                                     TBPR
                                                                                     TBPR
TBPR
                                                                                            80
                               MODE TABULATION FOR Y=
                                                           100-00 KILOTONS
                                                                                            81
                                                                                     TBPR
                                                                                     TBPR
                                                                                            83
                                                                                     TOPR
      MODE
              1
                                                                                     TBPR
                                                                                     TBPR
             OMEGA
                             VPHSE
                                                                                     TRPR
                                              AMPLID
                                                              PHASE
                                                                                            47
                                                                                     TRPR
                                                                                            88
89
                               0.33426 -7.01342F 20
0.24372 -8.02394E 20
                                                              -3.72139
                .00100
                                                                                     TRPR
                .00200
                                                              -4.56028
                                                                                     TRPR
                                                                                            90
                                                                                     TBPR
                                                                                     TRPR
                                                                                     TBPR
                                                                                            93
      MODE
                                                                                     TRPR
              2
                                                                                            94
                                                                                     TBPR
                                                                                            95
             OMEGA
                              VPHSE
                                                                                     TRPR
                                              AMPL TO
                                                              PHASE
                                                                                            96
                                                                                     TBPR
                .00100
                                        -7.95321F 10
                                                              -2.40798
                                                                                     TBPR
                                                                                            98
                .00200
                               0.48321
                                         -1.23108E 11
                                                              -2.30524
                                                                                     TBPR
                                                                                            99
                                                                                     TBPR
                                                                                          100
C FTC.
                                                                                     TBPR
                                                                                          101
                                                                                     TBPR
                                                                                          102
                     ---- PROGRAM FOLLOWS BELOW----
                                                                                     TBPR
                                                                                          103
Ċ
                                                                                     TBPR
                                                                                          104
       SUBROUTINE TABPET(YIELD. MOFND. KST. KFIN. OHMOD. VPMOD. AMPLTD. PHASO)
                                                                                     TBPR
                                                                                          105
                                                                                     TAPR
                                                                                          106
  VARIABLE DIMENSIONING IS USED
                                                                                     TBPR
                                                                                          107
      DIMENSION KST(1) -KFIN(1) - OMMOD(1) - VPMOD(1) - AMPLTD(1) - PHASQ(1)
                                                                                     TAPR
                                                                                          108
                                                                                     TRPR 109
C
                                                                                     TBPR
       WRITE (6.11) YIELD
                                                                                          110
   11 FORMATE 1H1
                       .1H .25x.22HMODE TABULATION FOR Y=.F9.7.9H KILOTONS)
                                                                                     TRPR
                                                                                          111
C START OF OUTER DO LOOP
                                                                                     TBPR
      DO 50 IT=1. MOFNO
                                                                                     TBPR
                                                                                     TBPR
                                                                                          115
   WRITE (6.21) II
21 FORMAT(1H ///.1H .4X. SHMODE .13//. 1H .9X.5HOMFGA.9X.5HVPHSE.9X.
1 6HAMPLTO.8X.5HPHASE/ )
                                                                                     TBPR
                                                                                          116
                                                                                     TBPR
                                                                                          117
                                                                                     TBPR
                                                                                          118
                                                                                     TRPR
C.
       K1=KST(II)
                                                                                     TBPR
       K2=KFINITT1
                                                                                     TBPR
                                                                                          121
                                                                                     TRPR
                                                                                          155
                                                                                     TRPR
C START OF INNER DC LOCP
                                                                                          123
                                                                                     TRPR
      00 50 J#K1.K?
                                                                                          124
                                                                                     TRPR
   50 WRITE (6,51) OMMCD(J). VPMOD(J). AMPLTD(J). PHASO(J)
                                                                                     TBPR
51 FORMAT( 1H ,4X.F14.5.F14.5.1PG14.5.0PFR4.5)
C END OF LOOPS
                                                                                     TRPR
                                                                                     TRPR 128
                                                                                     TBPR 129
                                                                                     TBPR
       RETURN
                                                                                          130
                                                                                     TBPR 131
       END
```

PROGRAM TABPRT PAGE

```
THEY - SUPROUTINES
                                                    7/19/68
                                                                                               THPT
                                                                                               TMPT
                                                                                               TMPT
                         ----ARSTRACT----
                                                                                               THPT
                                                                                               THOT
  TITLE - THEY
                                                                                               THOT
           CALCU' ATION AND PLOTTING OF FAP-FIELD TRANSIENT RESPONSE TO A
                                                                                               TMPT
            PRESSURE SOURCE IN THE ATMOSPHERE
                                                                                               THPT
                                                                                               THPT
                   THE RESPONSE OF MODE N IS FOUND BY INTEGRATING CAMPLED *
                                                                                               YMPT
                                                                                                      10
                   CIST DHEGA * (T - R/VP) + PHASO) OVER DHEGA FROM DHMOD
                                                                                               THPT
                   (KST(N)) TO OMMODERFINEN)) AND DEVEDING BY SORTER). VP.
                                                                                               TMPT
                   PHASO. AND AMPLTO APE FUNCTIONS OF BOTH N AND OMEGA. TOTAL RESPONSE IS THE SUM OF THE MODAL RESPONSES. THE RESPONSE IS CALCULATED FOR TIME TELEST AND AT INTERVALS
                                                                                               TMOT
                                                                                                      13
                                                                                               THOT
                                                                                               TMPT
                                                                                                      15
                   OF DELTT THEREAFTER UNTIL TEND IS REACHED. THE VALUE OF IOPT DETERMINES WHAT WILL BE CALCULATED. PRINTED AND PLOTTED. (SEE INPUT LIST FOR POSSIBLE IOPT VALUES.) THE
                                                                                               TMPT
                                                                                                      16
                                                                                               THPT
                                                                                                      17
                                                                                               THPT
                   RESULTS ARE TABULATED IN THE PRINTOUT AND GRAPHED BY THE
                                                                                               THPT
                                                                                                      19
                   CALCOMP PLOTTER.
                                                                                               THPT
                                                                                                      20
                                                                                               THPT
C LANGUAGE
                - FORTRAN IV (360, REFERENCE MANUAL C28-6515-4)
                                                                                               THPT
  AUTHOR
                - J.W.POSFY, M.I.T.. JUNE,1968
                                                                                               TMPT
                                                                                                      23
                                                                                               THPT
                                                                                                      24
                                                                                               TMPT
                                                                                                      25
                         ----USAGF----
                                                                                               THPT
                                                                                                      26
                                                                                               TMPT
       FORTRAN SUBROUTINE AKT IS CALLED
                                                                                               TMPT
                                                                                               TMPT
       CALCOMP PLOTTER SUBROUTINES PLOTI. AXISI. NUMBRI. SYMBLS. AND SCLEPH ARE CALLED TO WRITE THE CALCOMP TAPE. SUBROUTINE NEWPLT MUST HAVE BEEN CALLED PRIOR TO CALLING TMPT. AND ENDPLT MUST RE
                                                                                               TMDT
                                                                                                      30
                                                                                               THOT
                                                                                               THOT
                                                                                                      32
       CALLED AFTER RETURNING FROM TMPT. (SEE MAIN PROGRAM)
                                                                                               THPT
                                                                                                      32
                                                                                               THPT
                                                                                               THPT
       CALL TMPT(TFIRST.TEND.DELTT.ROBS.MDFND.KST.KFIN.OMMOD.VPMOD.AMPLTO
                                                                                               TMPT
                                                                                                      36
      1 .PHASO. TOPTE
                                                                                               THPT
                                                                                              TMPT
                                                                                                      35
  INDUTS
                                                                                               TMPT
                                                                                                      39
                                                                                               TMPT
      TFIRST
                   TIME AT WHICH TABULATION AND PLCTTING OF RESPONSE IS TO
                                                                                               TMPT
                                                                                                      41
                   BEGIN (SEC)
                                                                                               TMPT
                                                                                               TMPT
      TEND
                   TIME AT WHICH "ABULATION AND PLOTTING OF RESPONSE IS TO
                                                                                               TMPT
         9 *4
                   FND (.LE.(TFIRST+5400.)) (SEC)
                                                                                               TMPT
                                                                                              THPT
                   TIME INTERVAL RETWEEN SUCCESSIVE CALCULATIONS OF THE
      DELTT
                                                                                               TMPT
                   RESPONSE (.GF. (ITEND-TFIRST)/1000))
         R#4
                                                                 (SEC)
                                                                                               THOT
                                                                                                      48
                                                                                               TMPT
                                                                                                      49
      2095
                   DISTANCE OF THE OBSERVOR FROM THE SOURCE OF THE DISTUR-
                                                                                               TMPT
                                                                                                      50
                   BANCE (KM)
                                                                                               TMPT
                                                                                               TMPT
      MDFNO
                   NUMBER OF MODES FOUND (.LE.10)
                                                                                               TMPT
         1 *4
                                                                                              TMPT
                                                                                              TMPT
      KST
                   FLEMENT N OF THIS VECTOR IS NUMBER OF OMMOD ELEMENT WHICH
                                                                                              TMPT
                                                                                                      56
                   IS FIRST FREQUENCY CONSTDERED FOR MODE N
                                                                                              THPT
                                                                                                      57
                                                                                              TMPT
      KFIN
                   ELEMENT N OF THIS VECTOR IS NUMBER OF OMMOD FLEMENT WHICH
                                                                                              THP?
         1*4(0)
                   IS LAST FREQUENCY CONSIDERED FOR FINE N
                                                                                               TMPT
                                                                                                      60
                                                                                              TMPT
                                                                                                      61
                   ELEMENTS OF THIS VECTOR NUMBERED KST(N) THROUGH KF(N(N) ARE THE VALUES OF FREQUENCY (IN INCREASING ORDER) FOR WHICH THE COPPESPONDING MODE N PHASE VELOCITIES HAVE REEN
      OMMOD
                                                                                              TMPT
        R=4(D)
                                                                                              TMDT
                                                                                                      63
                                                                                              TMDT
                                                                                                      44
                   DETERMINED
                                                                                               TMPT
                                                                                                      45
                                                                                               TMPT
                                                                                                           PROGRAM
                                                                                                      66
      VPMOD
                   VECTOR OF PHASE VELOCITIES WHICH CORRESPOND TO THE FRE-
                                                                                               TMPT
                                                                                                              TMPT
        R#4(0)
                  QUENCIES OF VECTOR OMMOD
                                                                                              TMPT
                                                                                              TMPT
                                                                                                               PAGE
                   VALUES OF AMPLITUDE FUNCTION IN AKI INTEGRAL CELEMENTS
      AMPLITO
                                                                                              TMPT
                                                                                                                 83
```

```
R#4(D) CORRESPOND DIRECTLY TO FLEMENTS OF OMMOD) (DYNES/CM*#2)
                                                                                                    TMPT
                                                                                                            72
                                                                                                    TMPT
                    TERM IN ARGUMENT OF COS IN AKI INTEGRAL WHICH IS INDEPEN-
      PHASO
         R#4(D)
                    DENT OF TIME AND DISTANCE (ROBS)
                                                                                                    THET
                                                                                                    TMPT
                                                                                                            75
      TENT
                    COMPUTATION AND PRINT OPTION INDICATOR
                                                                                                    TMPT
                    THPT
                                                                                                    TMPT
                                                                                                            78
                                                                                                    TMPT
                                                                                                    THPT
                                                                                                    TMPT
                                                                                                            92
                                                                                                    TMPT
                                                                                                    TKPT
      THE ONLY OUTPUTS ARE THE PRINTOUTS AND PLOTS CALLED FOR BY TOPT. ALL GRAPHS ARE DRAWN TO THE SAME SCALE. THE PRESSURE SCALE IS DETERMINED BY THE MAXIMUM AMPLITUDE OF THE TOTAL PRESSURE. AND THE
                                                                                                    TMPT
                                                                                                            85
                                                                                                    TMPT
                                                                                                            36
                                                                                                    MPT
      TIME SCALE IS 600 SEC PER INCH. PRESSURE IS EXPRESSED IN DYNES/CH+
                                                                                                    TMPT
                                                                                                    TMPT
                                                                                                            89
                                                                                                    TMPT
                                                                                                            90
                           ---- PROGRAM FOLLOWS RFLOW----
                                                                                                    TMPT
                                                                                                    TMPT
                                                                                                            92
                                                                                                    TMPT
                                                                                                            93
        SHAROUTINE THPT(TFIRST.TEND.DELTT.ROBS.
                                                                                                    TMPT
                              MDFND.KST.KFIN.OMMOD.VPMOD.AMPLTD.PHASQ. 10PT)
                                                                                                    TMPT
C
                                                                                                    TMPT
                                                                                                            96
       DIMENSION KST(10).KFIN(10).UMMUD(1000).VPMOD(1000).AMPLTD(1000).
1 PMASO(1000).T(1001).TOTINT(1001).TN[NT(10.1001).Y(1001).
                                                                                                    TMPT
                                                                                                    THPT
                                                                                                    TMPT
                                                                                                            99
C VAX IS VECTOR OF LITERAL CONSTANTS. ELEMENT N IS THE EIGHT SPACE LABE FOR THE PRESSURE AXIS ON THE GRAPH OF THE MODE N RESPONSE.
                                                                                                          100
                                                                                                    TMPT
                                                                                                    TMPT
        THE PRESTURE MAIS UNITHE GRAPH OF THE MODE N RESPONSE.

DOUBLE PRECISION YAX(10)

DATA YAX/AH MODE 1 .8H MODE 2 .8H MODE 3 .8H MODE 4 .8H MODE 5 .

AN MODE 6 .8H MODE 7 .8H MODE 8 .8H MODE 9 .8H MODE 10/

IF(IOPT .NF. 11) GO TO 4
                                                                                                          101
                                                                                                    THPT
                                                                                                    TMPT
                                                                                                          103
                                                                                                    TMPT
                                                                                                          104
                                                                                                           105
         WRITE (6.2)
                                                                                                    TMDT
                                                                                                           106
                                                                                                    TMPT 107
     2 FORMAT (1H1+ 40X+23HTABULATION OF RESPONSES//)
                                                                                                    TMPT
                                                                                                          108
        WRITE (6.3)
      3 FORMAT (1H +20x.4HTIME+12x+5HTOTAL+11x+6PMODE 1+10x+6HMODE 2+10x+
                                                                                                    THPT
                                                                                                          109
   1 6HMODE 3-10X-6HMODE 4-10X-6HMODE 5/)
4 IF(INPT-EG-12) WRITE(6-753)
753 FORMAT (1H1-45X-40HTABULATION OF ACOUSTIC PRESSURE RESPONSE///1H -
                                                                                                    TMPT 110
                                                                                                    TMPT
                                                                                                          111
                                                                                                    TMPT
                                                                                                    TMPT 113
      1 48X.10HTIMF (SEC).9X.15HP (DYNES/CH++21//)
                                                                                                    TMPT 114
T & IS NUMBER OF TIMES AT WHICH RESPONSE IS TO BE CALCULATED L = (TEND -TEIRST) / DELTT + 1
                                                                                                    TMPT
                                                                                                    TMPT
                                                                                                    TMPT
C SIZE = ( TEND - TERST ) / 600.0
                                                                                                    TMPT
                                                                                                          118
                                                                                                    TMPT
                                                                                                    TMPT
C PRESET ALL RESPONSE VALUES TO 0.0
                                                                                                    TMPT
     5 DO 7 K=1.L
                                                                                                    THPT
                                                                                                          122
        TOTINT(K) = 0.0
DO 7 N=1.10
                                                                                                    TMPT
                                                                                                    THPT
                                                                                                    TMPT
     7 THINTINGE = 0.0
                                                                                                          125
                                                                                                    TMPT
                                                                                                          126
C SET UP TABLE OF TIMES REGINNING AT TEIRST AND TAKING VALUES OF TIME AT C INTERVALS OF DELTT UNTIL TEND IS PEACHED
                                                                                                    TMPT
                                                                                                    THOT
                                                                                                          128
    9 00 10 17=1+1
10 T(1T) = TFIRST + (1T-1)=DELTT
                                                                                                    THPT
                                                                                                          129
                                                                                                           130
                                                                                                    TMPT
C REGIN SET UP TO CALCULATE MODE 1 RESPONSE
                                                                                                    THPT
                                                                                                          132
                                                                                                    TAPT
                                                                                                    TMPT
C IF TOPT-LE-10 CALCULATE UNLY MODE INPT RESPONSE
IF (TOPT-LE-10) N = INPT
11 NOST = KST(N) + 1
                                                                                                    TMPT
                                                                                                          135
                                                                                                                 PROGRAM
                                                                                                    TMPT
                                                                                                          136
                                                                                                    TMPT
                                                                                                                    TMPT
                                                                                                    THPT 138
                                                                                                    TMPT
                                                                                                                     PAGE
                                                                                                          139
C THE MODE N RESPONSE IS FOUND FOR ALL VALUES OF T REFORE NEXT MODE IS
```

```
r considered
                                                                                                                                                               TMPT 141
             00 51 IT=1.L
                                                                                                                                                                THPT 142
                                                                                                                                                                THPT 143
C SET AZ-PHP FQUAL TO VALUES FOR AL-PHI IN FIRST INTEGRATION INTERVAL
                                                                                                                                                                TMPT 144
             A? = AMPLID(KST(N))
                                                                                                                                                                TMPT 145
              S2=OMMOD(KST(N))/VPMOD(KST(N))-PHASQ(KST(N))/RORS
                                                                                                                                                                THPT 146
             SLOW=T(TT) /ROBS
                                                                                                                                                               TMPT 147
             DIDDLE-SLOW-1.0/VPMOD(KST(N))
PM2=ROBS*(OMMOD(KST(N))*DIDDLE+PHASQ(KST(N))/ROBS)
                                                                                                                                                                TMPT
                                                                                                                                                                         148
                                                                                                                                                               THPT
             CTRIG2=COS(PH2)
                                                                                                                                                                TMPT
             STRIG2=SIN(PH2)
                                                                                                                                                               TMPT
                                                                                                                                                               TMPT
                                                                                                                                                                         152
C THE INTEGRAL OF (AMPLTO + COSCOMEGA + (T - ROBS/VP) + PHASQ)) OVER THE
                                                                                                                                                               TMPT
    INTERVAL FROM OMMODIKSTIN)) TO OMMODIKFININ)) IS FOUND BY SUMMING THE INTEGRALS FROM OMMODINOM-1) TO OMMODINOM) FOR NOM FROM KST(N)+1 TO
                                                                                                                                                               TMPT
                                                                                                                                                               TMPT
                                                                                                                                                                          155
    KF IN(N)
                                                                                                                                                               TMPT
                                                                                                                                                                         156
             DO SO NOM - NOST.NOFN
                                                                                                                                                               TMPT
             A1 = A2
             PH1 = PH2
                                                                                                                                                               THPT
                                                                                                                                                                         159
                                                                                                                                                               THPT 160
             CTRIGI=CTRIG2
             STRIGI=STRIG?
                                                                                                                                                               THPT
                                                                                                                                                                         161
              S1=52
                                                                                                                                                               THPT
              A? = AMPLTD(NOM)
                                                                                                                                                               TMPT
                                                                                                                                                                         163
              SZ=NMMOD(NOM)/YPMOD(NOM)-PHASO(NOM)/FORS
                                                                                                                                                               TMPT
                                                                                                                                                                         164
             DIDDLE=$LOW-1.0/VPMD[NDM]
PH2=RDRS=(DMMDD[NDM]+DIDDLE+PHASQ(NDM]/RDBS)
                                                                                                                                                               TMPT
                                                                                                                                                                         165
                                                                                                                                                                TMPT
                                                                                                                                                                         166
             OMEG1=OMMOD(NOM-1)
                                                                                                                                                               THPT
                                                                                                                                                                         167
             OMEG2=OMMOD(NOM)
                                                                                                                                                               TMPT
                                                                                                                                                                         168
             DELPH * ROBS * ( SL"H * ( OMEG2 - OMEG1 ) - ( 52 - 51 ) )
                                                                                                                                                               THPT
                                                                                                                                                                         169
             CALL AKTIOMEGI. OMFGZ. AL. AZ. CYRIGI. STRIGI. CTRIGZ. STRIGZ
                                                                                                                                                               TMPT
           1 DELPH. AKTINTE
                                                                                                                                                               TMPT
      SO THINT(N. IT) = THINT(N. IT) + AKISHT
                                                                                                                                                               THPT 172
                                                                                                                                                               TMPT
C PRESSURE IS FOULL TO ( 1 / SQRT(ROBS) ) * ( VALUE OF OMEGA INTEGRAL ) 51 TNINT(N.IT) * (1/SQRT(ROBS)) * TNINT(N.IT)
                                                                                                                                                               TMPT
                                                                                                                                                               TMPT 175
                                                                                                                                                               TMPT 176
C IF 10PT-LE-10 ALL THAT IS REQUESTED IS THE MODE 10PT RESPONSE. WHICH C HAS JUST REEN CALCULATED IF (10PT-LF-10) GO TO 101
                                                                                                                                                               TMPT 178
                                                                                                                                                               TMPT 179
                                                                                                                                                               THPT 180
C INCREASE HODE NUMBER BY THE
                                                                                                                                                               TMPT 181
                                                                                                                                                               THPT 182
            N = N + 1
                                                                                                                                                               TMPT 183
C IF N IS GREATER THAN HOPAD. ALL HODAL RESPONSES HAVE BEEN DETERMINED
                                                                                                                                                               THPT 184
             IF (N.LE. MOFNO) GO TO 11
                                                                                                                                                               THPT 185
                                                                                                                                                               TMPT 186
C FOR EACH TIME IN T SET TOTAL PRESSURE EQUAL TO SUM OF MODAL PRESURES
                                                                                                                                                               TMPT 187
      D1 60 [T=1.4
D0 53 N = 1.40FND
53 TOTINT(IT) = TOTINT(IT) + TNINT(N.IT)
                                                                                                                                                               TMPT 188
                                                                                                                                                               THPT 189
                                                                                                                                                               TMPT 190
             IF(INPT.FO. 11) GO TO 55
                                                                                                                                                               TMPT 191
C WRITE TIME AND CORRESPONDING TOTAL ACOUSTIC RESPONSE (DYNES/CM++2)
                                                                                                                                                               TMPT 193
      WRITE (6.54) TITT).TOTINT(IT)
54 FORMAT (1H .49X.F9.1.10X.F12.2)
                                                                                                                                                               TMPT 194
                                                                                                                                                               THPT 195
                                                                                                                                                               TMPT 196
C, WHEN TOPT-FO-12 ONLY TOTAL RESPONSE IS PRINTED IF (INPT-EQ-12) GO TO 59
                                                                                                                                                               TMPT 197
                                                                                                                                                               TMPT 198
                                                                                                                                                               TMPT 199
C WHEN INPT. EQ. 11 ALL MODAL RESPONSES ARE ALSO PRINTED
                                                                                                                                                               TMPT 200
      55 MM = MINO(MDFND.5)
WRITE (6.57) IT.T(IT).TOTINT(IT).(ININT(N.IT).N=1.MM)
57 FORMAT (1M .3X.14.10X.F9.1.5>.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.4X.F12.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.4X.F12.2.X.F12.2.4X.F12.2.4X.F12.2.4X
                                                                                                                                                               TMPT 201
                                                                                                                                                               TMPT 202
                                                                                                                                                               THPT
                                                                                                                                                                        203
              4X.F12.2.4X.F12.21
                                                                                                                                                               TMPT 204
       59 CONTINUE
                                                                                                                                                               THPT 205
                                                                                                                                                               TMPT 206
                                                                                                                                                                                   PROGRAM
      60 CONTINUE
             IF (MOEND .1 F. 5 .OR. TOPT .NE. 11 ) GO TO 65
                                                                                                                                                               TMPT 207
                                                                                                                                                                                        TMPT
      HPITE (6.61)
61 FORMAT (1HO.20X.4HTIME.12X.5HTOFAL.11X.6HMODE 6.10X.6HMODE 7.10X.
1 6HMODE 8.10X.6HMODE 9.10X.7HMODE 10/)
                                                                                                                                                               THPY 208
                                                                                                                                                               TMPT 209
                                                                                                                                                                                          PAGE
                                                                                                                                                               TMPT 210
```

THE WINDS WE WAS A STREET TO SERVICE AND A STREET TO BE

THE PERSON WAS A STREET OF THE PERSON OF THE

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OG 63 IT=1.L
63 WRITE (6.57) IT-T([T).TOTIWT([T].(TNINT(N.IT).N=6.MDFND)
                                                                                                                             TMPT 211
TMPT 212
                                                                                                                             TMPT 213
TMPT 214
TMPT 215
     65 CONTINUE
     66 CALL PLOT1(2...3.-3)
SIZF = (T(1)-T(1))/600.
IF (IOPT.LF.10) GO TO 107
CALL DXDY1(TOTINT,L.3.0.UMIN.DY.ND.K)
UMIN = AINT(UMIN/25) * 25.0
                                                                                                                             THPT 216
                                                                                                                             TMPT 217
                                                                                                                             TMPT 219
TMPT 220
TMPT 221
          UMIN = AMINITUMIN.-25.1
DY = ARSTUMIN)
                                                                                                                             TMPT 222
TMPT 223
TMPT 224
C IF INPT.EQ.12 PLOT ONLY THE TOTAL ACOUSTIC RESPONSE IF (IOPT.EQ.12) GO TO TO
                                                                                                                             TMPT 225
C DRAW PRESSURF AXTS
CALL PLOTI(0..0..3)
ABC = HDFN0
                                                                                                                             TMPT 226
TMPT 227
                                                                                                                             THPT 228
           CALL PLUTITARC .0. .2)
                                                                                                                             TMPT 229
     00 69 N=1.#DFND
D0 67 J=1.1
67 Y(J) = -1 * TNINT(N,J)
68 CALL PLOTI(1..0..-3)
                                                                                                                             TMPT 230
                                                                                                                             THPT
                                                                                                                                     231
                                                                                                                             THPT 232
                                                                                                                             TMPT 233
                                                                                                                             TMPT 234
   PLOT ACQUITTC RESPONSE (DYNES/CH+2) OF MODE N VERSUS TIME (SEC)
                                                                                                                             TMPT 235
                                                                                                                             TMPT 236
     69 CALL SCLGPHEY.T.L.O..1.0..0Y.T[1].600.1
                                                                                                                             TMPT 237
TMPT 238
     70 DO 73 J=1.L
73 Y(J) = (-1) * TOTINT(J)
                                                                                                                             THRT 239
                                                                                                                             TMPT 240
     TRAM PRESSURE AXIS

75 CALL PLOT1(0..0..3)

CALL PLOT1(1.5.0..-3)

CALL PLOT1(1.5.0..-3)

CALL NUMBRI(.9...15..15.DY.180..0)

CALL SYMBL5(.4...15..15.MICROBARS PER INCH*.180..18)

CALL AXIS1(1.5.0..* '-1.SIZE.90..T(1).1800..0.0.3.)

CALL SYMML5(1.8.2...15.*TIMF (SFC)*.90..10)

CALL SCLGPH(Y.T.L.0..1.0..DY.T(1).600.)

CALL PLOT1(8....3.-3)

GO TO 200
C DRAW PRESSURE AXIS
                                                                                                                             TMPT 241
                                                                                                                             TMPT 242
                                                                                                                             TMPT 243
                                                                                                                             THPT 244
                                                                                                                             TMPT 245
                                                                                                                             TMPT 246
                                                                                                                             THPT 247
                                                                                                                             TMPT 248
                                                                                                                             THPT 249
                                                                                                                             TMPT 250
TMPT 251
C PRINT HISTORY OF MODE IOPT ONLY 101 WRITE (8-102) IOPT ONLY 102 FORMAT (1H1-45x-19HTARULATION OF MODE +12+ 9H RESPONSE///H +48x+ 10HTINE (SEC)+9x+15HP (DYNES/CM**21//)
                                                                                                                                     252
                                                                                                                             TMPT 253
                                                                                                                             TMPT 254
                                                                                                                             THPT
                                                                                                                             THPT 256
   00 103 [T=1.L
103 WRITE (6.104) T([T].TNINT([OPT.IT)
                                                                                                                             THPT 257
                                                                                                                             TMPT 258
    104 FORMAT (1H ,49%, F9.1,10%, F12.2)
                                                                                                                             TMPT 259
                                                                                                                             TMPT 260
TMPT 261
          GD TO 66
C IF IOPT-LT-11 PLOT ONLY ACQUISTIC RESPONSE OF MODE IMPT
                                                                                                                             TMPT 262
   107 D() 108 J=1.L
108 Y(J) = (-1) * TMINT(10PT.J)
                                                                                                                             TMPT 263
TMPT 264
                                                                                                                             TMPT 265
TMPT 266
                                                                                                                             THPT 267
                                                                                                                             THPT 268
                                                                                                                             TMPT 269
TMPT 270
TMPT 271
                                                                                                                             TMPT 272
TMPT 273
   200 RETURN
          END
                                                                                                                             TMPT 274
```

PROGRAM TMPT

```
TOTINT (SURPOUTINE)
                                                      7/27/68
                                                                                                   TOTE
                                                                                                   TOTE
                         ----ABSTRACT----
                                                                                                   TOTE
  TITLE - TOTINT
                                                                                                   TOT
           THIS SURROUTINE COMPUTES THE TOTAL INTEGRAL
                                                                                                   TOTE
                                                                                                   TOTI
              XINT = INTEGRAL OVER Z FROM O TO INFINITY OF
                                                                                                   TOTI
                                                                                                   TOTE
                      A3(7)*(A1(Z)*F1(Z) + A2(Z)*F2(Z))**2
                                                                                                   Tott
                                                                                            (1)
                                                                                                           10
                                                                                                   TOTE
            THE ATMOSPHERE IS ASSUMED TO BE REPRESENTED IN A MULTILAYER FOR
                                                                                                   TOTI
           WITH AL.A2. AND A3 CONSTANT IN EACH LAYER. THE INTEGRA
EVALUATED AS A SUM OF INTEGRALS OVER INDIVIDUAL LAYERS.
                                                                      THE INTEGRAL IS
                                                                                                   TOTE
                                                                                                           13
                                                                                                   TOTE
                                                                                                   TOTE
            THE FUNCTIONS F1(Z) AND F2(Z) ARE CONTINUOUS ACROSS LAYER
                                                                                                   TOTE
            ROUNDARIES AND SATISFY THE RESTOUAL EQUATIONS
                                                                                                   TOTE
                                                                                                           17
                                                                                                   TOTI
                                                                                                           18
                                                                                                   TOTE
                DF1(7)/D7 = A(1.1)*F1(2) + A(1.2)*F2(2)
                                                                                            124
                                                                                                   TOTE
                NF2171/N7 = A(7.11#F1(2) + A(2.21#F2(2)
                                                                                                   TOT
            WHERE THE FLEPFNTS OF THE MATRIX A (COMPUTED BY SUBROUTINE AAAA
                                                                                                   TOTE
            ARE CONSTANT IN EACH LAYER.
                                                                                                   toti
                                                                                                   TOTI
           THE FUNCTIONS F1(2) AND F2(2) ARE ASSUMED TO SATISFY THE UPPER MODINDARY CONDITION THAT NOTH DECREASE EXPONENTIALLY WITH INCREASING HEIGHT IN THE UPPER HALFSPACE. THE NORMALIZATION
                                                                                                          25
                                                                                                   TOTE
                                                                                                   TOTI
                                                                                                           26
                                                                                                   TOTE
            OF THE FUNCTIONS IS SUCH THAT AT THE LOWER BOUNDARY ZO OF THE
                                                                                                   TOTY
                                                                                                          28
           UPPER HALFSPACE
                                                                                                   TOTE
                                                                                                   TOTI
                                                                                                           30
               F1(70)= -SQRT(G)=A(1.2)
F2(70)= SQRT(G)=(G+A(1.1))
                                                                                            (3A
                                                                                                   TOTI
                                                                                                   TOTE
                                                                                                          32
33
                                                                                                   TOTE
                                                                                                   TOTE
                                                                                                   TOT
                                                                                                           35
               G = SORT(A(1.11+2 + A(1.21+A(2.11)
                                                                                                  TOTI
                                                                                                          36
37
                                                                                                   TOTE
           THE ELEMENTS A(1,1) IN EONS. (3) AND (4) ARE THOSE APPROPRIATE TO THE UPPER MALESPACE. IF G==? IS NEGATIVE, THE PROGRAM RETURNS L=1. OTHERWISE IT RETURNS L=1.
                                                                                                   TOT
                                                                                                   TOTI
                                                                                                          39
4C
                                                                                                   TOTE
                                                                                                   TOTE
  PROGRAM NOTES
                                                                                                   TOT
                                                                                                  TOTE
                    THE INTEGRATION OVER THE UPPER HALFSPACE IS PERFORMED BY
                                                                                                   TOTI
                    CALLING UPINT.
                                        THE INTEGRATIONS OVER THE LAYERS OF FINIT
                                                                                                  TOTE
                    THICKNESS ARE PERFORMED BY CALLING ELINT.
                                                                                                   TOTE
                                                                                                   TOTE
                                                                                                   TOTE
                    THE PARAMETERS A1.A2.A3 DEPEND IN GENERAL ON ANGULAR
                   PREDIENCY THEGA. HUNIZONTAL MAYENUMER COMPONENTS AKX AND AKY. SOUND SPEED C. AND WIND VFLOCITY COMPONENTS VX AND VV. THE FORMULAS USED ARE CONTROLLED BY THE INPUT PARAMETER IT WHICH IS TRANSMITTED TO SUBPOUTINE USEAS.
                                                                                                   TOTE
                                                                                                   TOTE
                                                                                                          50
                                                                                                   TOTT
                                                                                                   TOTI
                                                                                                   TOTE
                                                                                                           53
                   THE PARAMETERS DEFINING THE MULTILAYER ATMOSPHERE ARE
                                                                                                   TOTI
                                                                                                          54
                   PRESUMED STORED IN COMMON
                                                                                                   TOTE
                                                                                                   TOTE
C LANGUAGE
                - FORTRAN IV (360, REFERENCE MANUAL C28-6515-4)
                                                                                                   TOTE
                                                                                                   TOTE
                                                                                                   TOTE
  AUTHOR
                 - A.D.PIFRCE, M.T.T., JULY,1968
                                                                                                   TOTE
                                                                                                          60
                                                                                                   TOTI
                         ----CALLING SEQUENCE----
                                                                                                   TOTE
  SEE SUBROUTINE NAMPDE
                                                                                                   TOTE
        DIMENSION CT(100).VXT(100).VYT(100).HT(100).PHII(100).PHII(100)
COMMON IMAX.CI.VXI.VYI.HI (THESE MUST RE IN COMMON)
                                                                                                   TOTE
                                                                                                          64
                                                                                                   TOTE
        CALL TOTINT (OMEGA-AKX-AKY-IT-L-XINT-PHIL-PHI2)
                                                                                                   TOTE
                                                                                                          66
                                                                                                                PROGRAM
                                                                                                   TOTE
                                                                                                          67
68
                                                                                                                 TOTINT
                         ---- EXTERNAL SUBROUTINES REQUIRED----
                                                                                                   TOTE
                                                                                                                    PAGE
        AAAA. MMMM. CAT. SAT. USFAS. UPINT. FLINT, RRPR
                                                                                                   TOTI
```

```
1101
         AAAA AND BRBR ARE CALLED BY ELINT.
CAI AND SAI ARE CALLED BY BRBR.
                                                                                                                         TOTI
TOTI
                                                                                                                                  72
73
74
75
76
77
                                                                                                                         TOTI
                               ----APGUMENT LIST----
                                                                                                                         TOTE
                                                                                                                         TOTI
TOTI
         OMEGA
                                                 INP
                           R#4
                                                                                                                                  78
79
80
pecceptoceser.
          AKX
                                                 IMP
                                                                                                                         TOTT
                                       ND
ND
                                                                                                                         TOTI
          AKY
                                                 INP
                           [94
[94
[94
[94
                                                 INP
          17
                                                                                                                         TOTI
                                       NO
                                                                                                                         TOTE
                                                 OUT
         XINT
PHI1
                                       NO
                                                 OUT
                                                                                                                         TOTE
                                       100
                                                                                                                                  83
84
85
                                                 INP
                                                                                                                         TOTE
         PH12
                                       100
                                                 INP
                                                                                                                         TOTE
                                                                                                                         TOT
  COMMON STORAGE USED COMMON TMAX.CI.V
                                                                                                                        TOTI
TOTI
                                                                                                                                  86
87
                                    TH.TYV.TX
                                                                                                                         TOTI
                                                                                                                                  89
90
          IMAX
                                                 TNE
                                                                                                                         TOTI
                           R#4
         CI
VXI
                                      100
100
                                                                                                                         TOTE
                                                 INP
                                                                                                                         TOTE
                                                 INP
                                                                                                                                  92
93
94
         VYT
HI
                            R#4
                                       100
                                                                                                                         TOTI
                            ...
                                       100
                                                 INP
                                                                                                                         TOTE
                                                                                                                         TOTE
                                    -INPUTS-
                                                                                                                         TOTE
                                                                                                                         TOTI
                                                                                                                                  96
97
                            =ANGULAR FREQUENCY IN RADIAMS/SEC
=X COMPONENT OF WAVE NUMBER VECTOR IN KM++(-1)
=Y COMPONENT OF WAVE NUMBER VECTOR IN KM++(-1)
=PARAMETER TRANSMITTED TO USEAS DEFINING FUNCTIONAL
DEPENDENCE OF A1.A2.A3 COMPUTED BY USEAS.
=YALUE OF F1 AT BOTTOM OF LAVER I
=VALUE OF F2 AT BOTTOM OF LAVER I
=NUMBER OF ATMOSPHERIC LAVERS WITH FINITE THICKNESS
=SOUND SPEED (KM/SEC) IN I-TH LAVER
=X COMPONENT OF WIND VELOCITY (KM/SEC) IN I-TH LAYER
=THICKNESS IN KM OF I-TH LAYER
         OMEGA
                                                                                                                         TOTE
          AKX
                                                                                                                         TOTI
                                                                                                                         TOTI
                                                                                                                                  99
          11
                                                                                                                         TOTI 100
                                                                                                                         TOT1 101
          PHI1(1)
                                                                                                                         TOTI
          PH12111
                                                                                                                         TOT I
                                                                                                                                103
          IMAY
                                                                                                                         TOTE
                                                                                                                                104
                                                                                                                         TOTI
                                                                                                                                 105
          CHIII
          VXI(I)
                                                                                                                         TOTI
                                                                                                                                 106
         WILL)
                                                                                                                         TOTI
                                                                                                                                107
                                                                                                                         TOTE
                                                                                                                                108
                                                                                                                         TOTI
                                                                                                                                109
                               ---- OUT PUT 5----
                                                                                                                         TOTI 110
                                                                                                                         TOTI
                                                                                                                                111
                             =1 OP -1 DEPENDING ON WHETHER UPPER BOUNDARY CONDITION
                                                                                                                         TOTI
         Ł
                             CAN OR CANNOT BE SATISFIED. SEE SUBROUTINE UPINT =INTEGRAL OVER 7 FROM 0 TO INFINITY AS DEFINED IN THE
                                                                                                                         TOTI 113
                                                                                                                         TOTE
          XINT
                                                                                                                                114
                               ARSTRACT.
                                                                                                                         TOTI
                                                                                                                         TOTE
                                                                                                                         TOTE 117
                               ---- PROGRAM FOLLOWS BELOW----
                                                                                                                         TOT1 118
                                                                                                                         TOTE
                                                                                                                         TOTI 120
          SUBROUTINE TOTINT(OMEGA.AKX.AKY.IT.L.XINT.PHI1.PHI2)
                                                                                                                         TOTE
                                                                                                                                121
                                                                                                                         TOTI
C DIMENSION AND COMMON STATEMENTS
                                                                                                                         TOTI 123
         DIMENSION CI(100).VXI(100).VVI(100).HI(100).EM(2.2)
DIMENSION PHIL(100).PHIZ(100)
                                                                                                                         TOT1 124
TOT1 125
          COMMON IMAX.CT.VXT.VYT.HI
                                                                                                                         TOTI
C COMPUTATION OF CONTRIBUTION FROM UPPER HALFSPACE
                                                                                                                         TOTI 127
                                                                                                                         TOTT 128
                                                                                                                         TOTE
          J= IMAX+1
          C-CIIJ)
                                                                                                                         TOTE
                                                                                                                                130
                                                                                                                         TOTI
                                                                                                                                131
          (L) IXV=XV
                                                                                                                         TOTE
          CALL USFAS IOMEGA.AKX.AKY.C.VX.VY.IT.A1.A2.A31
                                                                                                                         TOT1 133
          CALL UPINT(OMEGA.AKX.AKY.C.VX.VY.A1.A2.L.F1.F2.UINT)
                                                                                                                         TOT1 134
                                                                                                                         TOT1 135
                                                                                                                        TOTI 136
TOTI 137
TOTI 138
C CHECK IF & NEGATIVE
                                                                                                                                         PROGRAM
                                                                                                                                          TOTINT
          IFIL .LT. O) RETURN
THE DENOTE THE CONTRIBUTION ASSULTS BY XINT. AS THE COMPUTATION CONCETINUES, XINT WILL SUCCESSIVELY REPRESENT THE VARIOUS SUSTOTALS UNTIL
                                                                                                                         TOTI
                                                                                                                                139
                                                                                                                                              PAGE
                                                                                                                         TOT: 140
                                                                                                                                                 88
```

```
C CONTRIBUTIONS FROM ALL THE LAYERS HAVE BEEN ADDED IN.
                                                                                                                                    TOTI 141
                                                                                                                                    TOTE 142
TOTE 143
TOTE 144
TOTE 145
           XINT=A3+UINT
C STARY OF DO LOOP
DO 90 1=1.1MAX
J=1MAX+1-1
                                                                                                                                    TOTI 146
TOTI 147
TOTI 148
C COMPUTATION OF CONTRIBUTION FROM J-TH LAYER OF FINITE THICKNESS. C THE CURRENT VALUES F1 AND F2 REPRESENT F1(7) AND F2(2) AT TOP OF
                                                                                                                                    TGTI 149
TGTI 150
TGTI 151
TGTI 152
C J-TH LAYER.
          AX=AX1(1)
C=C1(1)
                                                                                                                                    TOTI 153
TOTI 154
TOTI 155
TOTI 156
           ILTTYV=YV
           H=H1(J)
           CALL USEAS(OMEGA.AKX.AKY.C.VX.VY.IT.A1.A2.A3)
CALL ELINT(OMEGA.AKX.AKY.C.VX.VY.H.F1.F2.A1.A2.AINT)
           XINT=XINT+AINT+A3
                                                                                                                                    TOTI 157
C COMPUTATION OF F1 AND F2 APPROPRIATE TO TOP OF (J-1)-TH LAYER F1 = PHI1(J) 90 F2 = PHI2(J) C END OF DO LOOP
                                                                                                                                    TOTI 158
TOTI 159
TOTI 160
                                                                                                                                    TOT1 161
                                                                                                                                    TOTI 162
TOTI 163
TOTI 164
           RETURN
           FND
                                                                                                                                    TOTE 165
```

PROGRAM TOTINT PAGE 89

* __KANDARKEN NIJE

```
UPINT (SUBROUTINE)
                                                    7/25/68
                                                                                               UPIN
                                                                                               UPIN
                        ----ARSYRACT----
                                                                                               UPIN
C TITLE - UPINT
                                                                                               UPIN
           THIS SUBROUTINE COMPUTES AN INTEGRAL OF THE FORM
                                                                                               UPIN
               UINT - INTEGRAL OVER 7 FROM 20 TO INFINITY OF
                                                                                               HOTM
                                                                                               UPIN
                        (A1*F1(7) + A2*F2(7))**2
                                                                                               UPIN
                                                                                                       10
                                                                                               UPIN
           THE FUNCTIONS FLUZ AND F2(Z) ARE THE SOLUTIONS OF THE COUPLED
           ORDINARY CIFFERENTIAL EQUATIONS
                                                                                               UPIN
                                                                                               UPIN
               DF1/D7 = All+F1 + Al2+F2
DF2/D7 = A21+F1 + A22+F2
C
                                                                                         (2A
                                                                                               UPIN
                                                                                                       16
                                                                                         128
                                                                                               WIN
                                                                                               UPIN
           WHERE THE ELEMENTS OF THE MATRIX A ARE INDEPENDENT OF Z. THE FUNCTIONS F1(Z) AND F2(Z) ARE SUBJECT TO THE UPPER ROUNDARY CONDITION THAT BOTH DECREASE EXPONENTIALLY WITH INCREASING ALTITUDE. SINCE THE MATRIX A IS COMPUTED BY AAAA. INSURING ALZ.2=-A(1,1). ROTH SHOULD VARY WITH HEIGHT AS EXP(-G*(Z-ZO))
CCCCCCCCCC
                                                                                               LIPIN
                                                                                               UPIN
                                                                                                       20
                                                                                               UPIN
                                                                                                       21
22
           WHERE
                                                                                               UPIN
                                                                                                       24
25
                                                                                               UPIN
               G = SORT(A(1.1)**2*A(1.2)*A(2.1))
                                                                                         (3)
                                                                                               UPIN
           IT IS ASSUMED GOOD IS POSITIVE. OTHERWISE LE-1 IS RETURNED.
                                                                                               UPIN
0000
                                                                                               UPIN
                                                                                                       28
           THE EXPLICIT FORMS ADOPTED FOR F1 AND F2 WHICH SATISFY (2) ARE
                                                                                               UPIN
                                                                                                       29
                                                                                               UPIN
                                                                                                       30
               F1 =-SORY(G)+A(1,2)+EXP(-G+(2-20))
                                                                                         {4A
                                                                                               UPIN
               F2 = SORT(G)+(G+A(1.1))+EXP(-G+(Z-20))
                                                                                         14R
                                                                                               UPIN
                                                                                                       32
                                                                                               UPIN
                                                                                                       33
           THUS UINT IS GIVEN BY
                                                                                               UPIN
                                                                                               UPIN
               UINT = ( !- A1 + A(1,2 !+ A2 + (G+A(1,1)) ++2)/2.0
                                                                                        (5)
                                                                                               UPTN
                                                                                                       36
                                                                                               UPIN
                                                                                                       37
                 - FORTRAN IV (360, REFFRENCE MANUAL C28-6515-4)
                                                                                               UPIN
C AUTHOR
                - A.D.PTERCE, M.T.T., JULY.1968
                                                                                                       40
                                                                                               UPIN
                                                                                                       41
                        ----CALLING SEQUENCE----
                                                                                               UPIN
                                                                                               UPIN
  SEE SUBPOUTINE TOTINT
C
  NO DIMENSION STATEMENTS REQUIRED
                                                                                               UPIN
                                                                                                       45
       CALL UPINTIOMEGA.AKX.AKY.C.VX.VY.A1.A2.L.F1.F2.UINTI
                                                                                               UPIN
                                                                                               UPIN
                        --- EXTERNAL SUBROUTINES REQUIRED----
                                                                                                       48
                                                                                               UPIN
       ...
                                                                                               UPIN
                                                                                               UPIN
                        ---- ARGUMENT LIST----
                                                                                                       52
                                                                                               UPIN
        OMEGA
                                       INP
                                                                                               UPIN
                                                                                               UP IN
UP IN
       AKY
R 44
                               ND
                                       IMP
                      R #4
                                       INP
                               ND
                                                                                                       56
57
        Č
                                                                                               UPIN
                               ND
                                       INP
        ٧x
                      R+4
                               ND
                                       INP
                                                                                               UPIN
                              ND
ND
                                                                                               UPIN
       VY
                                      INP
       AI
                                      INP
                                                                                                       60
       AZ
                               ND
                                       INP
                                                                                               UPIN
                      104
                               M
                                      NUT
                                                                                               UPIN
       L
F1
                      R+4
                                                                                               UPIN
                              ND
                                      OUT
                                                                                                      63
                              ND
                                      OUT
                                                                                                       64
                                                                                               UPIN
                                                                                               UPIN
                                                                                                            PROGRAM
  NO COMMON STORAGE USED
                                                                                                      67
                                                                                                              UPINT
                                                                                               UPIN
                        ----INPUTS----
                                                                                               UPIN
                                                                                                               PAGE
                                                                                               HPIN
                                                                                                                  90
```

```
*ANGULAR FREQUENCY IN RADIANS/SEC
                                                                                                                          UPIN
          ONEGA
                             ** COMPONENT OF WAVE NUMBER VECTOR IN KM**(-1)
**Y COMPONENT OF WAVE NUMBER VECTOR IN KM**(-1)
                                                                                                                          UPIN
00000
                                                                                                                                    73
          AKY
                                                                                                                          UPIN
                             SOUND SPEED IN KM/SEC

X COMPONENT OF WIND VELOCITY IN KM/SEC

Y COMPONENT OF WIND VELOCITY IN KM/SEC
                                                                                                                                    74
75
                                                                                                                          UPIN
          C
          ٧x
                                                                                                                          UPIN
                                                                                                                                    76
                             =COEFFICIENT OF F1(Z) IN INTEGRAND
=COEFFICIENT OF F2(Z) IN INTEGRAND
                                                                                                                          UPIN
                                                                                                                                    77
( c c c
                                                                                                                          UPIN
                                                                                                                                    78
          42
                                                                                                                          UPIN
                               ----OUTPUTS----
                                                                                                                          UPIN
                                                                                                                                    50
                                                                                                                          UPIN
                                                                                                                                    81
#1 OP -1 DEPENDING ON WHETHER UPPER ROUNDARY CONDITION OF F1(2).F2(2) DECREASING EXPONENTIALLY WITH INCREASI HEIGHT CAN OR CANNOT BE SATISFIED. IT REPRESENTS THE SIGN OF G**2 WHERE G IS DEFINED IN THE ABSTRACT.

#VALUE OF F1(7) AT BOTTOM OF HALFSPACE, DEFINED AS -SORT(G)*A(1.2) FROM EON. (4A).

#VALUE OF F2(2) AT ROTTOM OF HALFSPACE, DEFINED AS SORT(G)*(G+A(1.1)) FROM EON. (4A).

#THE INTEGRAL DEFINED BY EONS. (1) AND (5) IN THE
                                                                                                                          UPIN
                                                                                                                                   82
83
                                                                                                                          UPIN
                                                                                                                          UPIN
                                                                                                                          UPIN
                                                                                                                                    85
                                                                                                                          UPTN
                                                                                                                                   86
87
                                                                                                                          UPIN
                                                                                                                          UPIN
                                                                                                                                    88
                                                                                                                          UPIN
                                                                                                                                    89
                              #THE INTEGRAL DEFINED BY EONS. (1) AND (5) IN THE
          UINT
                                                                                                                          UPIN
                                                                                                                                    90
                                                                                                                          UPIN
                                                                                                                                    91
                               ABSTRACT
                                                                                                                          UPIN
                                                                                                                          UPIN
000
                               ----PROGRAM FOLLOWS BELOW----
                                                                                                                          UPIN
                                                                                                                                    94
                                                                                                                          UPIN
                                                                                                                                    95
                                                                                                                          UPIN
                                                                                                                                    96
          SURFRUITINE UPINT (OMEGA. AKX. AKY. C. VX. VY. A1. A2. L. F1. F2. UINT)
                                                                                                                          UPIN
                                                                                                                                    97
          DIMENSION A(2.2)
                                                                                                                          UPIN
                                                                                                                                    98
                                                                                                                          UPIN
                                                                                                                                    99
C COMPUTATION OF A MATRIX AND OF X=G**2
                                                                                                                          UPIN 100
         CALL AAAA(OMEGA.AKX.AKY.C.VX.VY.A)
                                                                                                                          UPIN 101
                                                                                                                          UPIN 102
UPIN 103
          X=A(1.1)**2+A(1.7)*A(2.1)
C CHECK ON SIGN OF X
2 IF( X .GT. 0.0 ) GO TO 3
                                                                                                                          UPIN 104
                                                                                                                          UPIN 105
                                                                                                                          UPIN 106
C X IS NEGATIVE
                                                                                                                          UPIN 107
UPIN 108
          L=-1
          RETURN
C CONTINUING FROM 2 WITH X POSITIVE
                                                                                                                          UPIN 109
       3 L=1
                                                                                                                          UPIN 110
          G=SORT(X)
                                                                                                                          UPIN 111
          GRT=SORT(G)
                                                                                                                          UPIN 112
          F1=-GRT=4(1,2)
                                                                                                                          UPIN 113
F2=GRT=(G+A(1.1))
C COMPUTATION OF UINT
                                                                                                                          UPIN 114
UPIN 115
                                                                                                                          UPIN 116
          UINT= (-A1+A(1.2)+A2+(G+A(1.11))++2/2.0
          RETURN
          END
                                                                                                                          UPIN 118
```

- ANT THE PROPERTY OF THE PERSON OF THE PERS

PROGRAM UPINT PAGE

```
USEAS (SUBROUTINE)
                                                                               7/25/68
C
                                                                                                                                               USEA
                                                                                                                                               USEA
                                    ----ARSTRACT----
                                                                                                                                               USEA
C TITLE - USEAS
                                                                                                                                               USEA
                 THE PURPOSE OF THIS SUBROUTINE IS TO COMPUTE THE NUMBERS AL, AZ AND AS WHICH DEPEND ON ANGULAR FREQUENCY ONEGA, HORIZONTAL MAYE NUMBER COMPONENTS AKX AND AKY, THE SOUND SPEED C, AND THE WIND SPEED COMPONENTS YX AND YY. THE INTEGER IT DETERMINES WHICH FORMULAS ARE USED FOR AL, AZ, AND AS ACCORDING TO THE FOLLOWING
                                                                                                                                              USFA
                                                                                                                                               USEA
                                                                                                                                               USFA
                                                                                                                                              USFA
                                                                                                                                               USEA
                                                                                                                                               USEA
                       (11)
                                            CAT 1
                                                                (A2)
                                                                                                  (A3)
                                                                                                                                                          13
14
15
                                                                                                                                              HISEA
                                                                                                                                              USEA
                                                n
                                                                                                                                               USEA
                                                                                      BDM+(KDOTY)/(C++2+K)
                                                                   0
                                                                                                                                               USFA
                                                                   ō
                                                                                                                                               USEA
                                                                                       VX+BOM/C++2
                                                                 -C
-C
                                                                                                                                              USEA
                                                                                       VY+BDM/C++2
                                                                                                                                                          20
                                                                                      K+OMEGA/80M++3
1.0/80M++2
                                            6/C
6/C
                                                                                                                                               USEA
                                                                                       K++2/80M++3
                                                                                      VX+K++2/80M++3
VY+K++2/80M++3
                                                                                                                                              USEA
USEA
                                                                                                                                                          24
25
                         10
                                                                                                                                               USEA
                HERE BOM=OMEGA-KDOTY IS THE DOPPLER SHIFTED ANGULAR FREQUENCY. KDGTV=AKX*VX+AKV*VY IS THE DOT PRODUCT OF MAVE NUMBER WITH THE WIND VELOCITY. AND R=SQRT(AKX**2*AKY**2) IS THE MAGNITUDE OF THE MAVE NUMBER VECTOR. THE ACCELERATION OF GRAVITY G IS TAKEM AS .0098 KM/SEC**2 IN THE COMPUTATION. COMPUTED VALUES SHOULD BE IN KM.SEC SYSTEM OF UNITS.
                                                                                                                                               USEA
                                                                                                                                              USEA
                                                                                                                                                          28
                                                                                                                                              USEA
                                                                                                                                               USEA
                                                                                                                                              USEA
                                                                                                                                              USEA
C LANGUA
                        - FORTRAN 1V (360. REFERENCE MANUAL C28-6515-4)
- A.D.PIERCE, M.I.T., JUNE,1968
   LANGUAGE
                                                                                                                                              USEA
USEA
USEA
                                                                                                                                                          35
                                    ----CALLING SEQUENCE----
                                                                                                                                              USEA
   SEE SUBROUTINE TOTINT
           NO DIMENSION STATEMENTS ARE REQUIRED
                                                                                                                                              USEA
   CALL USEAS(OMEGA.AKX.AKY.C.VX.VY.IT.A1.A2.A3)
A1.A2.A3 ARE NOW AVAILABLE FOR FUTURE COMPUTATIONS
                                                                                                                                              USEA
                                                                                                                                               USEA
   NO EXTERNAL LIBRARY SUBROUTINES ARE REQUIRED
                                                                                                                                              USEA
                                                                                                                                              USEA
                                                                                                                                                          46
47
                             ----ARGUMENT LIST----
                                                                                                                                               USEA
                                                                                                                                              USEA
           OMEGA
                                 R 44
                                                          IND
                                 R#4
                                                                                                                                              USEA
                                                          INP
           AKX
                                              ND
           AKY
                                 R#4
                                              ND
                                 R 94
                                              ND
                                                          INP
                                                                                                                                              USEA
                                 R=4
           VX
                                              ND
                                                          INP
                                                                                                                                              USEA
                                              NO
                                                          INP
                                                                                                                                              USEA
            ٧٧
            IT
                                 1+4
                                              ND
                                                          INP
                                                                                                                                               USEA
                                                                                                                                              USEA
                                                                                                                                                         56
57
                                 244
                                              ND
                                                         OUT
                                                                                                                                              USEA
                                                         DUT
           12
                                              ND
                                                         OUT
                                                                                                                                              USEA
                                                                                                                                                          59
                                                                                                                                              USEA
                                                                                                                                                          60
   NO COMMON STORAGE USED
                                                                                                                                              USEA
                                    ---- INPUTS----
                                                                                                                                              USEA
                                                                                                                                              USEA
                                                                                                                                                          63
                                                                                                                                              USEA
                                  -ANGULAR FREQUENCY IN RAD/SEC
           OMEGA
                                  -ANGULAR FREQUENCY IN RAD/SEC

=X COMPONENT OF MAVE NUMBER VECTOR IN KM++(-1)

-Y COMPONENT OF MAVE NUMBER VECTOR IN KM++(-1)

-SOUND SPEED IN KM/SEC

-X COMPONENT OF WIND VELOCITY IN KM/SEC

-Y COMPONENT OF WIND VELOCITY IN KM/SEC

-CONTROL PARAMETER FOR SELECTION OF FORMULAS (SEE
                                                                                                                                              USEA
           AFX
           AKY
                                                                                                                                              USEA
                                                                                                                                                         66
                                                                                                                                                                 PROGRAM
           C
VX
                                                                                                                                              USEA
                                                                                                                                                         67
                                                                                                                                                                     USEAS
                                                                                                                                              USEA
                                                                                                                                                         68
                                                                                                                                              USEA
                                                                                                                                                                       PAGE
                                                                                                                                              USFA
                                                                                                                                                                           92
```

```
USEA
                          ABSTRACT).
                                                                                                     USEA
0000000000
                          ----OUTPUTS----
                                                                                                     USEA
                         =PARAMETER DEFINED BY FORMULAS IN ABSTRACT
=PARAMETER DEFINED BY FORMULAS IN ABSTRACT
=PARAMETER DEFINED BY FORMULAS IN ABSTRACT
                                                                                                     USEA
                                                                                                     USFA
                                                                                                     USEA
                                                                                                     USEA
                          ----PROGRAM FOLLOWS BELOW----
                                                                                                      USEA
                                                                                                      USEA
C
         SUBROUTINE USEAS COMEGA. AKX. AKY. C. VX. VY. IT. A1. A2. A3)
                                                                                                      USEA
C WE ASSIGN VALUES TO AL.AZ.A3 WHICH WILL NOT NECESSARILY BE THEIR EXIT
                                                                                                      USEA
                                                                                                      IISFA
                                                                                                              86
C VALUES.
                                                                                                      USEA
                                                                                                      USEA
USEA
USEA
         A2=0.0
                                                                                                              89
A2=0.0
A3=1.0
C IF IT IS 1. THESE ARE CORRECT. HOMEVER.
IF(IT .EQ. 1) RETURN
IF(IT .GT. 2) GO TO ZOO
                                                                                                      USEA
                                                                                                      USEA
                                                                                                      USEA
 C IT IS 2. THE CURRENT VALUES ARE 1.0.1. HE CHANGE THE FIRST TWO.
                                                                                                      USEA
         A1=0.0
A2=1.0
                                                                                                      USEA
USEA
USEA
USEA
          RETURN
 USEA
                                                                                                             101
                                                                                                       USEA 102
 BON-DMEGA-AKY
AK-SORT(AKSO)
C THE CURRENT VALUES OF A1.A2.A3 ARE STILL 1.0.1.
[F(IT .GT. 3) GO TO 300
                                                                                                       USEA 103
                                                                                                       USEA 104
                                                                                                       USEA 105
                                                                                                       USEA 106
                                                                                                       USEA 107
  C IT IS EQUAL TO 3. ONLY AS NEED BE CHANGED.
AS=BOM=AKY/(C==2+AK)
                                                                                                       USEA 108
                                                                                                       USEA 109
USEA 110
          RETURN
  C IT IS 4 OR GREATER. WE SET AS TO VALUE APPROPRIATE FOR IT=4.
                                                                                                       USEA 111
USEA 112
USEA 113
     300 A3-ROM/C++2
  300 A3=RDM/C==2
C THE CURRENT VALUES OF A1 AND A2 ARE 1 AND 0
IF(IT .E0. 4) RETURN
IF(IT .E0. 5) A3=VX*A3
IF(IT .E0. 5 .OR. IT .E0. 6) RETURN
                                                                                                       USEA 114
USEA 115
                                                                                                        USEA 116
                                                                                                        USFA 117
                                                                                                       USEA 118
USEA 119
  C IT IS 7 OR LARGER
                                                                                                       USEA 120
USEA 121
           Al=. 0098/C
           AZ=-C
                                                                                                        USEA 122
  C THE ONLY QUANTITY WE NEED DETERMINE IS AS
                                                                                                        USFA 123
                                                                                                        USEA 124
                                                                                                        USEA 125
           IF(IT .GT. 7) GO TO 700
                                                                                                        USEA 126
  C 11=7
                                                                                                        USEA 127
           A3=AK+NMFGA/BNM++3
                                                                                                        USEA 120
           RETURN
                                                                                                        USEA 129
                                                                                                        USFA 130
   C
      700 IF(IT .GT.8) GO TO 800
                                                                                                        USEA 131
      TT=8
                                                                                                        USEA 132
           A3=1.0/80M=+2
                                                                                                        USEA 133
USEA 134
           RETURN
   C FOR IT=9.10.11 WE NEED THE FACTOR AKSQ/BOM##3
BOO A3=AKSQ/BOM##3
IF(IT .E9. 4) RETURN
IF(IT .GT. 10) GO TO 1000
                                                                                                         USEA 135
                                                                                                                      PROGRAM
                                                                                                        USEA 136
USEA 137
                                                                                                                         USFAS
                                                                                                         USEA 138
                                                                                                                          PAGE
                                                                                                         USEA 139
   C 1T=10
A3=VX=A3
                                                                                                                             93
                                                                                                         USEA 140
```

PROPERTY OF THE PROPERTY OF TH

RETURN
C
C IT=11 (YOU SHOULDN-T INPUT IT FOR VALUES OUTSIGF RANGE OF 1 TC 11.)
1000 A3=YY=A3
RETURN
FND
USEA 141
USEA 143
USEA 144
USEA 145
USEA 146

PROGRAM USEAS PAGE 94

```
WIDEN (SUBPROUTINE)
                                                       6/19/68
                                                                                                   WIDE
                                                                                                    WIDE
                                                                                                    WIRE
                                                                                                             3
                           ---- ARSTRACT----
                                                                                                    MIDE
                                                                                                    WIDE
  TITLE - WIDEN
                                                                                                    MIDE
            WIDEN MATRIX INMODE BY ADDING KW COLUMNS BETWEEN COLUMNS NI AND
                                                                                                   WIDE
C.
            N1+1
                                                                                                   WIDE
                                                                                                    MIDE
                    WIDEN ADDS KW ELEMENTS TO THE VECTOR OF ANGULAR FREQUENCI
                                                                                                   WIDE
                                                                                                           10
                    MIDEN AUDS RW ELEMENTS TO THE VECTOR OF ANGULAR PREDUENCE
OM . DEVIDING THE INTERVAL BETWEEN OM(NI) AND OM(NI+1) IN
KW-I EQUAL PARTS. FOR EACH NEW ANGULAR FREQUENCY, A NEW
COLUMM IS ADDED TO THE INMODE MATRIX (DEFINED IN SUBROU-
TINE MPOUT). INMODE IS STORED IN VECTOR FORM. COLUMN AFT
                                                                                                   MIDE
                                                                                                   MIDE
                                                                                                           13
                                                                                                   WIDE
                                                                                                           15
                    COLUMN.
                                                                                                   WIDE
                                                                                                           16
                                                                                                    WIDE
C LANGUAGE
                 - FORTRAN IV (360, REFERENCE MANUAL C28-6515-4)
                                                                                                   WIDE
                                                                                                   WIDE
                                                                                                           18
C AUTHORS
                                                                                                           19
                 - A.C.PIERCE AND J.POSEY. M.I.T., JUNE.1968
                                                                                                   MIDE
                                                                                                   WIDE
                                                                                                           20
                           ----USAGE----
                                                                                                   WIDE
                                                                                                   WIDE
                                                                                                           23
        OM. V. INHODE MUST BE DIMENSIONED IN CALLING PROGRAM
                                                                                                   MIDE
        THE ONLY SUBROUTINE CALLED IS NHOFN. DESCRIBED ELSEWHERE IN THIS
                                                                                                   HIDE
                                                                                                   WIDE
C FORTRAN USAGE
                                                                                                   MIDE
                                                                                                           28
                                                                                                           29
       CALL WIDEN(OM.V. INMODE.NOM.NOMP.NVP.N1.KW.THETK)
                                                                                                   MIDE
                                                                                                   MIDE
                                                                                                           30
                                                                                                   WIDE
                                                                                                   MIDE
                                                                                                           32
                    VECTOR WHOSE ELEMENTS ARE THE VALUES OF ANGULAR FREQUENCY
C
      04
                                                                                                   MIDE
                                                                                                           33
34
         R#4(D)
                    CORRESPONDING TO THE COLUMNS OF MATRIX INMODE. (RAD/SEC)
                                                                                                   WIDE
                                                                                                   WIDE
                    VECTOR WHOSE ELEMENTS ARE THE VALUES OF PHASE VELOCITY CORRESPONDING TO TEL ROMS OF MATRIX INMODE. (KM/SEC)
        R#4(D)
                                                                                                   WIDE
                                                                                                           37
                                                                                                   WIDE
                                                                                                           38
      INMORE
                    EACH ELEMENT OF THIS MATRIX CORRESPONDS TO A POINT IN THE
                                                                                                   MIDE
                    PREQUENCY (OM: - PHASE VFLOCITY (V) PLANE. IF THE NORMAL MODE DISPERSION FUNCTION (FPP. FOUND BY CALLING SUBROUTIN NMORN) IS POSITIVE AT THAT POINT. THE ELEMENT IS +1. IF FPP IS NEGATIVE, THE ELEMENT IS -1. IF FPP DOES NOT EXIST THE ELEMENT IS 5. INMODE IS STORED IN VECTOR FORM. COLUM
         144(0)
                                                                                                           40
                                                                                                   MIDE
                                                                                                   WIDE
                                                                                                   WIDE
                                                                                                           42
                                                                                                   WIDE
                                                                                                           43
                                                                                                   WIDE
                    AFTER COLUMN.
C
                                                                                                   WIDE
                                                                                                   WIDE
                    NUMBER OF ELEMENTS IN OM (AND NO. OF COLUMNS IN INMODE)
      NOM
                                                                                                   WIDE
                                                                                                           47
                    WHEN WIDEN IS CALLED.
         144
                                                                                                           48
                                                                                                   WIDE
                    NUMBER OF FLEMENTS IN V (AND NO. OF ROWS IN INMODE).
      NVP
                                                                                                   WIDE
         1+4
00000
                                                                                                   WIDE
                                                                                                           50
                                                                                                   MIDE
                    NUMBER OF INMODE COLUMN IMMEDIATELY LEFT OF SPACE IN WHIC
      NI
                                                                                                   MIDE
                                                                                                           52
                    NEW COLUMNS ARE TO BE ADDED.
                                                                                                           53
         1+4
                                                                                                   WIDE
                                                                                                   WIDE
                                                                                                   MIDE
                    NUMBER OF COLUMNS TO BE ADDED TO INMODE.
                                                                                                   WIDE
                                                                                                           56
                                                                                                           57
                                                                                                   MIDE
      THETK
                    PHASE VELOCITY DIRECTION MEASURED COUNTER-CLOCKWISE FROM
                                                                                                   WIDE
                                                                                                           58
                    X-AXIS (RADIANS).
                                                                                                   WIDE
                                                                                                   WIDE
                                                                                                           60
  OUTPUTS
                                                                                                   MIDE
                                                                                                           61
                                                                                                   WIDE
                                                                                                           62
      THE OUTPUTS ARE NOMP (= NOM + KM = THE NEW NUMBER OF ELFRENTS IN OM
                                                                                                   WIDE
                                                                                                           63
       AND THE NEW NUMBER OF COLUMNS IN INMODE) AND REVISED VERSIONS OF OM
                                                                                                   WIDE
       AND INMODE.
                                                                                                   WIDE
                                                                                                           65
                                                                                                   WIDE
                                                                                                           66
67
                                                                                                                 PRCGRAM
                                                                                                   WIDE
                                                                                                                   WIDEN
                          ---- EXAMPL F----
                                                                                                   WIDE
                                                                                                           69
                                                                                                   WIDE
                                                                                                                    PAGE
      SUPPOSE OM = 1.0.2.0.3.0 AND WIDEN IS CALLED WITH KW = 3. AND N1 =
                                                                                                   WIDE
                                                                                                                       95
```

MANUFACTURE CONTRACTOR
```
2. THEN UPON RETURN TO CALLING PROGRAM. ON = 1.0.2.0.2.25.2.5.2.75. 3.0. NONP = 6. AND INMODE WILL HAVE THREE NEW ROWS CORRESPONDING TO THE NEW ELEMENTS OF DM.
                                                                                            WIDE
                                                                                            WIDE
                                                                                             MIDE
                                                                                            WIDE
                                                                                             WIDE
                         ---- PROGRAM FOLLOWS BELOW----
                                                                                             WIDE
C
                                                                                            WIDE
                                                                                             MIDE
       SUBPOUTINE WIDENCOM. V. I MMODE. NOM. NOMP. NVP. N1. KW. THETK I
                                                                                             WIDE
٤
                                                                                             WIDE
C VARIABLE DIMENSIONING
                                                                                             MIDE
       COMMON IMAX.CI(100).VXI(100).VVI(100).HI(100)
                                                                                             WIDE
                                                                                             WIDE
                                                                                             WIDE
C INTERVAL AT WHICH NEW VALUES OF OM ARE BE PLACED BETWEEN OM(N1) AND C OM(N1+1) IS DETERMINED.
                                                                                                    85
                                                                                             WIDE
                                                                                             WINE
       DELOM=("M(N1+1)-UM(N1))/(KW+1)
                                                                                             MIDE
                                                                                             MIDE
C NOMP IS NUMBER OF ELEMENT IN EXPANDED OF
                                                                                             WIDE
                                                                                             WIDE
                                                                                             MIDE
C NSTART IS THE NUMBER OF THE ELEMENT IN THE NEW ON WHICH CORRESPONDS TO C FLEMENT NI+1 IN THE CLD OM VECTOR NSTART=N1+1+KW
                                                                                            WIDE
                                                                                             WIDE
                                                                                            WIDE
. MOVE ALL ELEMENTS OF OM BEYOND ELEMENT NI TO THEIR NEW POSITIONS. BEGI
                                                                                            WIDE
                                                                                             MIDE
       DO 90 NJ=NSTART.AOMP
                                                                                             WIDE
       (TRATZH-LM)-9MOM=L
                                                                                             MIGE
                                                                                                    99
       JOFU-1-KM
                                                                                            WIDE 100
C MOVE COLUMN JOLD OF INMODE INTO POSITION FOR COLUMN J OM(J)=0M(J)LD)
                                                                                             WIDE 101
                                                                                            MIDE 102
                                                                                            WIDE 103
       10 40 TP=1.NVP
                                                                                             WIDE 104
       []=(]=1)=NVP+(NVP-IP) + 1
[]NLD=(]NLD=1)=NVP+(NVP-IP) + 1
INMODE([])=INMODE([]OLD)
                                                                                             WIDE 105
                                                                                            WIDE 106
                                                                                             WIDE 107
   40 CONTINUE
                                                                                            WIDE 109
C NSTART IS NUMBER OF FIRST NEW COLUMN
                                                                                            MIDE 110
       NSTART=N1+1
                                                                                            WIDE 111
                                                                                            WIDE 112
C NEND IS NUMBER OF LAST NEW COLUMN
                                                                                            WIDF 113
       NEND=N1+KW
                                                                                            WIDE 114
                                                                                            WIDE 115
                                                                                            WIDE 116
C NEW VALUES OF OM ARE ESTABLISHED
       OMEGA-OMEN1 )
                                                                                            WIDE 117
       OR 190 JENSTAPT.NEND
                                                                                             WIDE 119
       OMEJE-OMEGA + DELOM
                                                                                             WIDE 119
       OMEGA = OM(J)
DO 190 I=1.NVP
                                                                                             WIDE 120
                                                                                            WIDE 121
                                                                                            WIDE 122
  IJ IS MUMBER OF FLEMENT IN VECTOR REPRESENTATION OF INMODE WHICH IS
                                                                                             WIDE 123
C ELFMENT J IN ROW I OF INMODE IJ=(J-1)=NVP+I
                                                                                            WIDE 124
WIDE 125
       VPHSE=V(1)
                                                                                            WIDE 126
                                                                                            WIDE 127
WIDE 128
C CALL NMOFN TH EVALUATE THE NORMAL MODE DISPERSION FUNCTION (FPP)
CALL NMOFN (OMEGA, VPHCF, THETK, L, FPP, K)
                                                                                            WIDE 129
                                                                                            WIDE 130
  IF FPP DOFS NOT FXIST L =
                                                                                            WIDE 131
       1Ft 1 .FQ. -1 1 GO TO 150
                                                                                            WIDE 132
                                                                                            WIDE 133
C IF FPP DOES FXIST ( * 1 AND INMODELLY) = (FPP/ARS(FPP))
                                                                                            WIDE 134
                                                                                            WIDE 135
WIDE 136
       INMODELIUS = 1
                                                                                                         PROGRAM
        IF (FPP.LF.O.O) INMODELIAL = -1
       GO TO 180
                                                                                            WIDE 137
                                                                                                           HIDEN
   150 INMODELLUT=5
                                                                                            WIDF 138
WIDF 139
                                                                                                            PAGE
  180 CONTINUE
   190 CONTINUE
                                                                                            WIRE 140
```

RETURN FND

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WIDE 141 WIDE 142

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PROGRAM WIDEN

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13 ARCTRACT					

A computer program is described which enables one to compute the pressure waveform at a distant point following the detonation of a nuclear explosion in the atmosphere. The theoretical basis of the program and the numerical methods used in its formulation are explained; a deck listing and instructions for the program's operation are included. The primary limitation on the program's applicability to realistic situations is that the atmosphere is assumed to be perfectly stratified. However, the temperature and wind profiles may be arbitrarily specified. Numerical studies carried out by the program show some discrepancies with previous computations by Harkrider for the case of an atmosphere without winds. These discrepancies are analyzed and shown to be due to different formulations of the source model for a nuclear explosion. Other numerical studies explore the effects of various atmospheric parameters on the waveforms. In the remainder of the report, two alternate theoretical formulations of the problem are described. The first of these is based on the neglect of the vertical acceleration term in the equations of hydrodynamics and allows a solution by Cagniard's integral transform technique. The second is based on the hypothesis of propagation in a single guided mode and permits a study of the effects of departures from stratification on the waveforms.

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